

# Physics Opportunities and Site Requirements for 2<sup>nd</sup> and 3<sup>rd</sup> generation Noble Liquid detectors for direct Dark Matter Search

Davide D'Angelo

Universita degli Studi and INFN Milano (Italy)

3<sup>rd</sup> Town Meeting – Monterey, CA – 8<sup>th</sup> Sep 2013

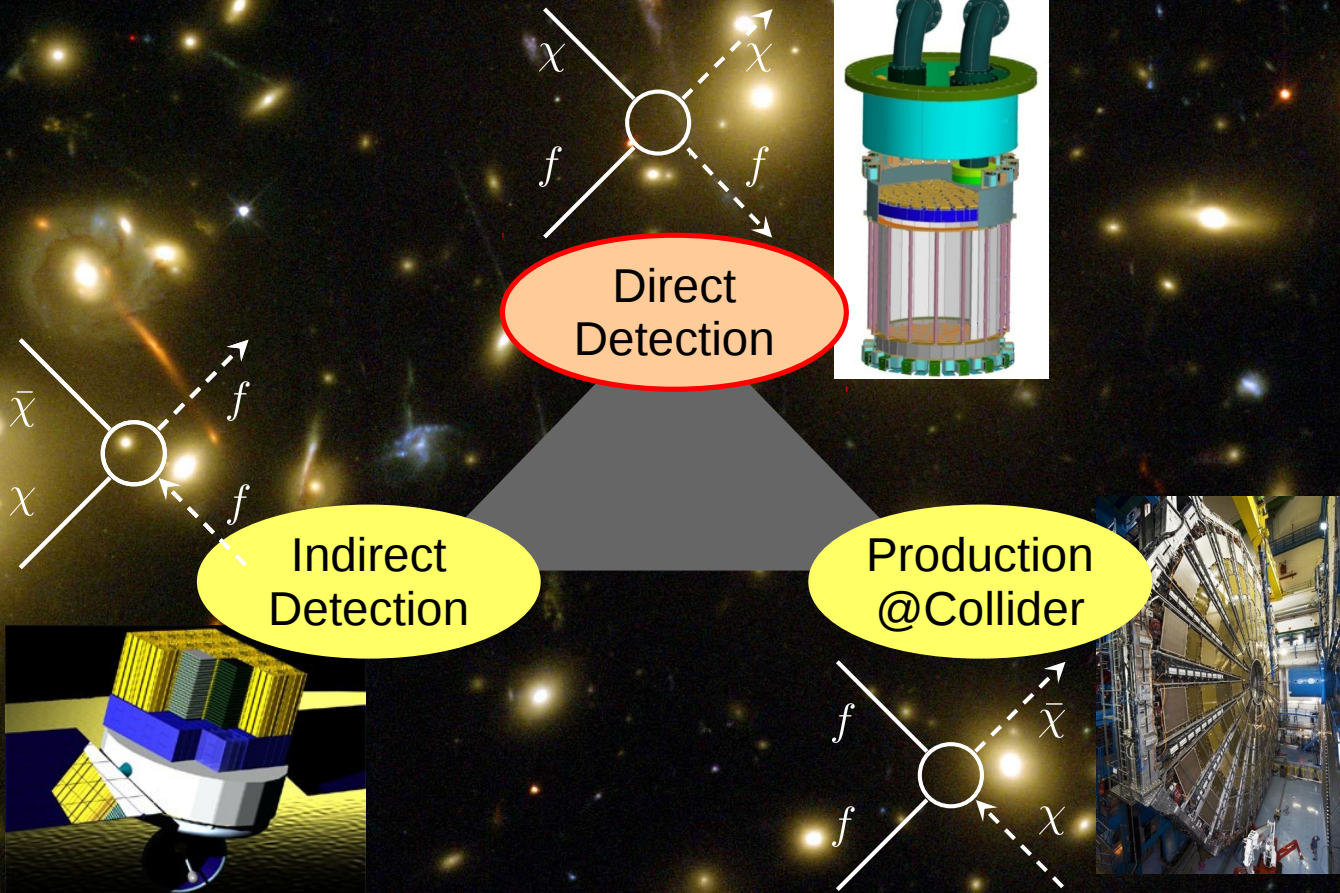


# Outline

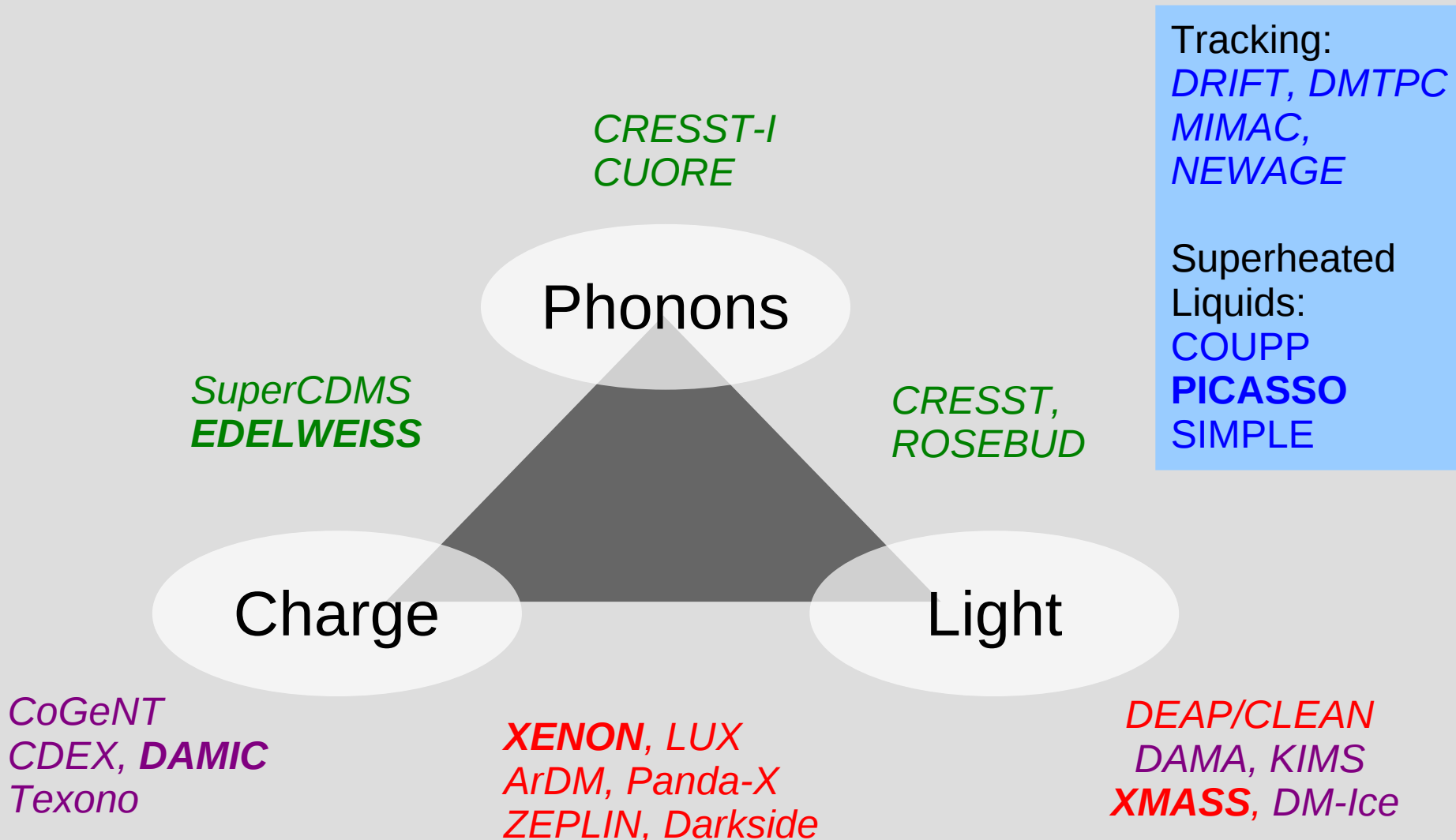
- ⊗ Introduction
- ⊗ Noble gases
- ⊗ Single or double phase
- ⊗ Current projects ArDM, DarkSide, Xenon, DEAP/  
miniCLEAN, XMASS, LUX
- ⊗ G2 scale-up
- ⊗ G3 scale-up
- ⊗ Cosmogenic backgrounds

# Complementary approaches

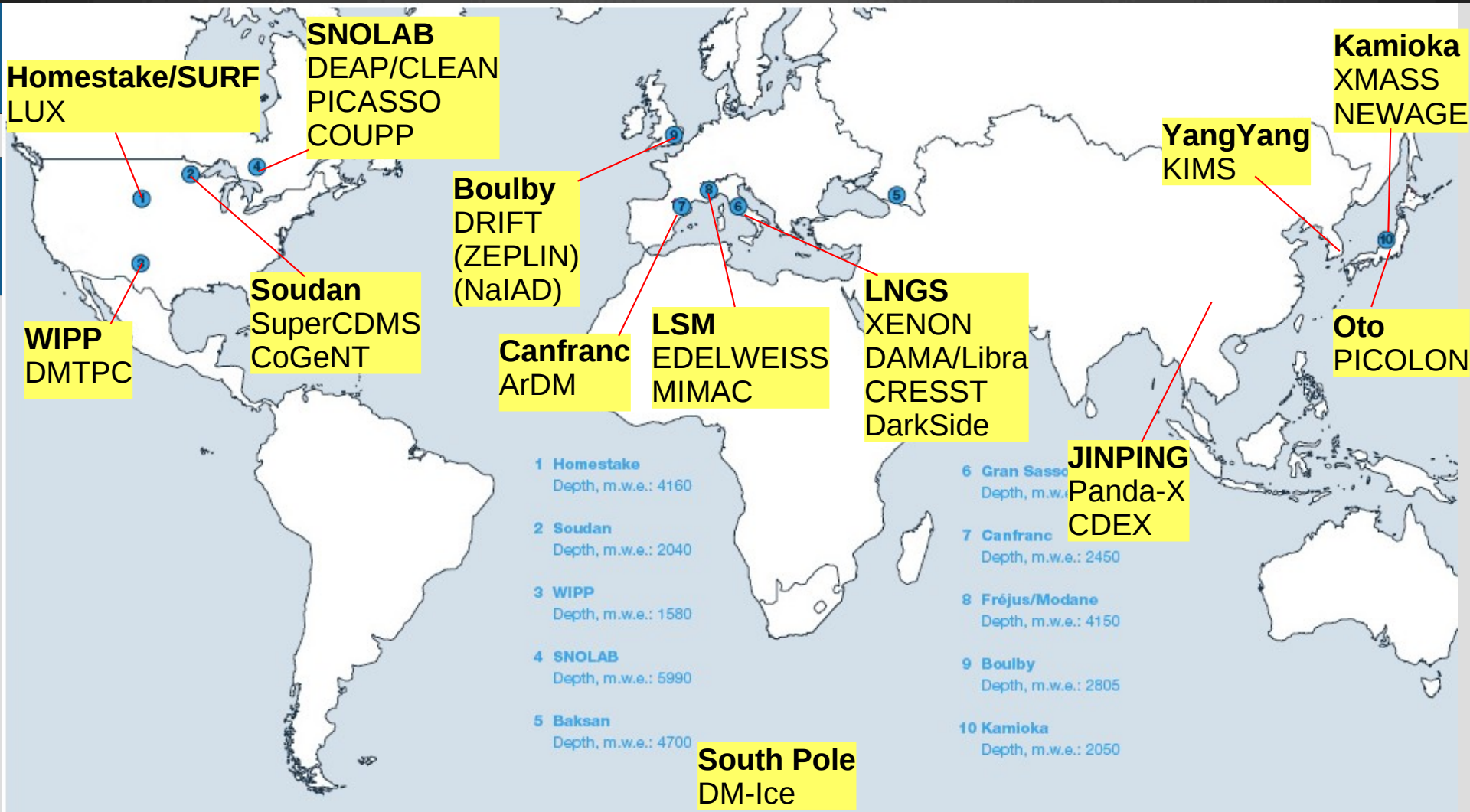
## Dark Matter Search



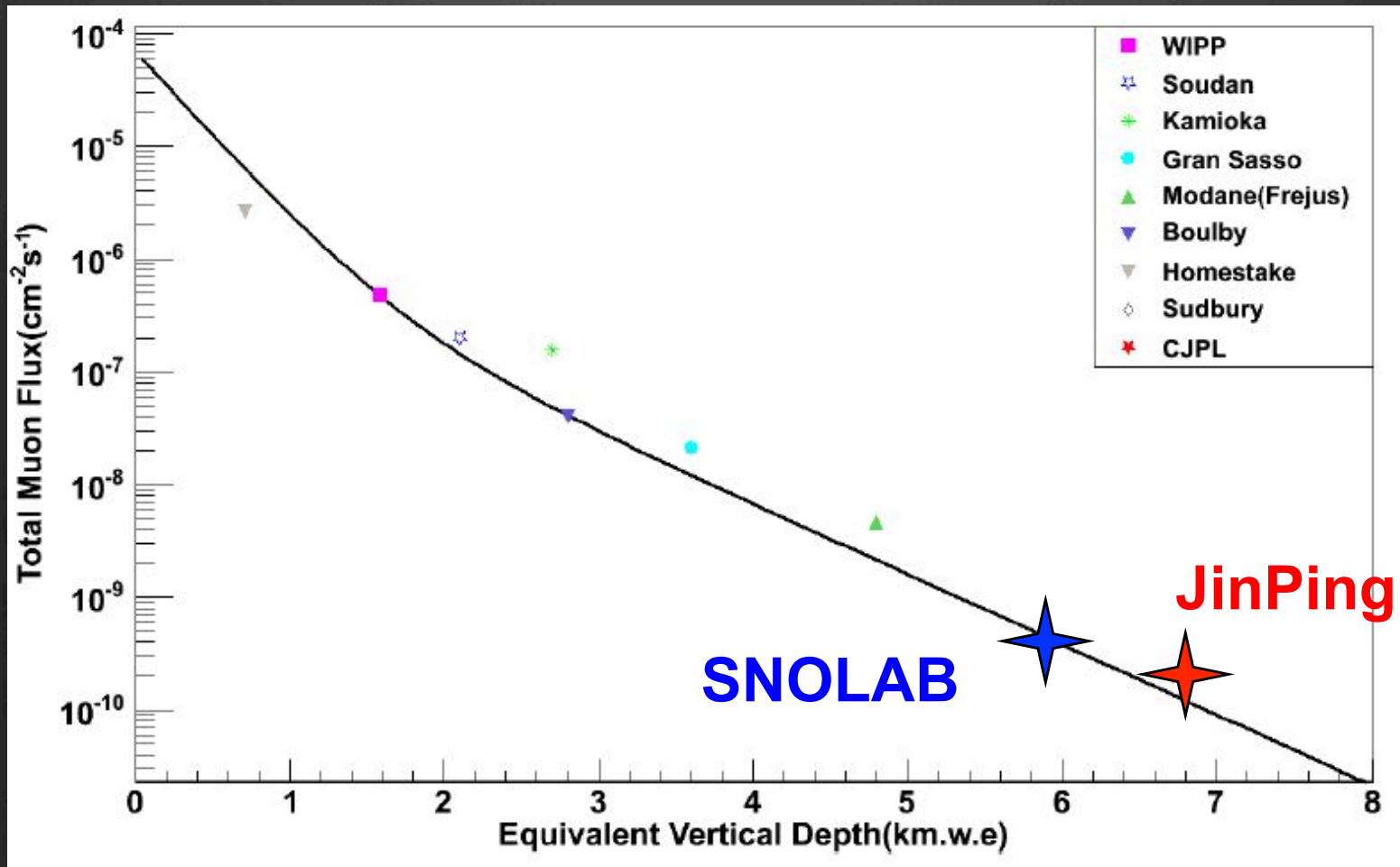
# WIMP signature



# Underground projects



# Underground laboratories



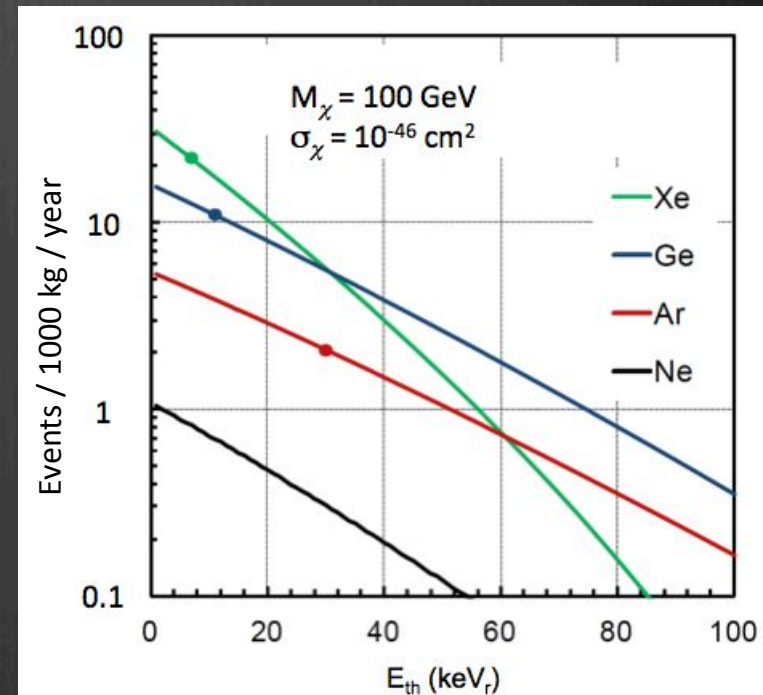
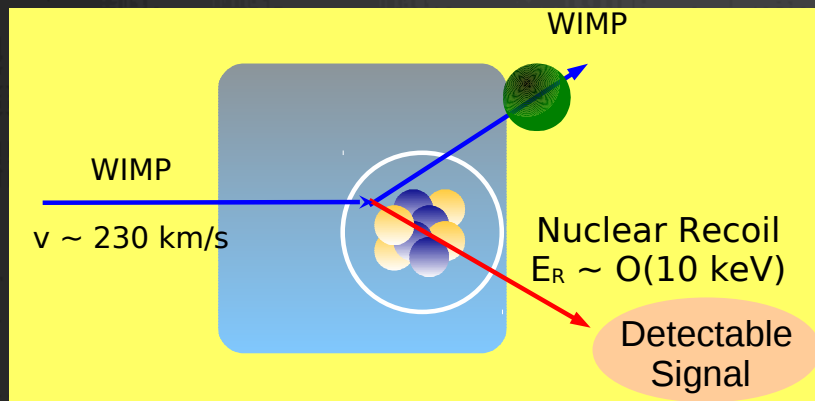
<b>18</b>	
2	2
<b>He</b>	
Helium	
4.002602	
10	2 8
<b>Ne</b>	
Neon	
20.1797	
18	2 8 8
<b>Ar</b>	
Argon	
39.948	
36	2 8 18 8
<b>Kr</b>	
Krypton	
83.798	
54	2 8 18 18 8
<b>Xe</b>	
Xenon	
131.293	
86	2 8 18 32 18 8
<b>Rn</b>	
Radon	
(222.0176)	

Noble gases	Neon	Argon	Xenon
Atomic Number	10	18	54
Atomic Mass	20.2	40.0	131.3
Boiling Point ( $T_b$ )	27.1 K	87.3 K	165.0 K
Liquid density at $T_b$ (g/cm <sup>3</sup> )	1.21	1.40	2.94
Fraction in atmosphere (ppm)	18.2	9340	0.09
Cost	\$\$	\$	\$\$\$\$
Light Yield (ph/keV)	25	40	42
Prompt Time constant	2.2ns	6ns	2.2ns
Late Time constant	16us	1.6us	21ns
PSD	yes	yes ( $3 \cdot 10^{-8}$ )	no
e <sup>-</sup> drift velocity at 1kV/cm	2cm/s	$2 \cdot 10^5$ cm/s	$2 \cdot 10^5$ cm/s
S2/S1 discrimination	no	$2 \cdot 10^{-2} - 10^{-3}$	$5 \cdot 10^{-3} - 10^{-4}$
Open Project lines	(1)	3	3
Nuclear recoil $L_{\text{eff}}$		0.25 (>20keV)	~0.1 (@8keV)
WIMP ROI (keV)		30-200	8-45
Wimp Mass of peak sensitivity		~100GeV	~50GeV

# Signal expected

- $\rho \approx 0.3 \text{ GeV/cm}^3$
- $\langle v \rangle \approx 230 \text{ km/s}$
- a few tens of events/ton/year  
@  $\sigma_\chi = 10^{-46}$

$$E_r = \frac{|\vec{q}|^2}{2m_N} = \frac{\mu^2 v^2}{m_N} (1 - \cos \theta) \sim \mathcal{O}(10 \text{ keV})$$





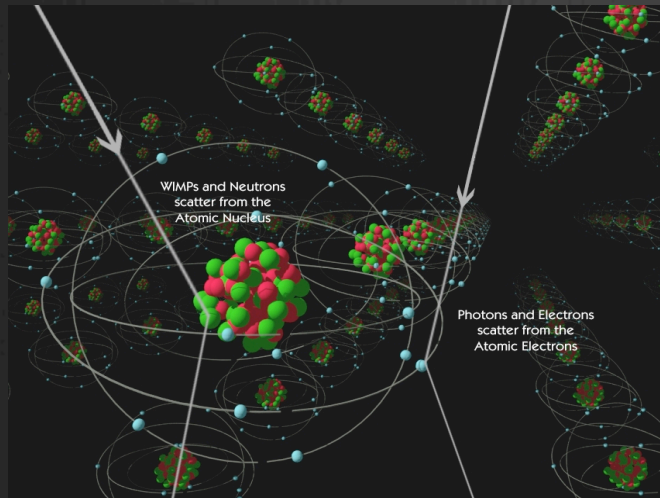
# Background

## ☼ Sources of background:

- ☼ Target material
- ☼ Detector material
- ☼ Site radioactivity (Radon, gammas, neutrons)
- ☼ Cosmogenics
- ☼ Solar neutrinos

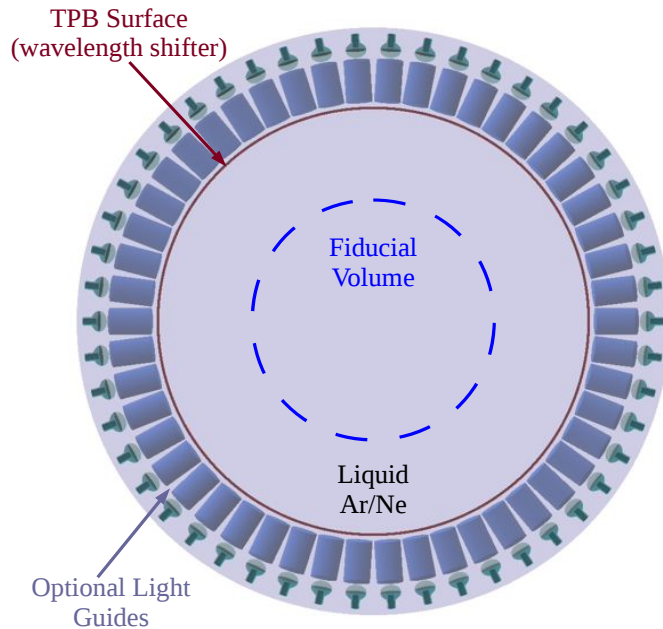
## ☼ Strategy:

- ☼ Target purification/depletion
- ☼ Selection of Materials (e.g. QPIDs for PMTs)
- ☼ ER/NR discrimination:
  - ☼ S2/S1 (better for Xe)
  - ☼ PSD (Ar only)  $\times 3 \times 10^{-8}$
  - ☼ single/multi sites (mostly TPC).
- ☼ Self shielding/fiducialization
- ☼ Site selection
- ☼ Active veto
- ☼ Passive Shielding

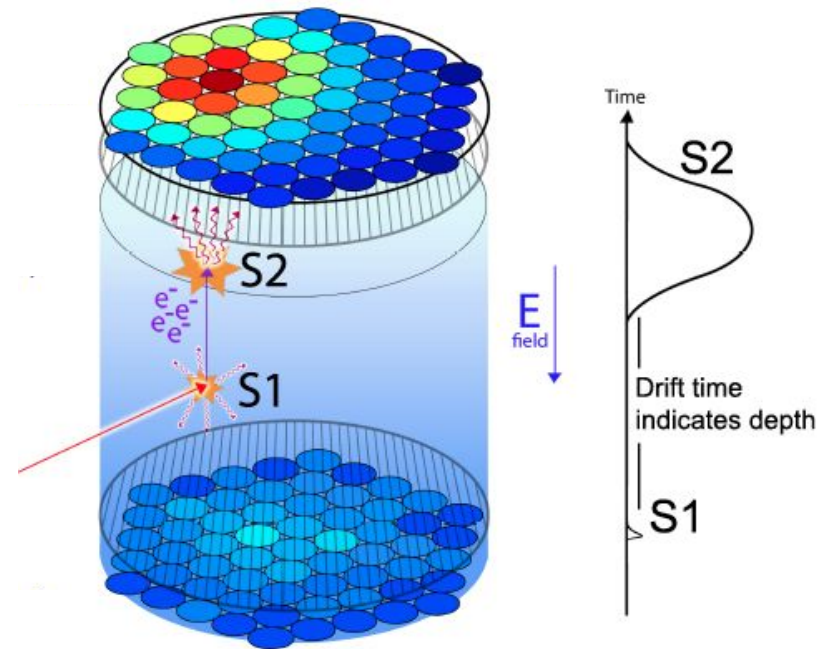


# Single or Dual phase?

**Single-Phase**  
LNe / LAr / LXe



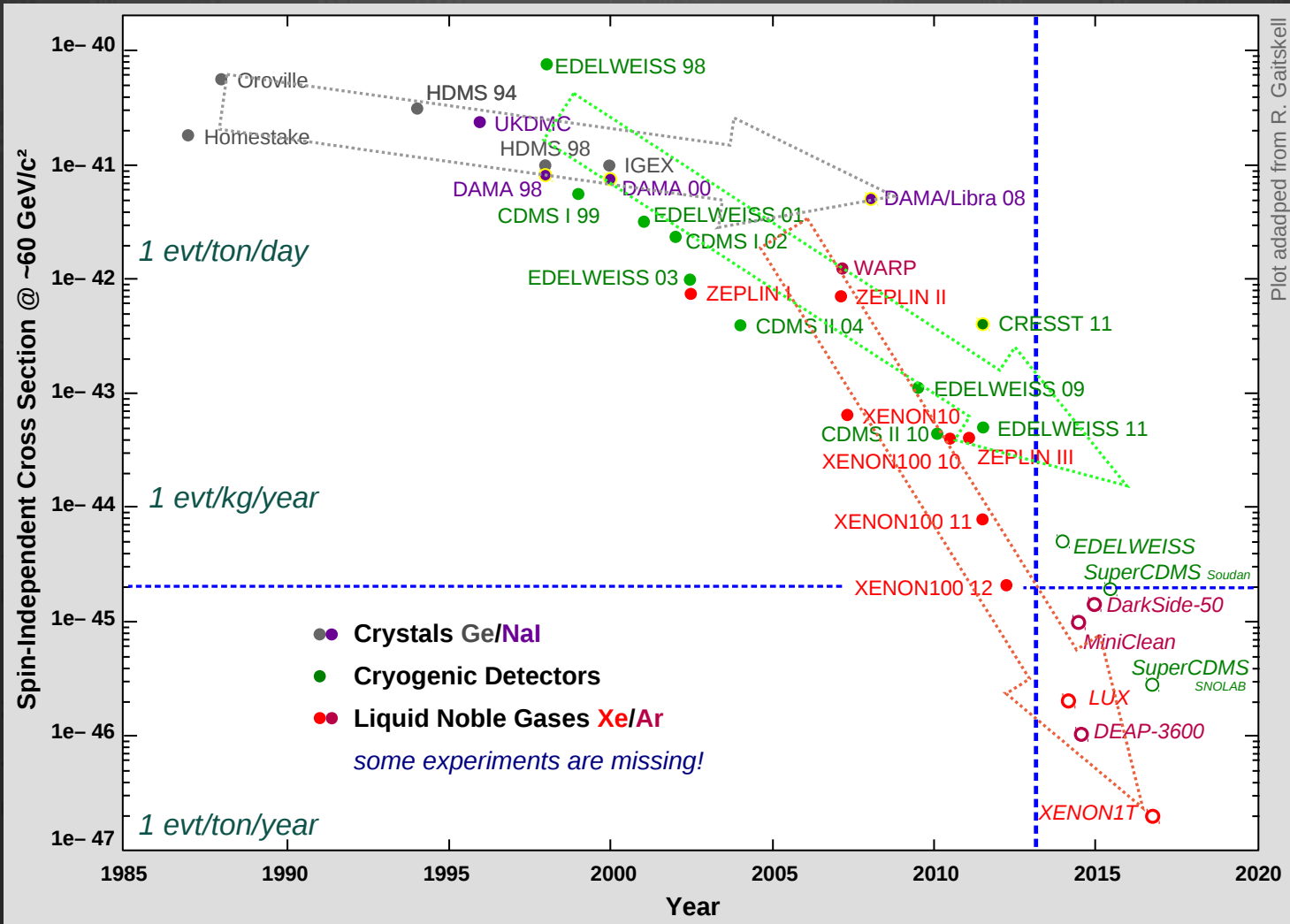
**Dual-Phase**  
LAr / LXe

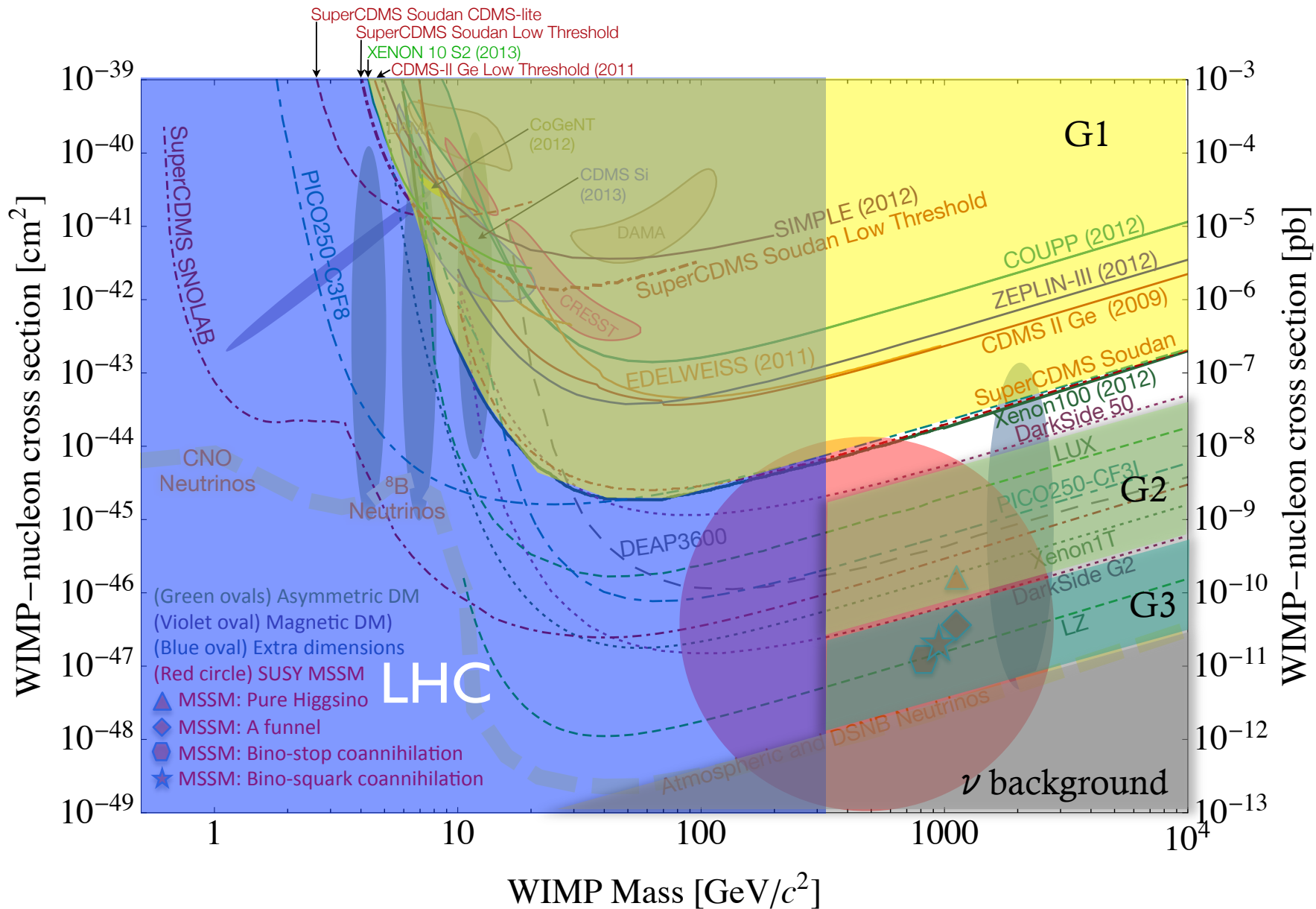


$\sigma \approx 10\text{cm}$   
No S2/S1 discrimination, but no pile-up  
Strong fiducialization needed  $\sim 10\%$   
high optical coverage  $\sim 70\text{-}80\%$   $\rightarrow$  lower threshold

$\sigma_{x,y} \approx 3\text{mm}$   
 $\sigma_z < 1\text{mm}$   
moderate fiducialization  $\sim 50\% - 70\%$   
several kV electric field

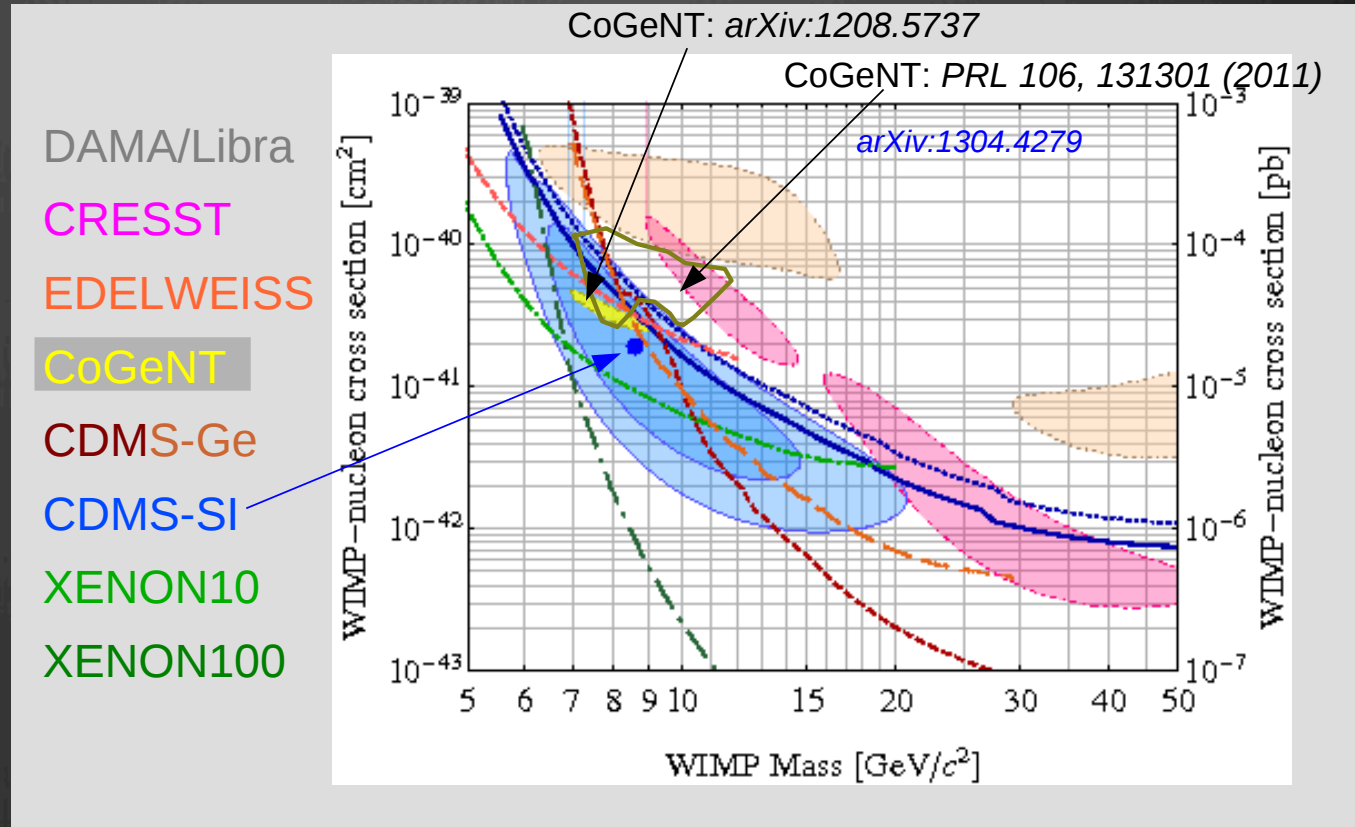
# Why noble gases?





# The low mass struggle

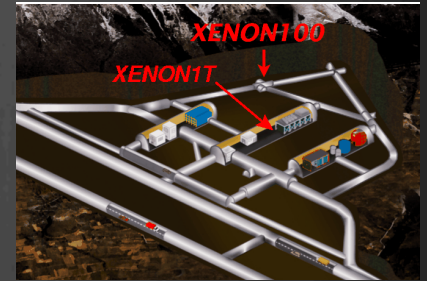
CDMS-Si favors a WIMP region of interest at 8.6 GeV with  $1.9 \times 10^{-41} \text{ cm}^2$  cross section. Consistent with CDMS Ge limits and with a WIMP interpretation of the COGENT experiment, not so much with DAMA and CRESST. In tension with limits from Xenon 10, Xenon 100 experiments



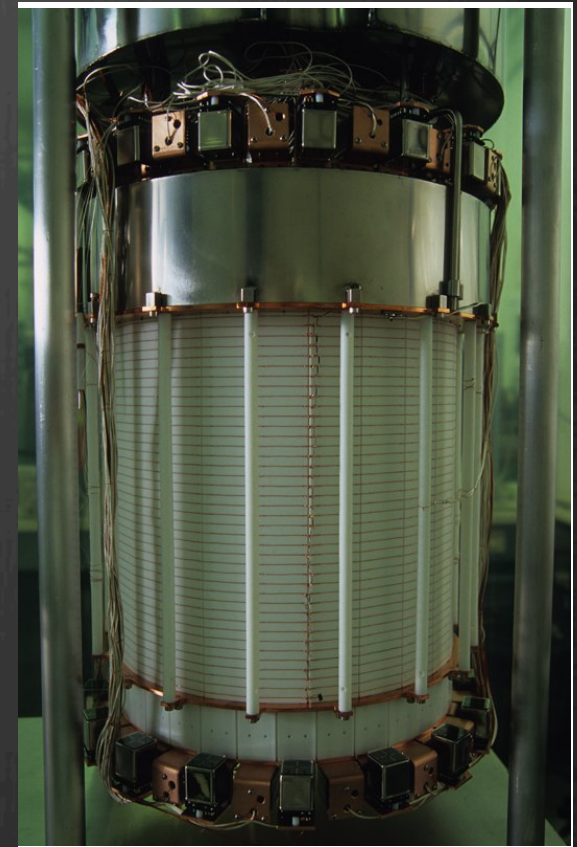
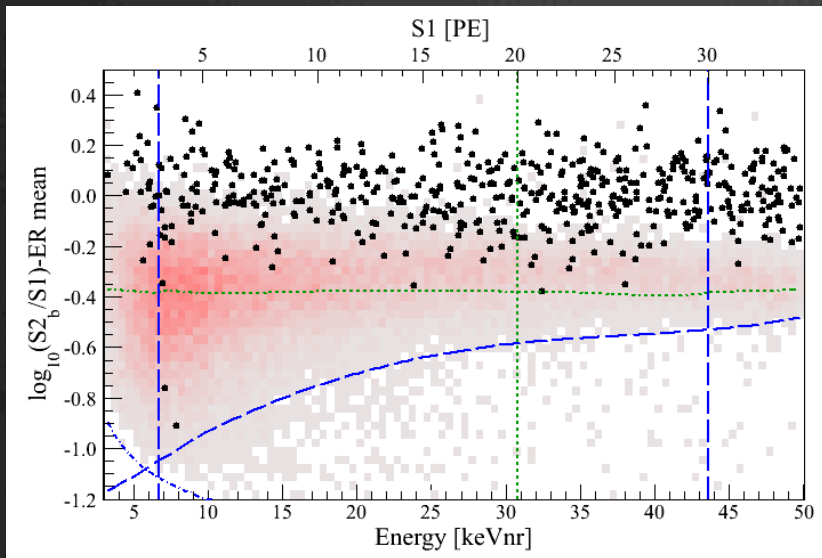
All region excluded by LHC:  
if this is a WIMP, it's not the same one...

Generation 1  
 $10^{-45} \text{ cm}^2$

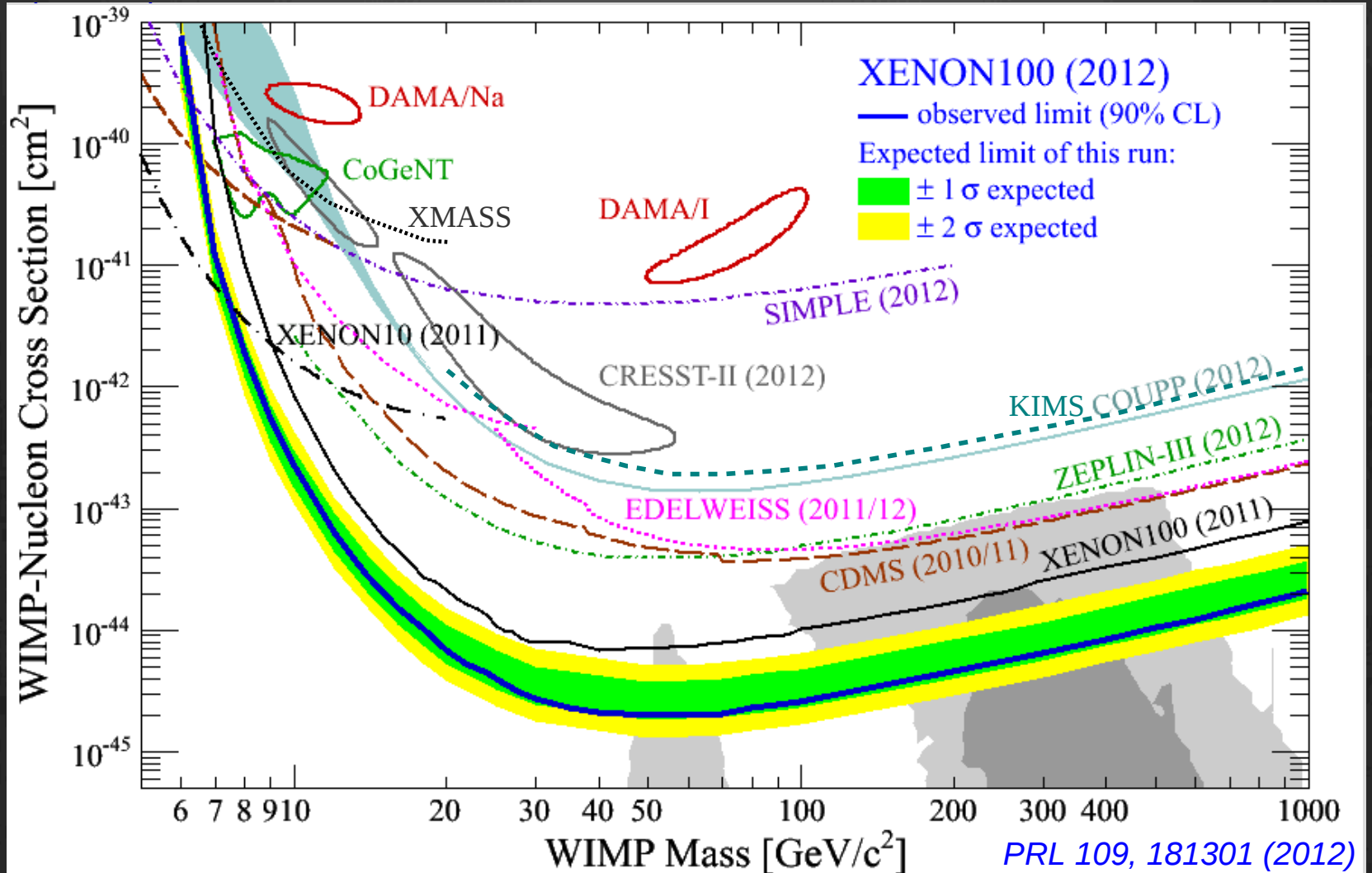
# Xenon 100



Located in LNGS (3800mwe)  
62kg LXe (34kg FM)  
dual phase TPC 30cm x 30cm  
241 1" PMTs  
in 2012 2 events observed  
compatible with bkg expectations  
Currently holding best limit for  $M_\chi > 10\text{GeV}$

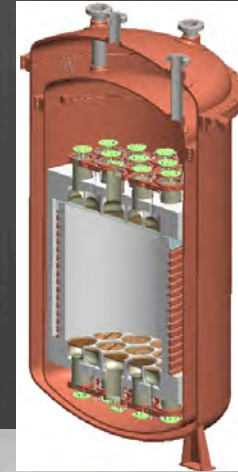


# Xenon 100 and the present scenario





# Dark Side 50



2-phase argon TPC  
Argon depleted from  $^{39}\text{Ar}$   
Three-fold discrimination  
(S1 pulse shape, S2/S1, sub-mm reconstruction)  
50kg active target, 33kg fiducial  
38 3" PMTs  
Goal:  $1.5 \cdot 10^{-45} \text{ cm}^2$



# Active Neutron Veto

Installed in LNGS Hall C, CTF of Borexino

30 tons liquid scintillator neutron veto

110 8' PMTs

Borated PC+PPO mixture

~60keV n capture

@0.6pne/keV

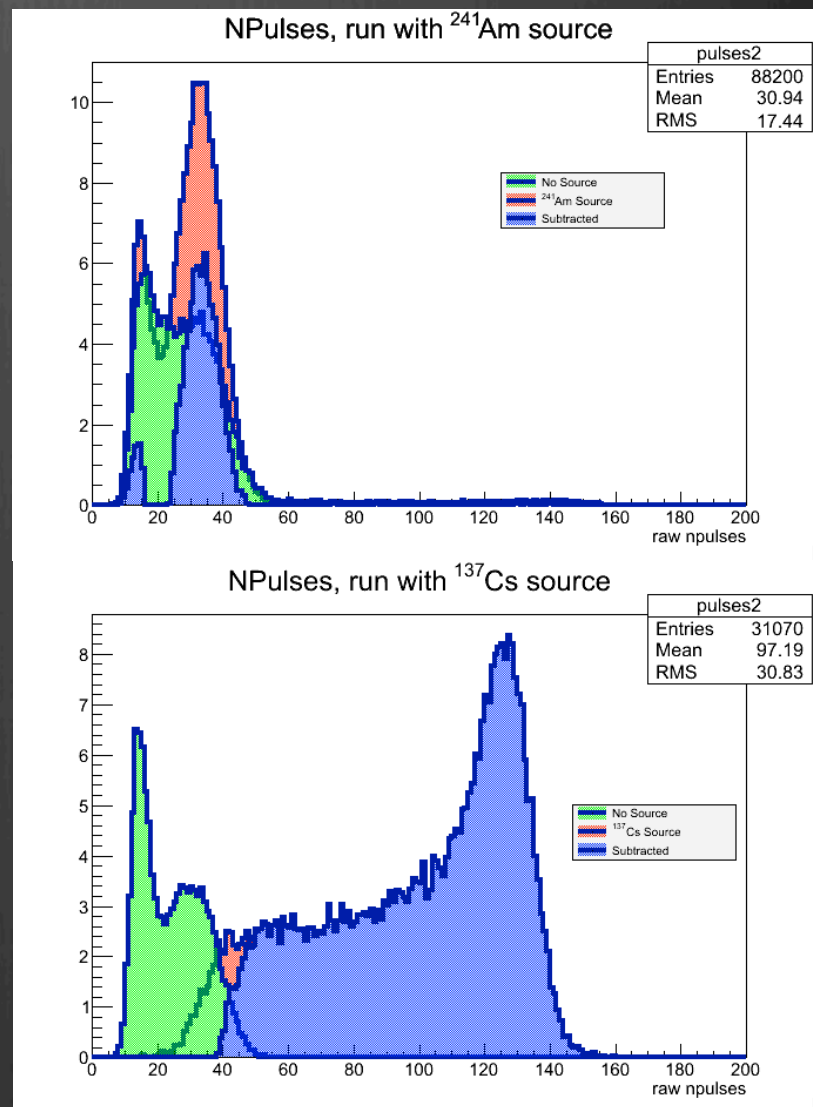
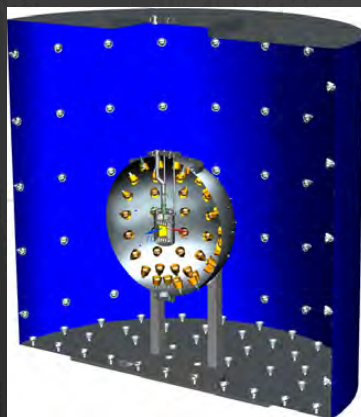
capture time reduced 250us  $\rightarrow$  2.3us

99.5% efficiency on radiogenic neutrons

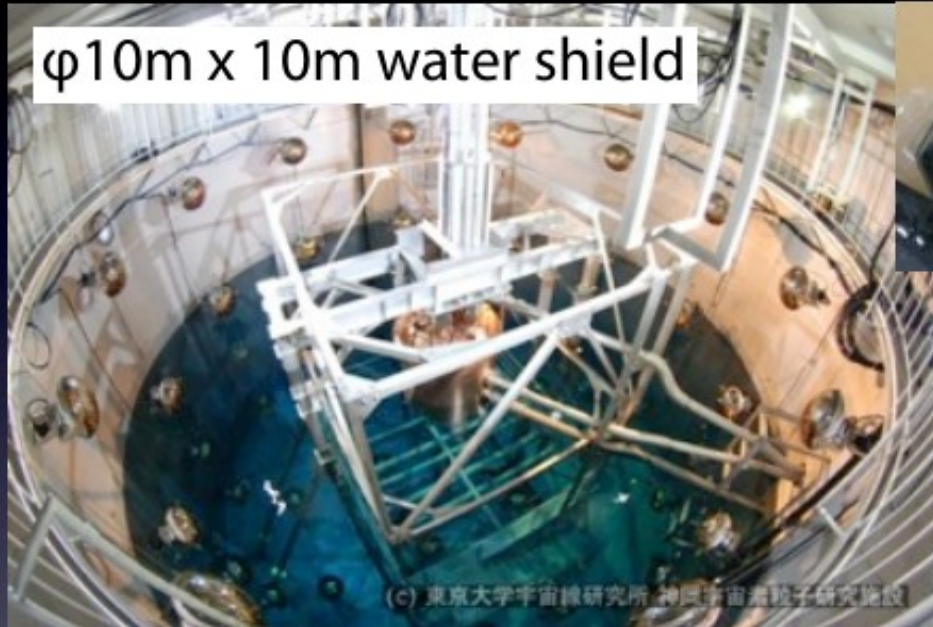
1,000 tons water Cherenkov muon veto

80 8' PMTs

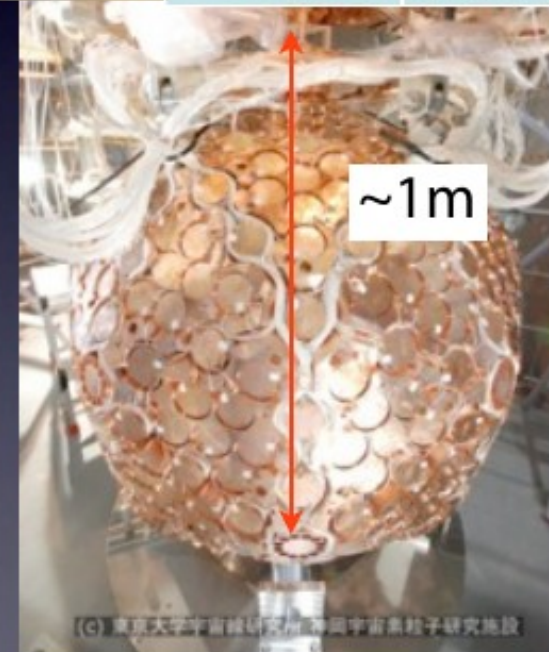
99.9% efficiency



# XMASS800kg in Kamioka



RI in PMT	Activity per 1PMT(mBq/
238U-chain	0.70+/-0.28
232Th-chain	1.51+/-0.31
40K	9.10+/-2.15
60Co	2.92+/-0.16



- $\phi 10\text{m} \times 10\text{m}$  ultra pure water shield with 20 inch x 70 PMTs for muon veto
- 642 ultra low background 2 inch PMTs
- 835 kg of LXe for sensitive volume.

Masaki Yamashita

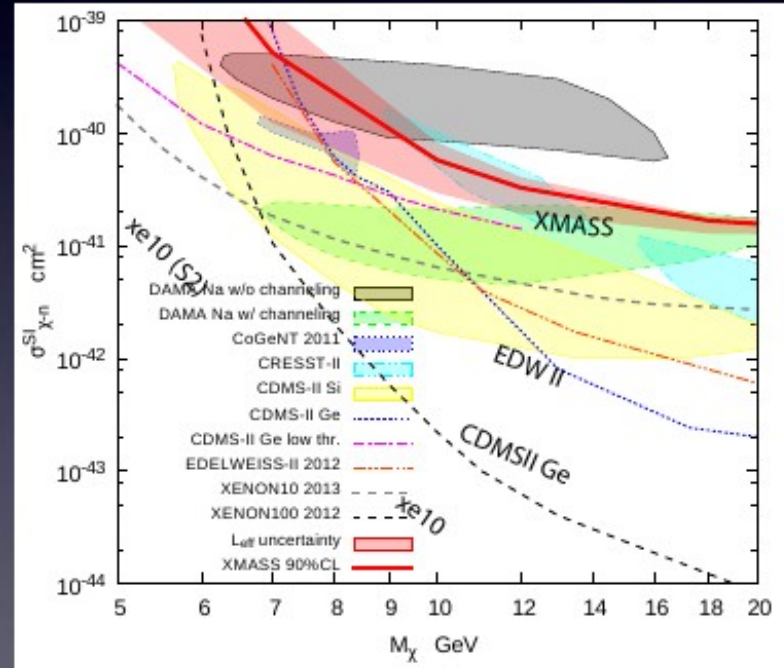
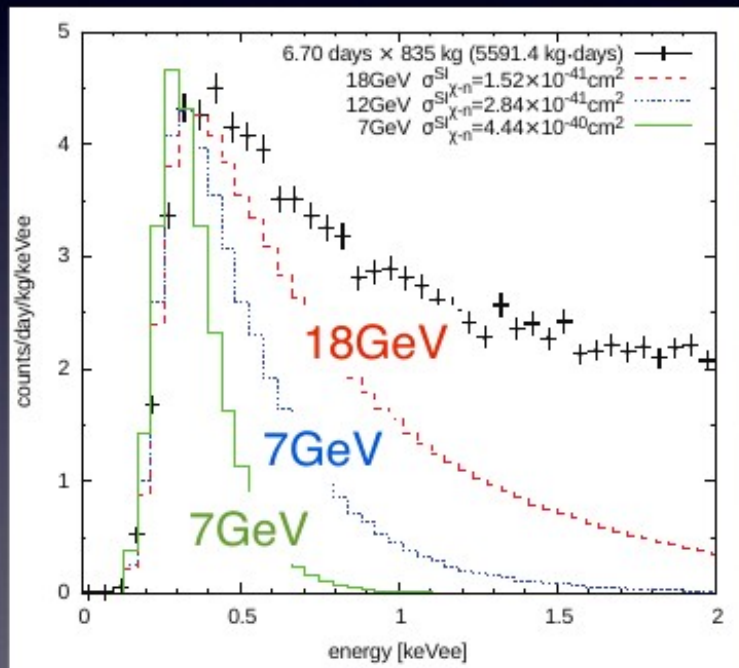
Plans to scale to G2 (5t->1.5tFM) and G3(20t->12tFM)

# Recent Result of XMASS

Masaki Yamashita

## Light mass WIMP

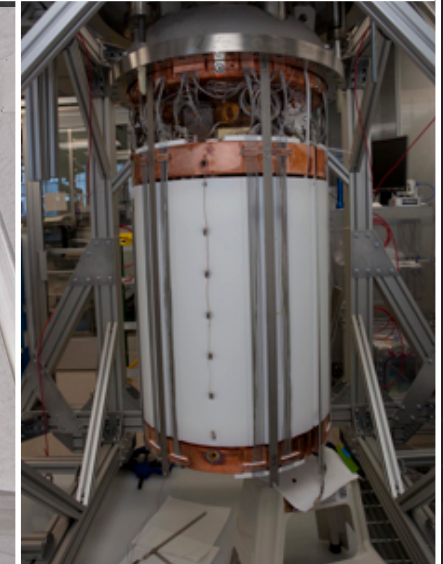
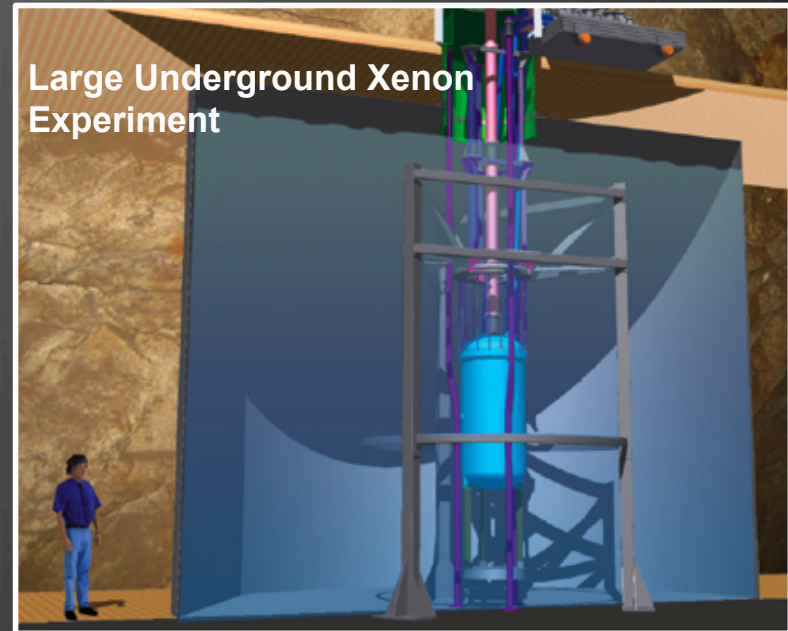
- Full volume analysis with 835 kg LXe. (without fiducial volume cut.)
- High Light Yield 14.7 PE/keV
- Eth 0.3 keVee (scaled by 122keV)
- Scintillation Efficiency ( $L_{eff}$ ) from XENON (E. Aprile et al., Phys. Rev. Lett. 107 (2011) 131302)



For higher WIMP mass, unexpected surface background.  
In 2013 PMTs will be refurbished to handle this problem

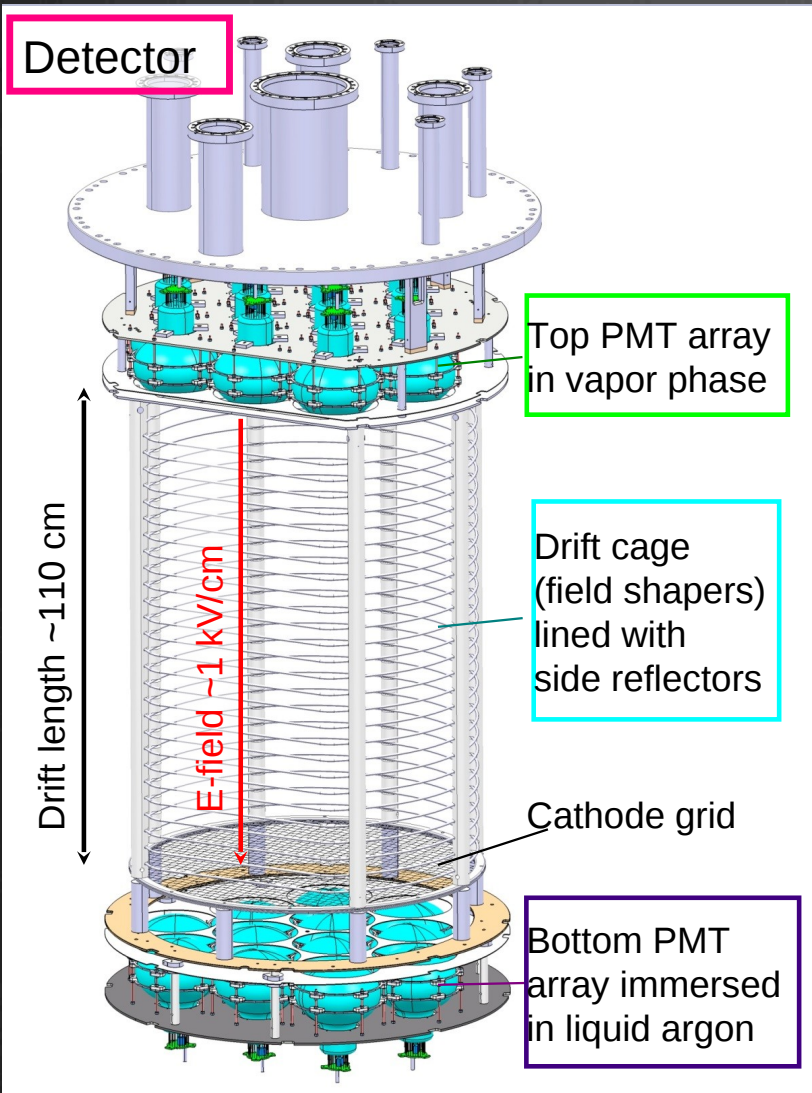
# LUX @ Sanford Lab 2013

- LXe TPC - 300 kg active / 100 kg fid.
  - ◆ Installed in water shield at Sanford Lab Davis Campus 4850' level Aug 2012
  - ◆ Xenon condensed Feb 2013
- Detector
  - ◆ Circulating > 20 SLPM with 2-phase heat exchanger @ >90% eff.
  - ◆ Good purity after < 2 months (Electron drift attenuation >100 cm)
  - ◆ Excellent light yield - 8 phe/keVee, zero field, 122 keVee
  - ◆  $^{85}\text{Kr}$  @ 4ppt (less than PMT bkg.)
- WIMP Searches
  - ◆ Plan short (~ 60 day) WIMP search run - result by end 2013 - non-blind analysis
  - ◆ Full year-long WIMP search run to begin in 2014/5 - blind analysis



122 Hamamatsu  
R8778 Low bkg. PMTs

# ArDM



- Fully PMT-based readout:
  - 2 new arrays of 12 x 8" Hamamatsu PMTs (R5912-02MOD-LRI), TPB coating
  - primary scintillation light (in liquid)
  - charge via proportional scintillation (in vapor)
    - discrimination with PSD, charge/light ratio
- Active LAr target: ~0.8 ton
- Tetratex® side reflectors coated with TPB
- Drift field : ~1 kV/cm
- ~100 kV at cathode, supplied using VHV feedthrough



# ArDM



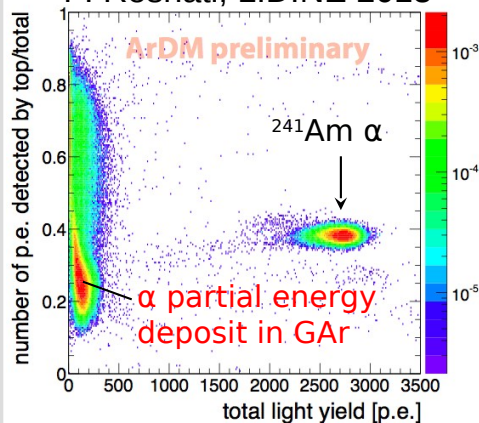
ETHZ

Installed at  
Laboratorio  
Subterráneo  
de Canfranc (LSC)

The new ArDM detector,  
fully assembled in the LSC  
clean room, being installed  
into the detector vessel

## GAR data@LSC

F. Resnati, LIDINE 2013

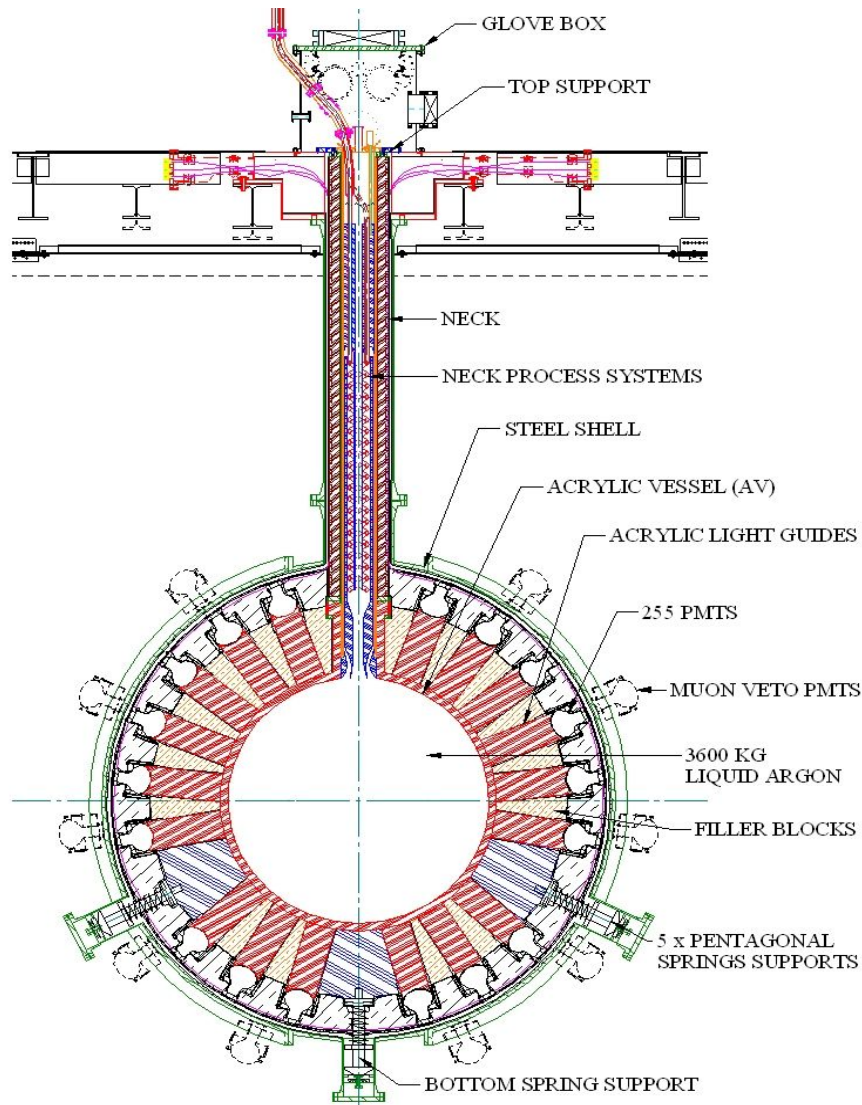


- Installation of ArDM finished March 2013
- **currently: commissioning with GAR**  
improved uniformity. [Detector is taking data.](#)  
LY=2 pe/keVee @ E=0 keV, measured with  $\alpha$   
material screening with HPGE @ LSM  
in-situ n-measurement with liquid scintillator
- **Next: LAr commissioning**  
LAr tests: HV, purification, cryogenics...  
[expect physics run by 2014](#)

Generation 2  
 $10^{-47} \text{ cm}^2$



# DEAP 3600



## DEAP-3600 Detector

3600 kg argon target  
(1000 kg fiducial)  
in sealed ultraclean  
Acrylic Vessel

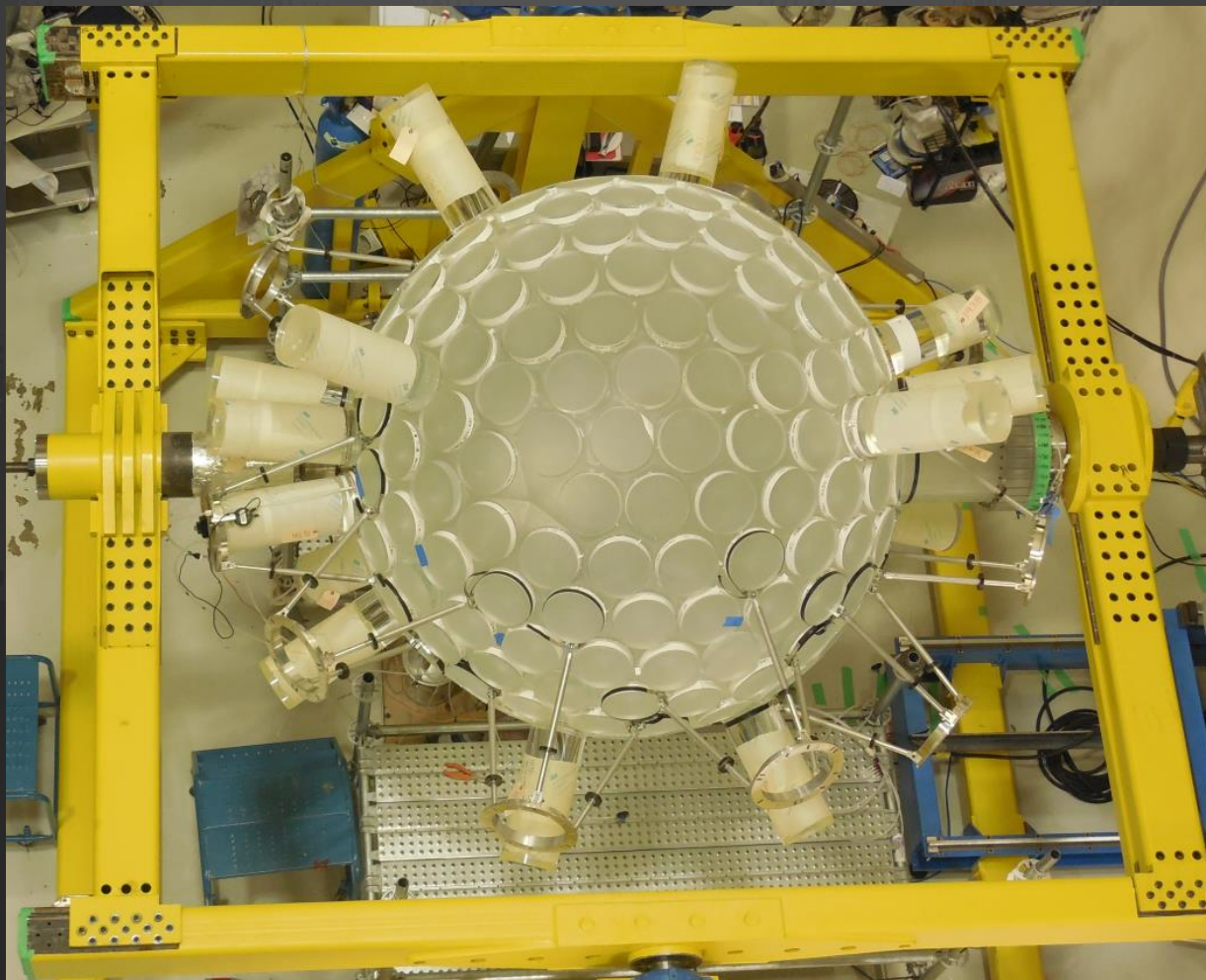
Vessel is “resurfaced”  
in-situ to remove  
deposited Rn daughters  
after construction

255 Hamamatsu  
R5912 HQE PMTs 8-inch  
(32% QE, 75% coverage)

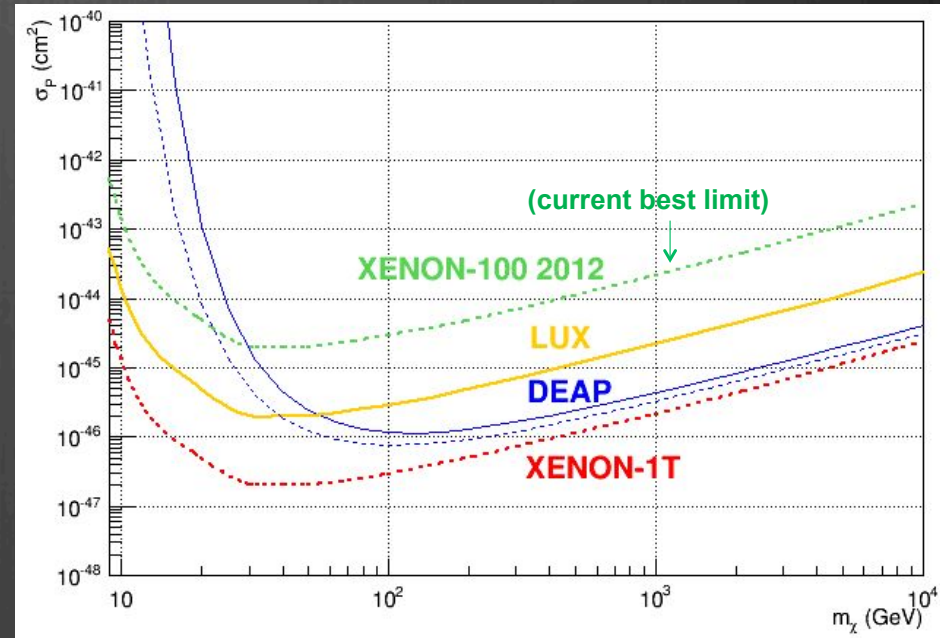
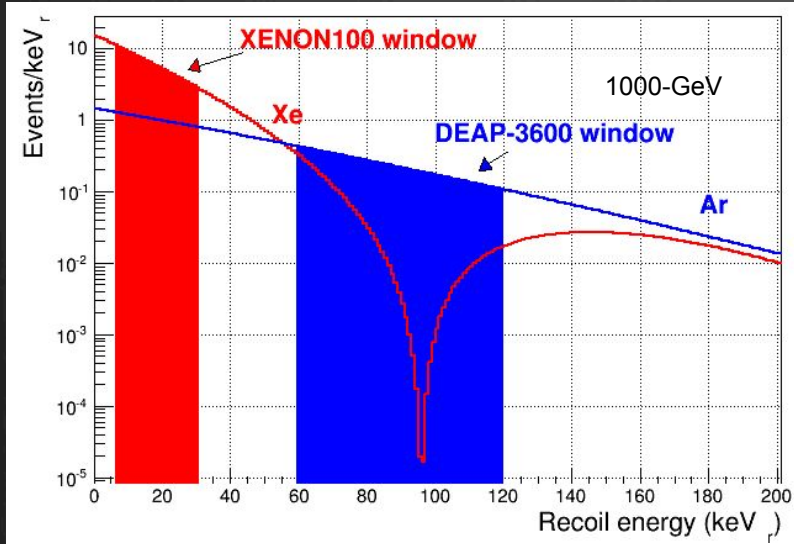
50 cm light guides +  
PE shielding provide  
neutron moderation

Detector in 8 m water  
shield at SNOLAB

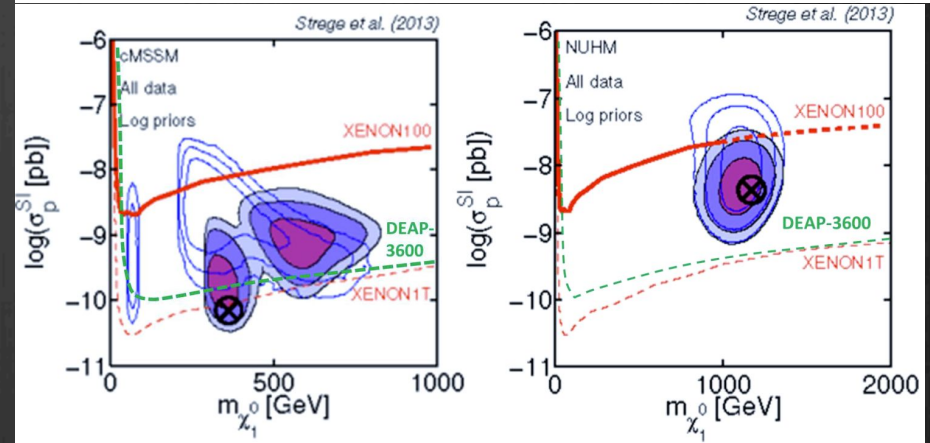
# DEAP 3600



# DEAP 3600 physics potential



Post LHC remaining minimal SUSY models can be investigated at  $m_\chi > 350$  GeV



# DEAP 3600: scale-up

## Tentative Project Schedule

2013,2014:

Conceptual design/safety analysis, develop budget  
Identify space requirements, submit space request  
and development requests  
(Start DEAP-3600 Data collection, focus of effort)

2014,2015:

More detailed engineering for budgeting  
Design/plans for depleted argon storage and delivery

2015-2017:

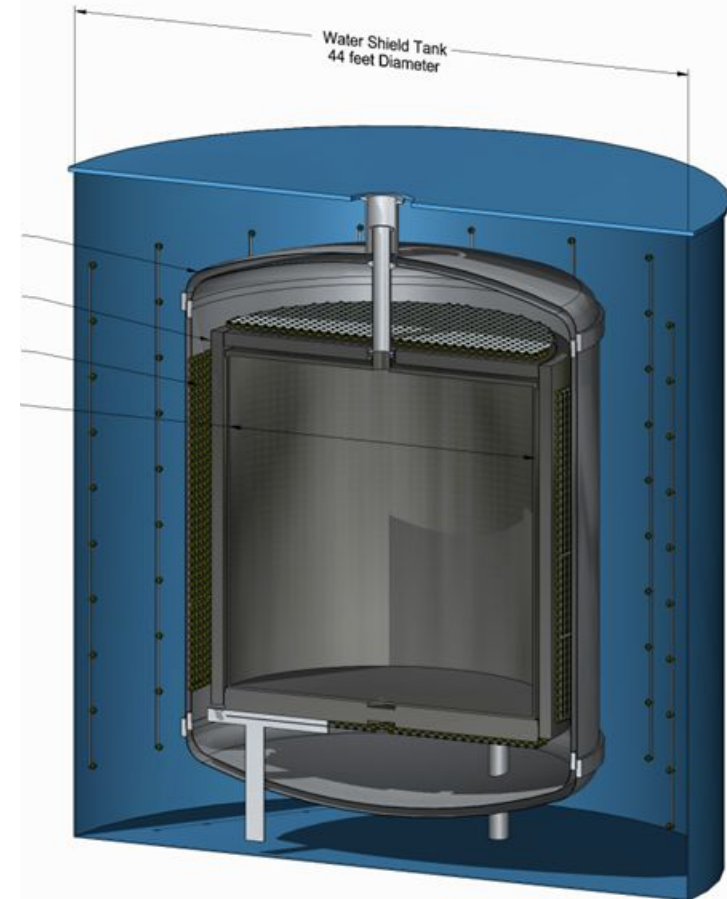
Detailed engineering for contracts/fabrication  
Implementation of DAr storage and argon collection start

2017-2020:

Construction and Installation  
Continued DAr collection/storage  
(End DEAP-3600 Data collection)

2020-2025:

Operation



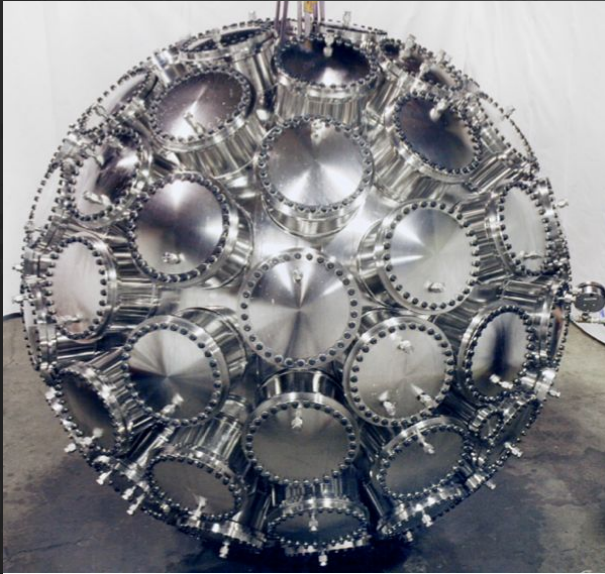
# Depleted Argon

- ⊗ Ordinary atmospheric argon contains cosmogenic  $^{39}\text{Ar}$ 
  - ⊗  $\beta$ -emitter ( $Q=565\text{keV}$ ,  $\tau = 388\text{yr}$ )
  - ⊗  $^{39}\text{Ar}/\text{Ar} = 8 \cdot 10^{-16} \rightarrow \sim 1\text{Bq/kg}$ .
- ⊗ TPC drift times:  $\sim 500 \mu\text{s/m}$ .
  - ⊗ Above 1t pile-up becomes an issue.
- ⊗ Underground Argon facility established in 2011 in Colorado within DarkSide.
  - ⊗ Will serve DarkSide50 and DEAP 3600.
- ⊗ Production rate  $\sim 1\text{kg/d}$ 
  - ⊗ need to improve to  $>100\text{kg/d}$  for multi-ton detectors

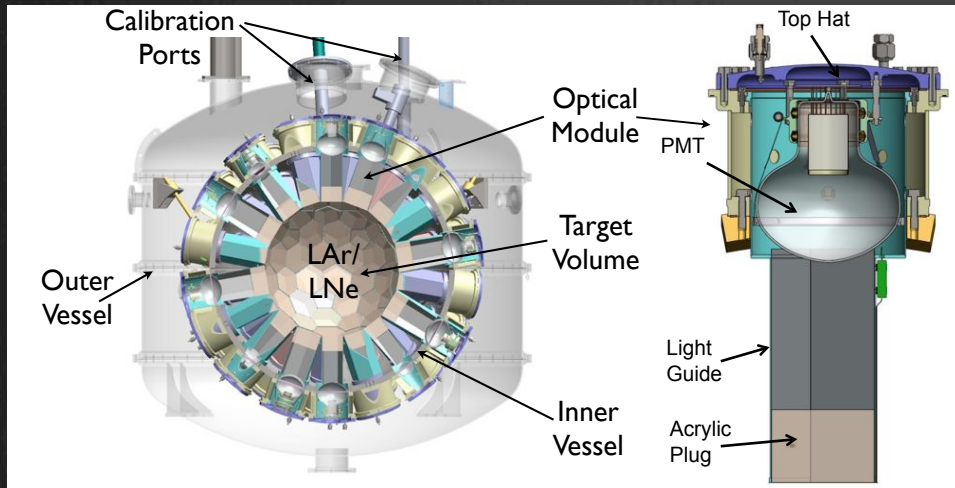


depletion factor:  $>100$

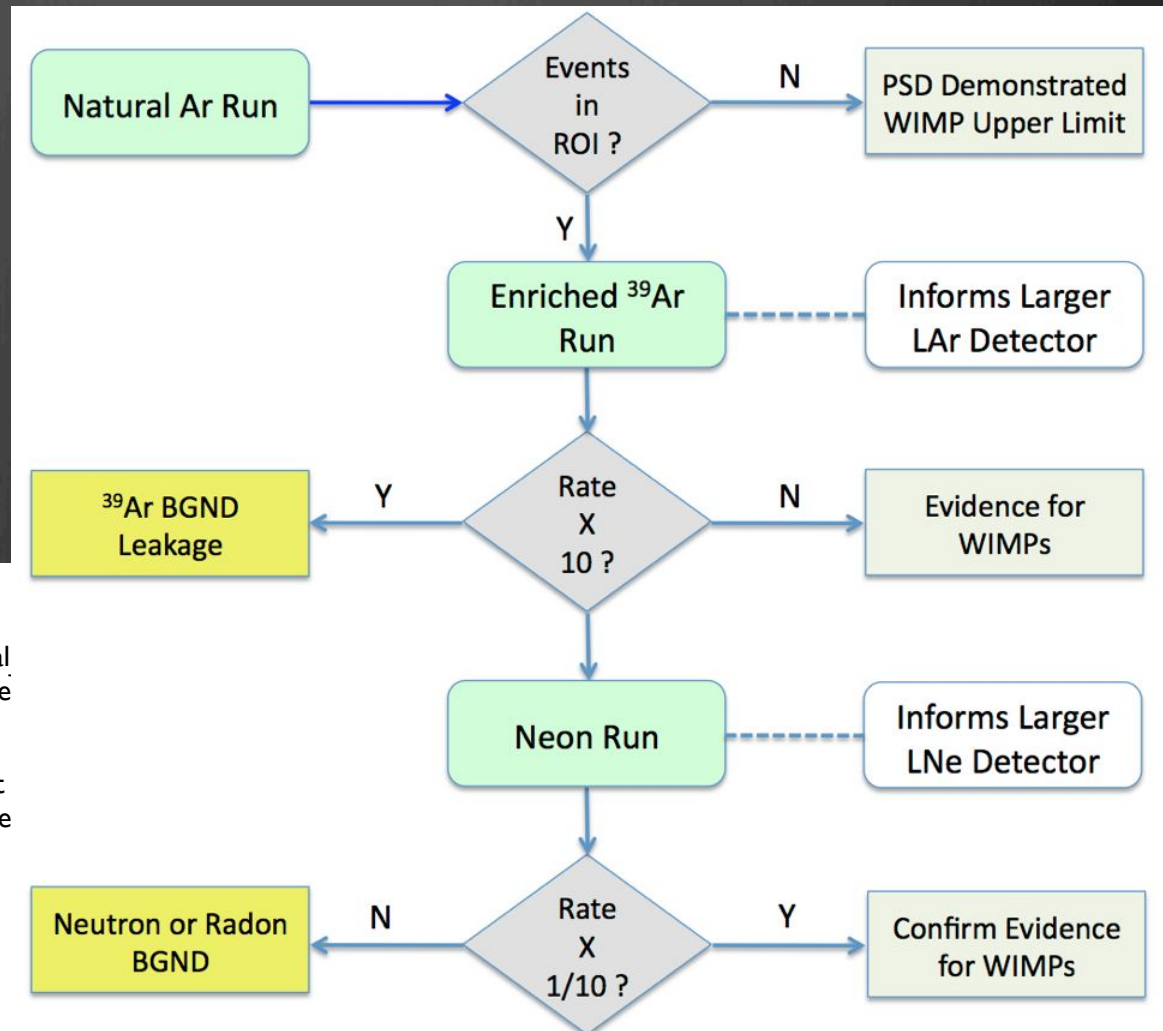
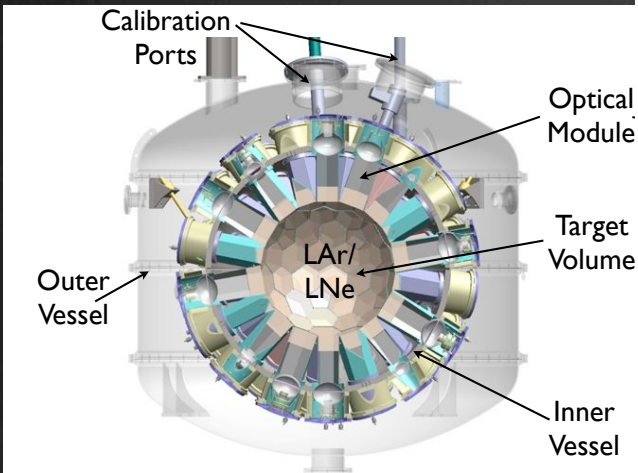
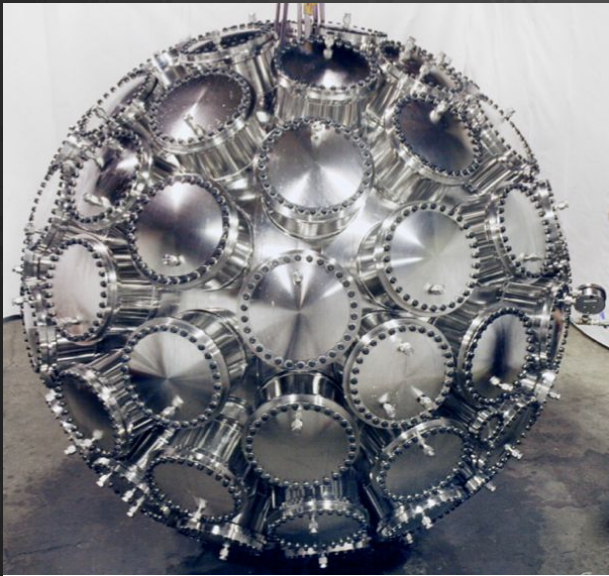
# MiniCLEAN



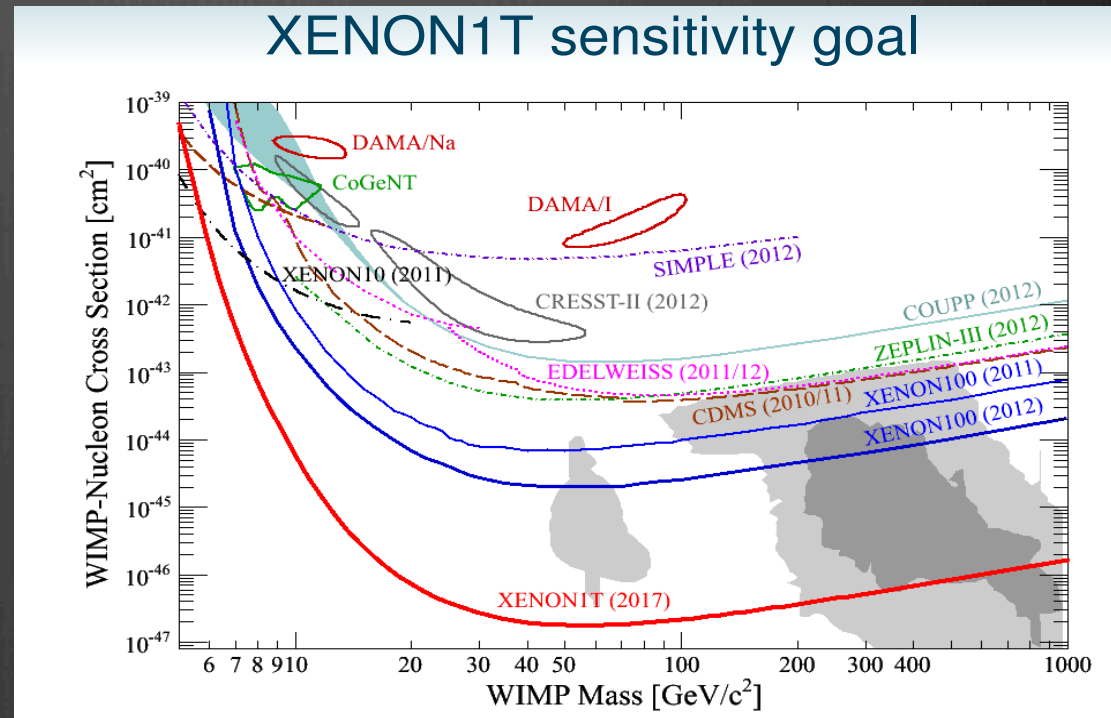
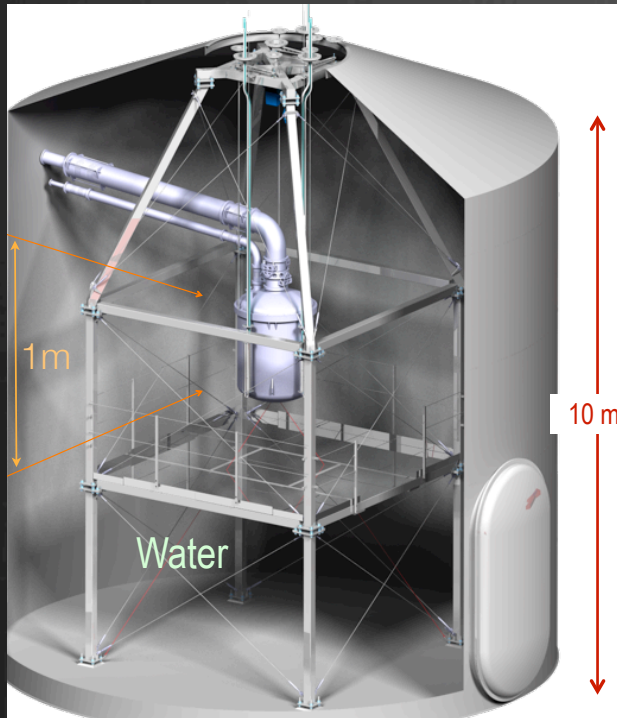
DEAP twin experiment:  
investigation/confirmation  
500kg/150kgFM  
Dual target: LAr and LNe  
Plans to scale up to 45t



# MiniCLEAN



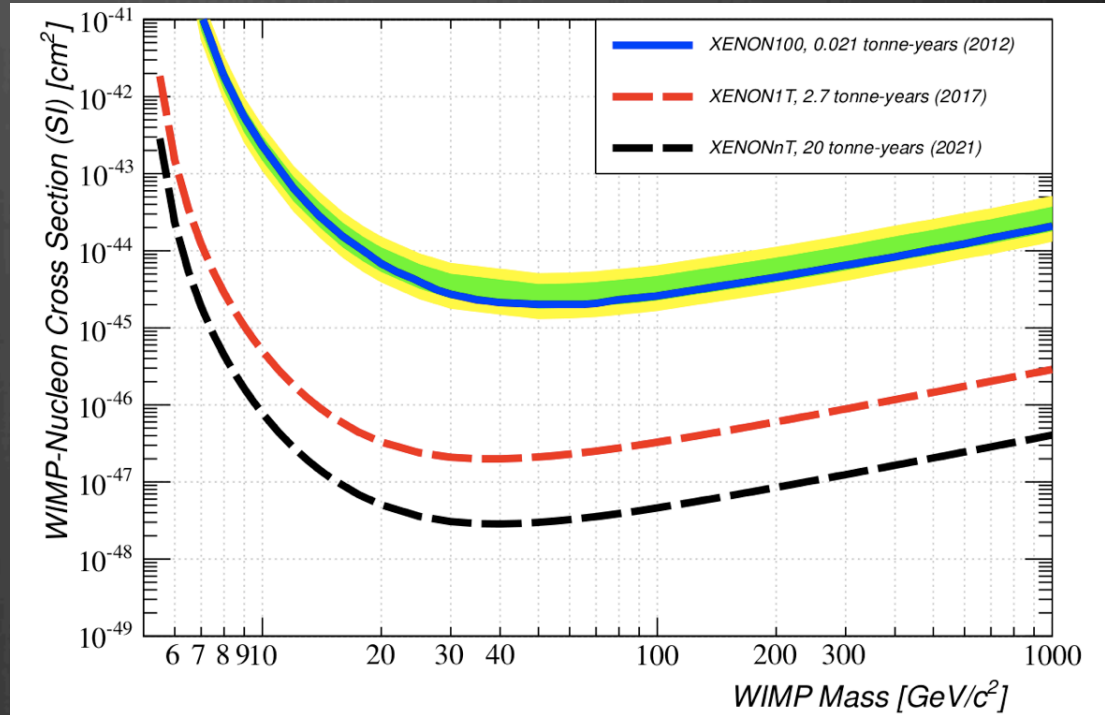
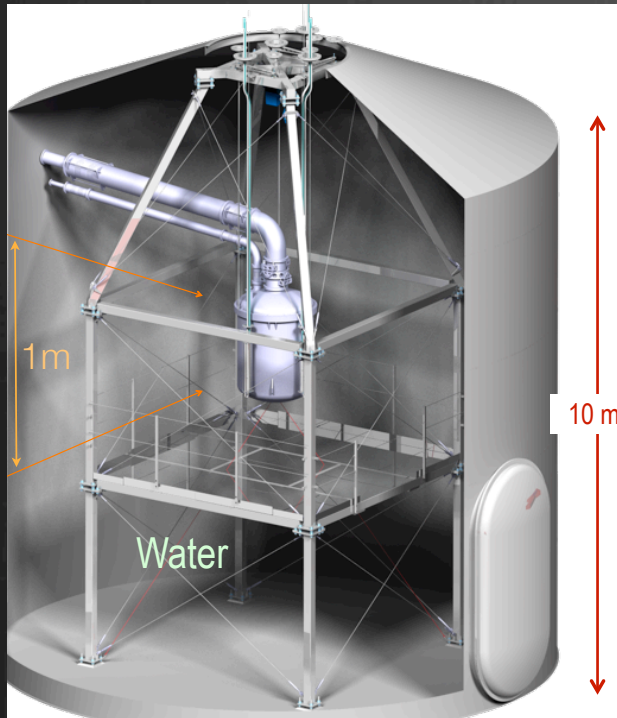
# Xenon 1t



1m x 1m dual-phase Xe TPC with 100kV  
Construction started ~2 months ago  
3.5t active target: 2t fiducial  
248 3" PMTs



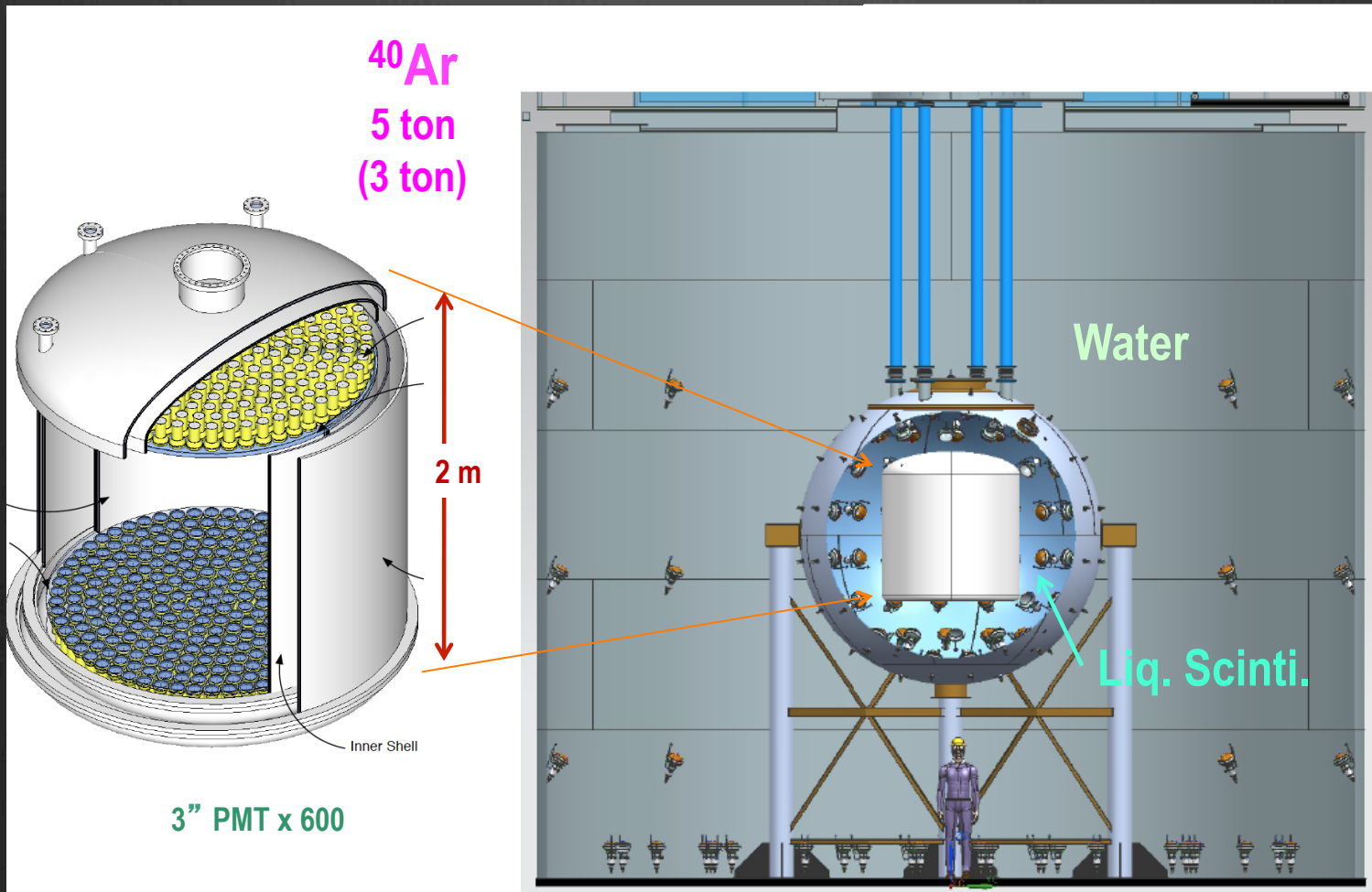
# Xenon 1t



1mx1m dual-phase Xe TPC with 100kV  
Construction started ~2months ago  
3.5t active target: 2t fiducial  
248 3" PMTs

# Dark Side 5t

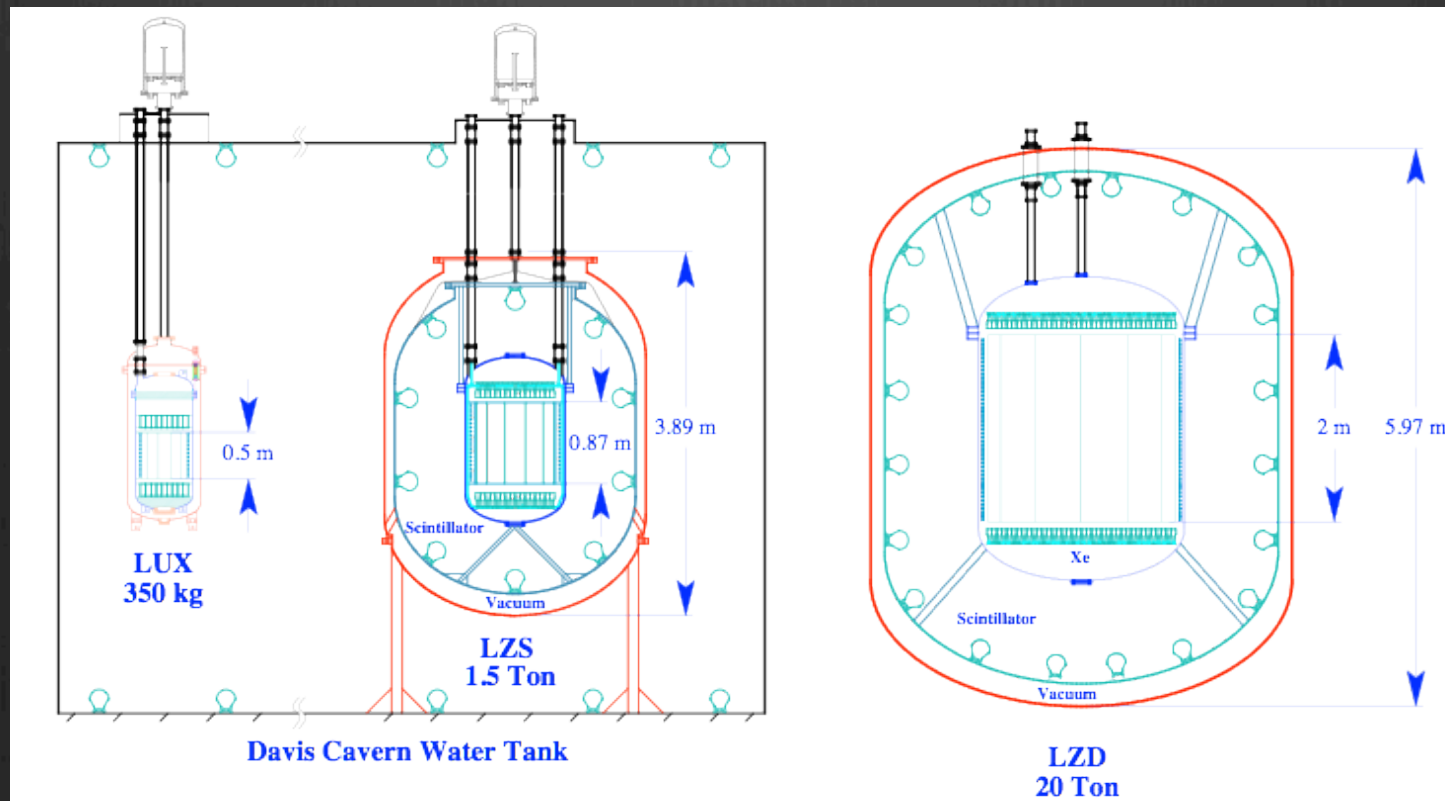
submitted for DOE approval in November 2013



Generation 3  
 $10^{-48} \text{ cm}^2$   
(and beyond?)

# LZ

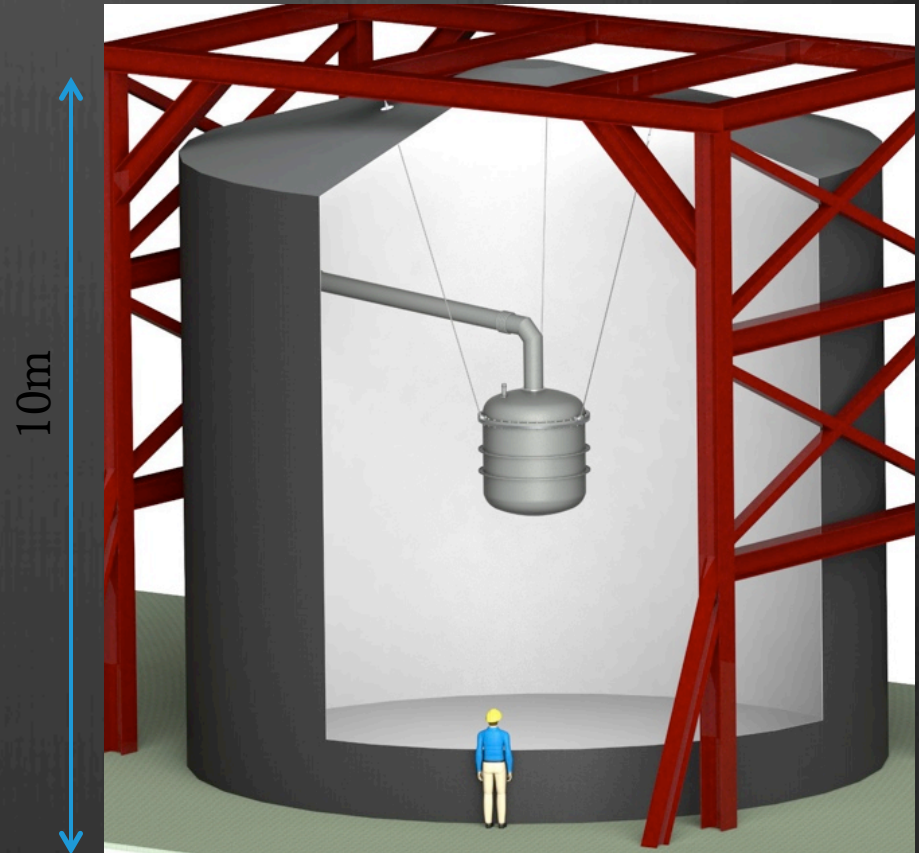
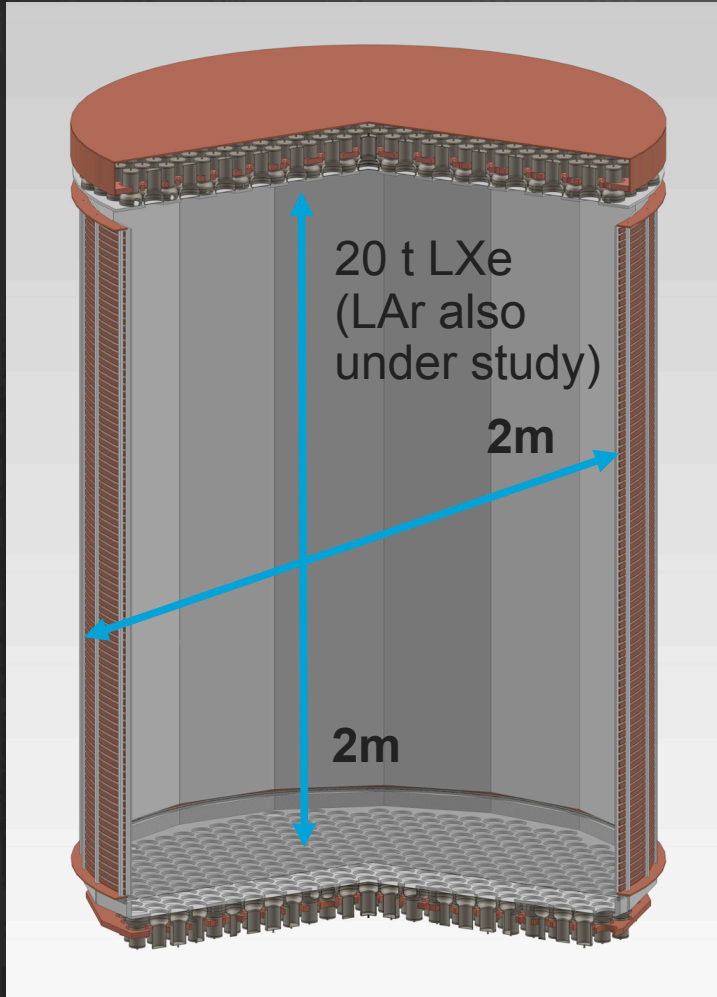
2 stages Scale-up of LUX, joint effort of Lux and Zepelin collaborations



SANFORD underground laboratory

# Darwin

20t LXe (~12t fiducial); ~ 1050 PMTs,  
physics run to start in 2020



# Darwin: site radioactivity

Energy interval [keV]	LNGS: Hall A	
	gamma flux [m <sup>-2</sup> d <sup>-1</sup> ]	gamma flux [cm <sup>-2</sup> s <sup>-1</sup> ]
0-500	4.4 · 10 <sup>8</sup>	0.51
500-1000	1.1 · 10 <sup>8</sup>	0.13
1000-2000	7.0 · 10 <sup>7</sup>	0.081
2000-3000	1.3 · 10 <sup>7</sup>	0.015
Entire spectrum	6.3 · 10 <sup>8</sup>	0.74

C. Bucci et al., Eur. Phys. J. A 41, 155 (2009)

Lab	Neutron Flux ( $\times 10^{-6}$ cm <sup>-2</sup> s <sup>-1</sup> )	
	all energies	E>1MeV
LNGS [61] (measurements)	3.78±0.25	0.60±0.07 or 0.70±0.14
LNGS [61] (simulations)	3.75±0.67	0.58±0.13
LNGS - Hall A [62] (measurements)	3.8±1.2	1.2±0.4
LSM	≈2 [64]	1.06±0.1(stat)±0.59(syst) [63]

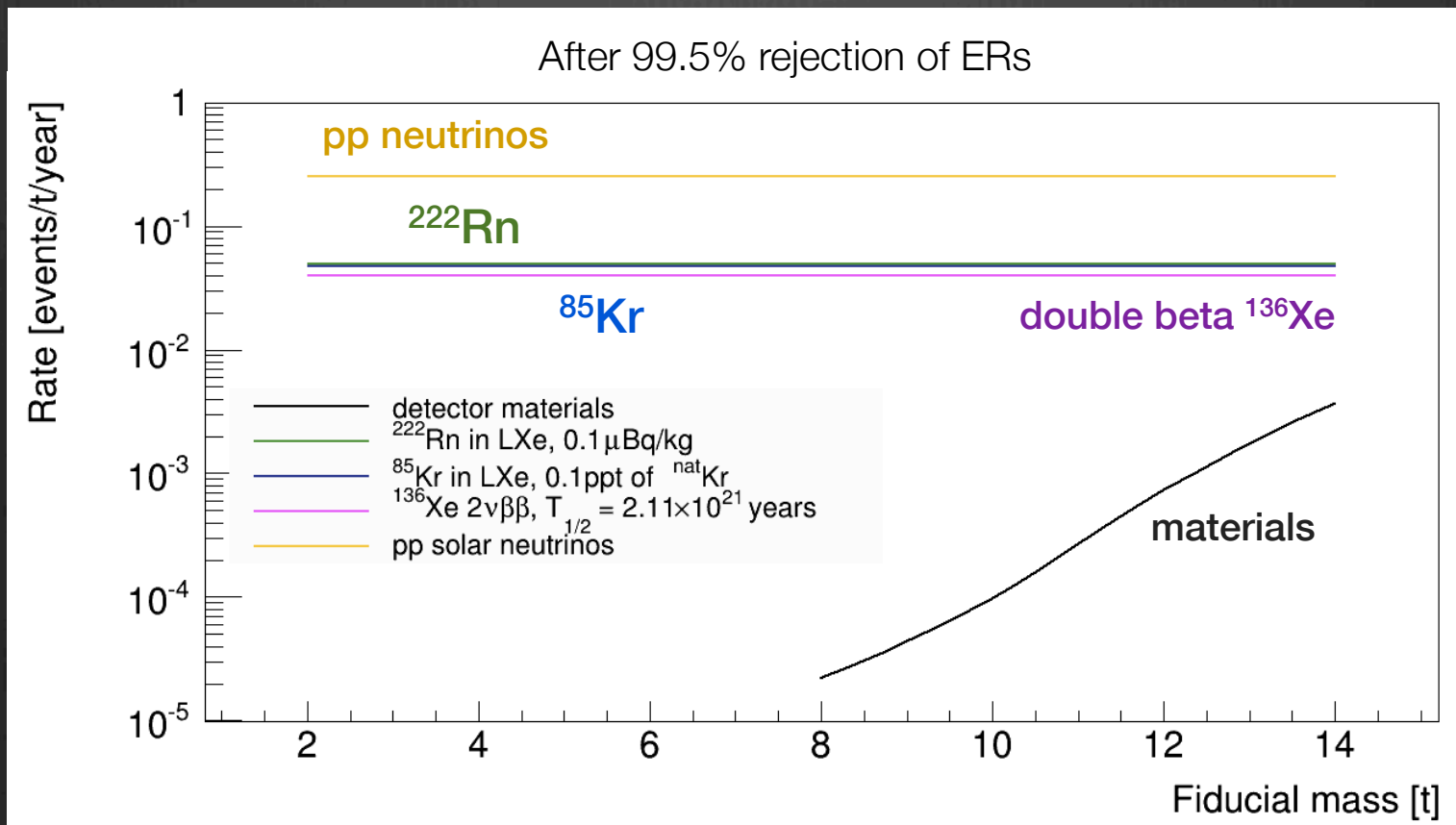
H. Wulandari et al., arXiv:hep-ex/0312050

Lab	Depth (m.w.e)	Equivalent vertical depth [65] (m.w.e.)	Muon flux (m <sup>-2</sup> d <sup>-1</sup> )	Mean energy (GeV)	Muon-induced neutron flux (m <sup>-2</sup> d <sup>-1</sup> )
LNGS	≈ 3750	≈ 3100	22.3±2.6	≈ 270	2.35
LSM	≈ 4800	≈ 4200	4.17±0.43	≈ 300	0.54

D.-M. Mei, A. Hime, Phys. Rev. D 73 (2006)

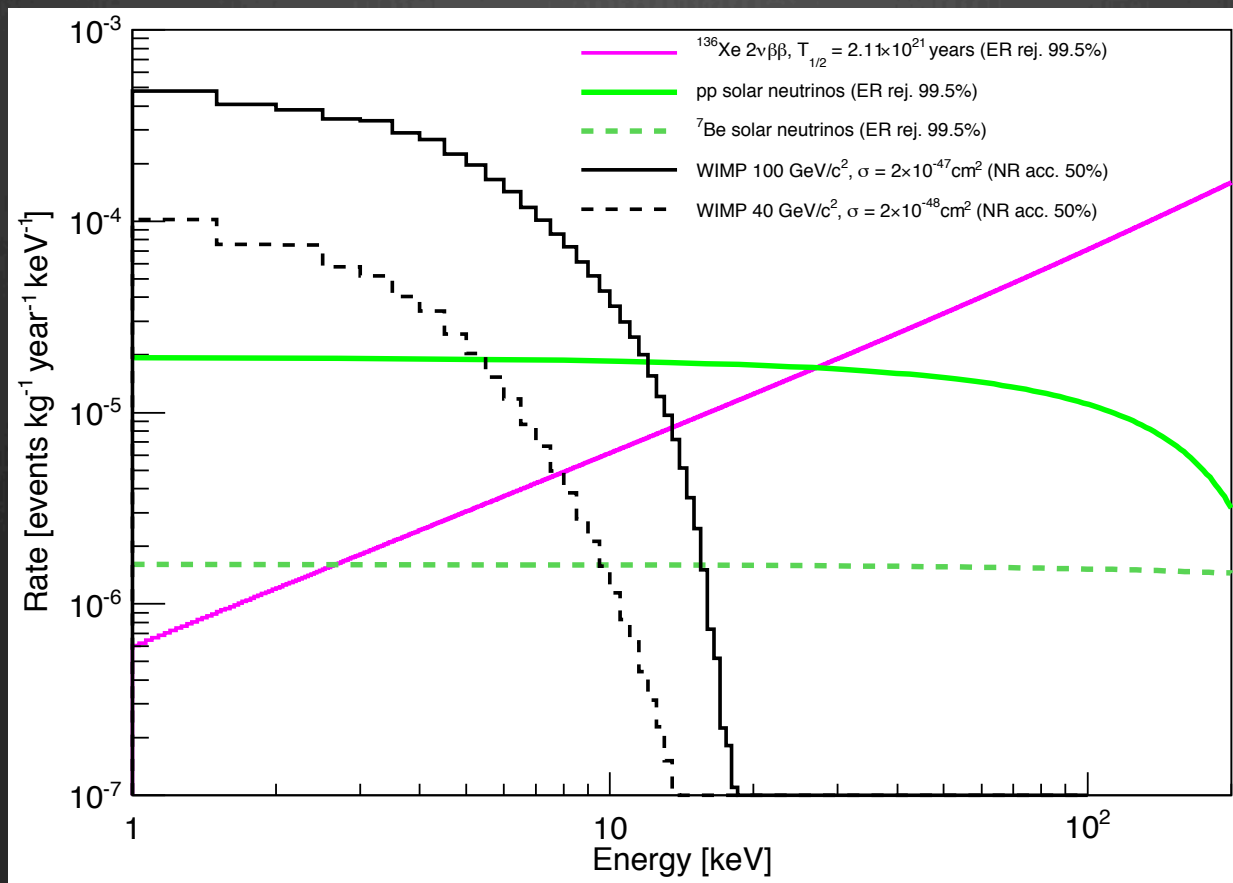
# Darwin

In LNGS environment, NR backgrounds would be subdominant



# Darwin

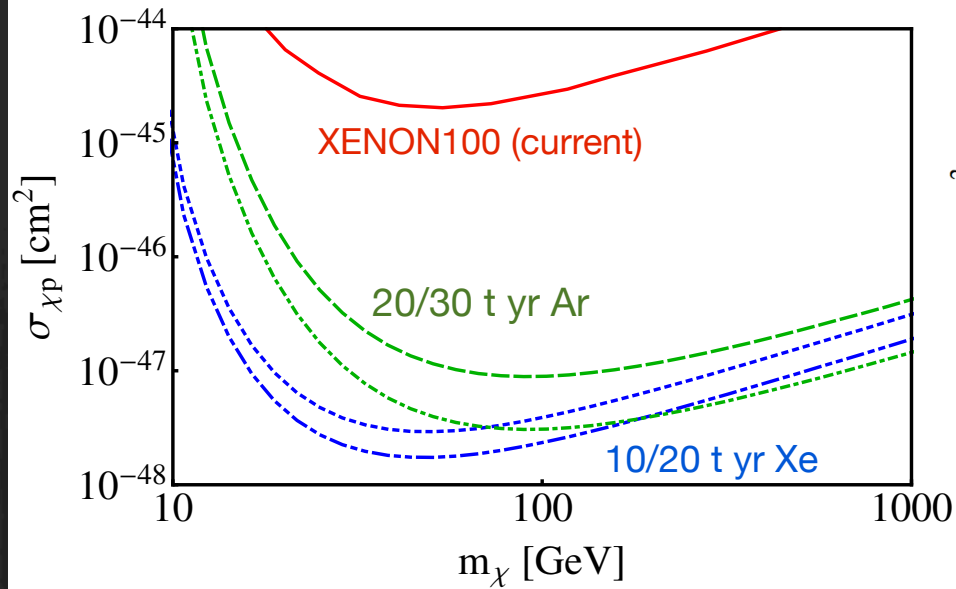
In LNGS environment, NR backgrounds would be subdominant





# Darwin

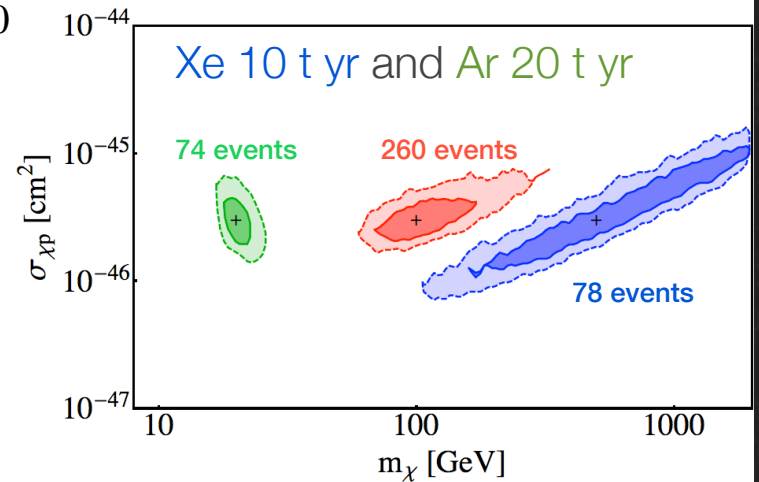
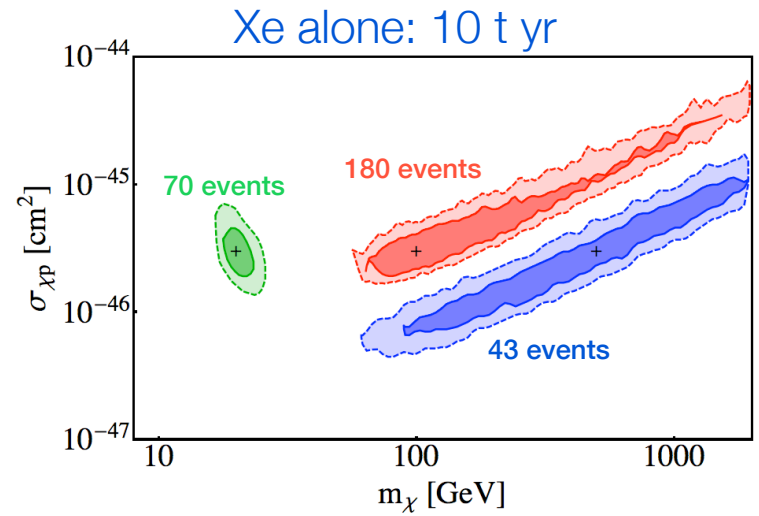
arXiv:1306.3244



$$v_{esc} = 544 \pm 40 \text{ km/s}$$

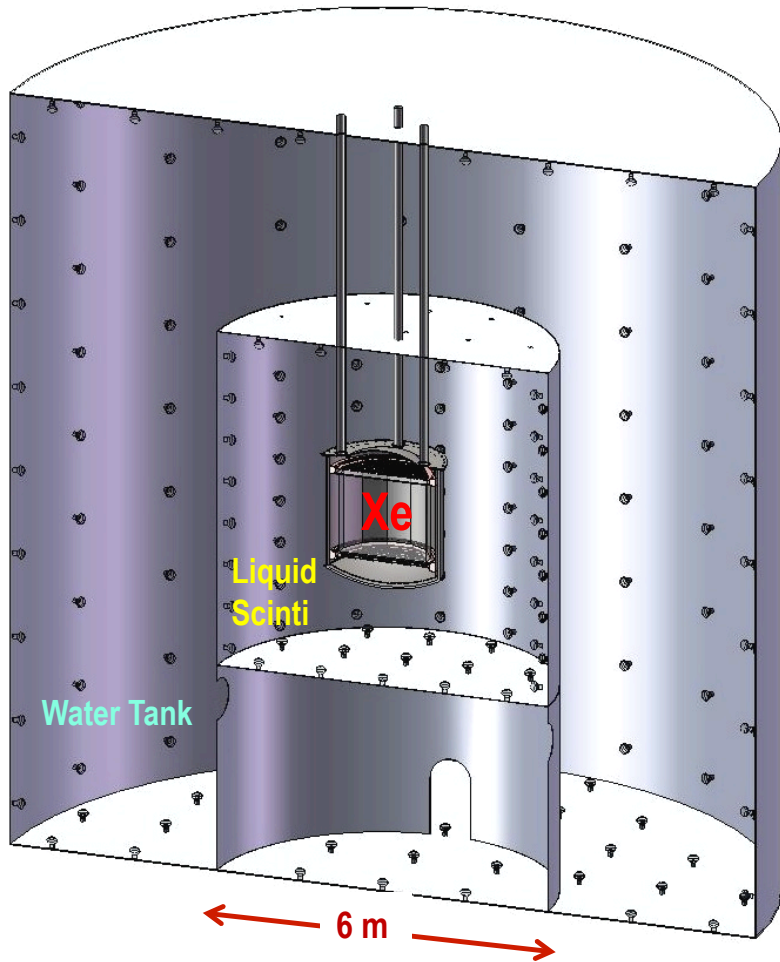
$$v_0 = 220 \pm 20 \text{ km/s}$$

$$\rho_\chi = 0.3 \pm 0.1 \text{ GeV/cm}^3$$

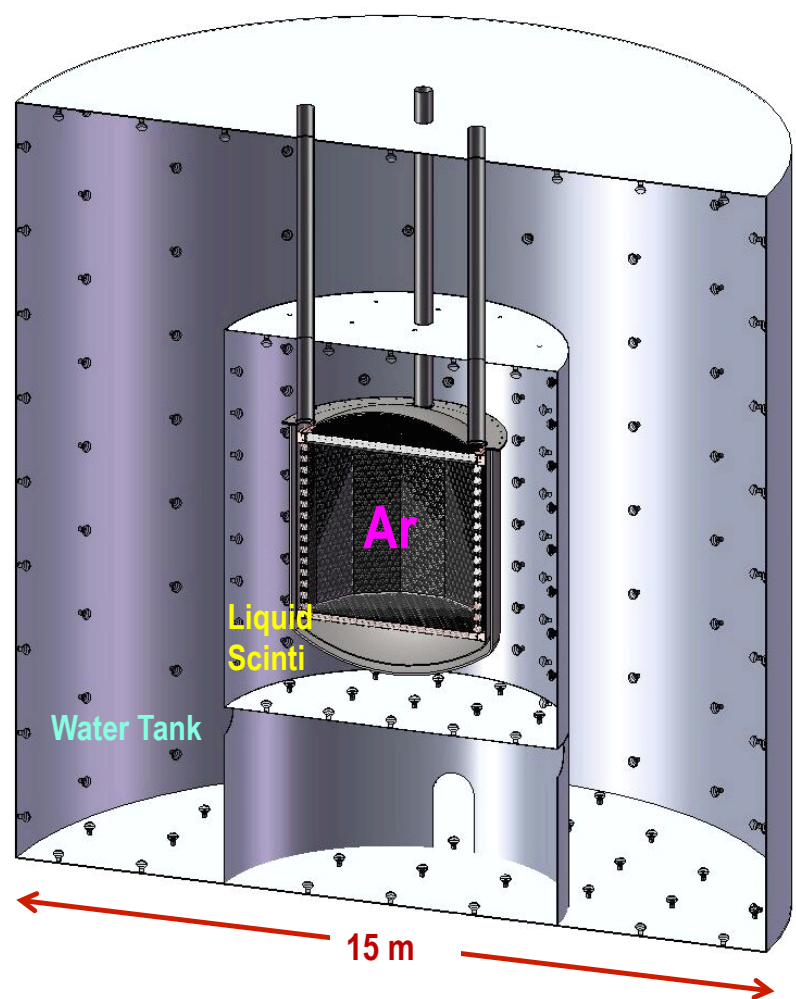


# MAX

Xe 20 ton (10 ton)



$^{40}\text{Ar}$  70 ton (50 ton)



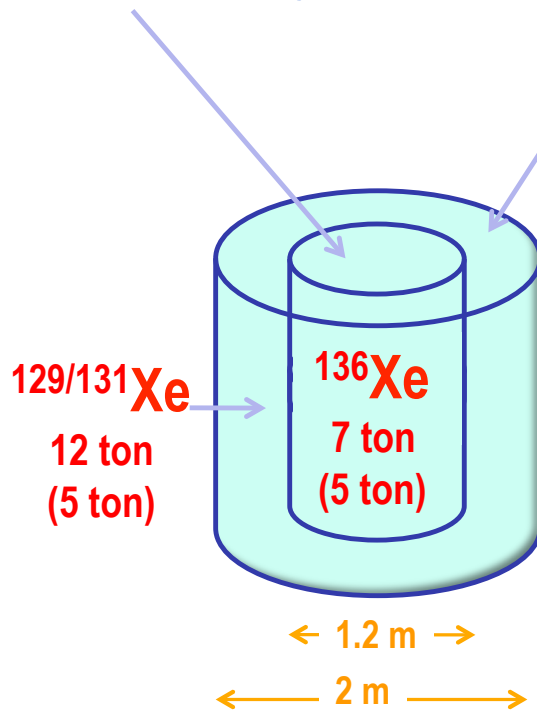
# XAX

arXiv:0808.3968

*WIMP (Spin even)  
Double Beta Decay*

*WIMP (Spin odd)  
pp Solar Neutrino*

*WIMP (Spin even)*



# Projects summary

G	Experiment	Target	Detector	Location	Active mass	Fiducial mass	Year physics	Peak sensitivity
G1	Xenon 100	Xe	TPC	LNGS	62	34	2012	$2 \cdot 10^{-45}$
G1	Dark Side 50	Ar	TPC	LNGS	50	33	2013	$1.5 \cdot 10^{-45}$
G1	Xmass	Xe	single	Kamioka	800	100	2014?	???
G1	LUX	Xe	TPC	SURF	350	100	2014/5	$7 \cdot 10^{-46}$
G1	ArDM	Ar	TPC	Canfranc	850	???	2014/5	???
G2	Deap 3600	Ar	single	SNOLab	3600	1000	2015	$10^{-46}$
G2	MiniClean	Ar/Ne	single	SNOLab	500	150	2015?	--
G2	Xenon 1t	Xe	TPC	LNGS	3500	2200	2017	$2 \cdot 10^{-47}$
G2	DarkSide 5t	Ar	TPC	LNGS	5000	3000	2017	$10^{-47}$
G2	LZS	Xe	TPC	SURF	1500	800	2017	$4 \cdot 10^{-47}$
G3	Darwin	Xe(Ar)	TPC	LNGS?	20t	12t	~2020	$\sim 10^{-48}$
G3	LZD	Xe	TPC	???	20t	12t	~2020	$\sim 10^{-48}$
G3	MAX/XAX	Xe+Ar	2TPCs	DUSEL???	20t+70t	12t+50t	~2020	$\sim 10^{-48}$

# Borexino for Dark Matter?

**J**ournal of **C**osmology and **A**stroparticle **P**hysics  
An IOP and SISSA journal

## Cosmogenic Backgrounds in Borexino at 3800 m water-equivalent depth



The Borexino collaboration

JCAP08(2013)049

# Cosmogenic Neutrons

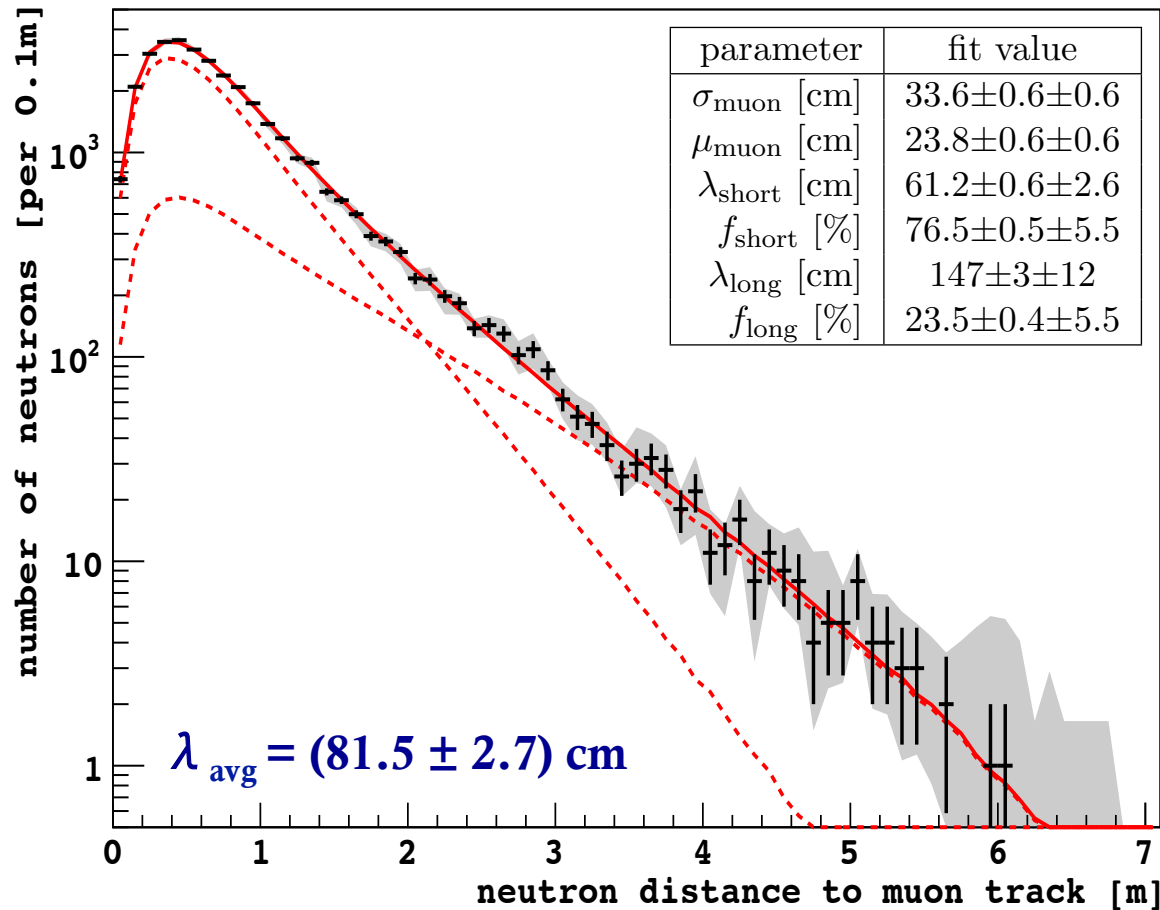
Cosmogenic neutron production  
in organic liquid scintillator:

$$\text{Yield} = (3.10 \pm 0.07_{\text{stat}} \pm 0.08_{\text{syst}}) 10^{-4} \text{ n}/(\mu \text{ g}/\text{cm}^2)$$

$$\text{Flux} = (7.31 \pm 0.17_{\text{stat}} \pm 0.19_{\text{syst}}) \text{ n}/\text{m}^2/\text{d}$$

LNGS	Experiment	Year	$10^{-4} \mu \text{ m}^{-2} \text{ s}^{-1}$	$\mu \text{ m}^{-2} \text{ d}^{-1}$
Hall A	LVD	2009	$3.31 \pm 0.03$	$28.5 \pm 0.2$
Hall B	MACRO	1995	$3.22 \pm 0.08$	$27.8 \pm 0.7$
Hall C	BOREXINO	2012	$3.41 \pm 0.01$	$29.46 \pm 0.08$

# Cosmogenic Neutrons



# Comparing with simulations

Borexino and surrounded area simulated

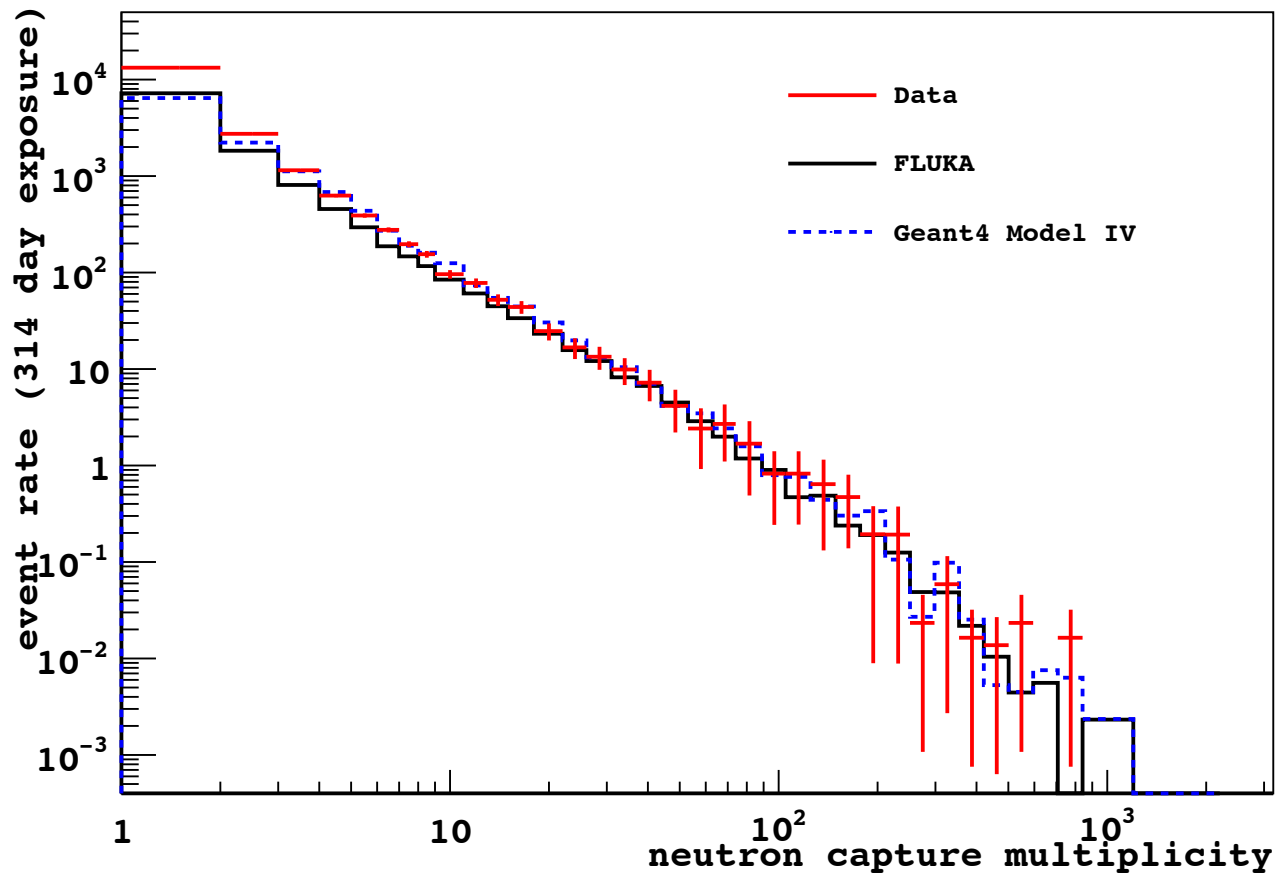
Muon energy and angular distributions from MACRO

$\mu^+ / \mu^- = 1.38$  from OPERA

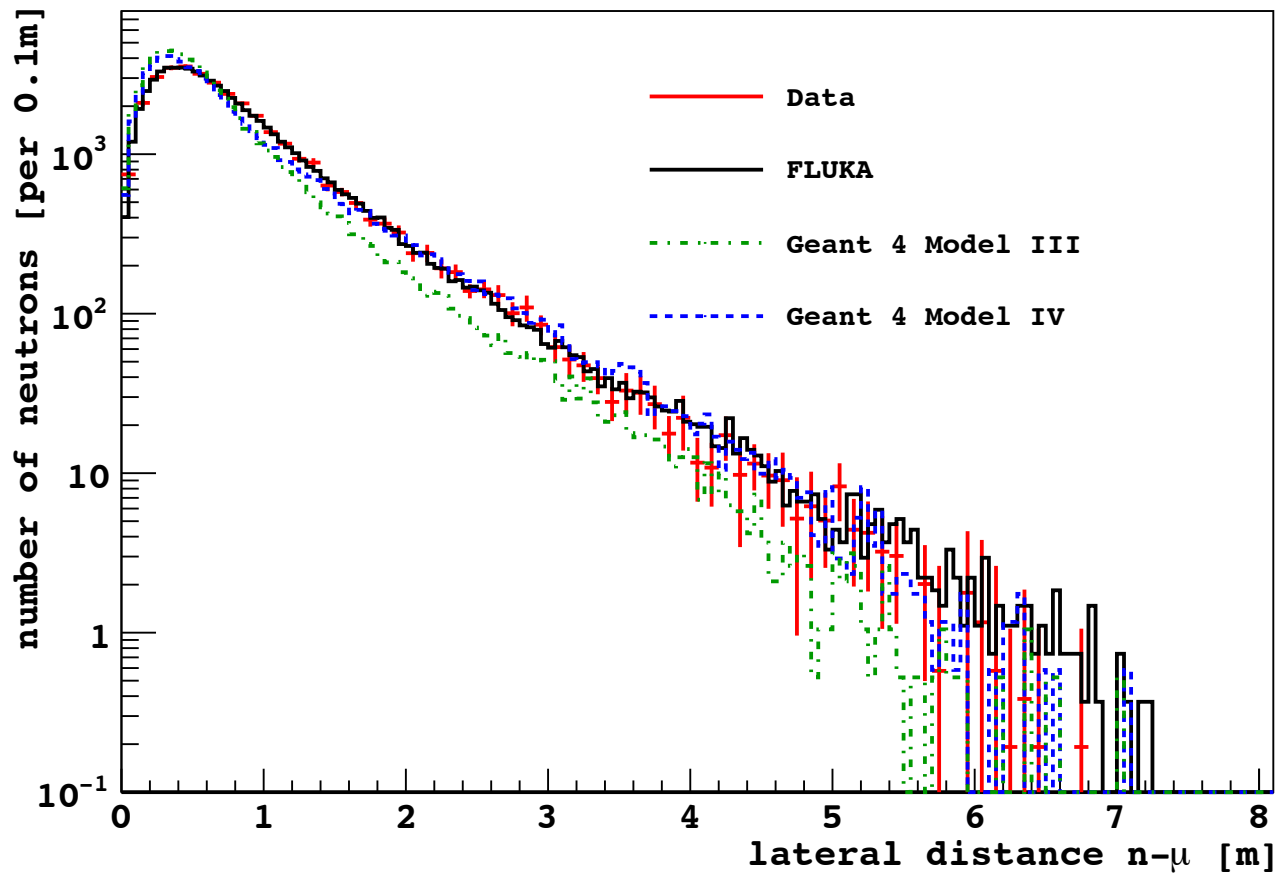
	<b>GEANT4</b> Model III	<b>GEANT4</b> Model IV	<b>FLUKA</b>	<b>Borexino</b>	<b>KamLAND</b>
		— $\langle E_\mu \rangle = 283 \pm 19 \text{ GeV}$ —			$\langle E_\mu \rangle = 260 \pm 8 \text{ GeV}$
<b>Isotopes</b>	Yield $[10^{-7} (\mu \text{ g/cm}^2)^{-1}]$				
$^{12}\text{N}$	$1.11 \pm 0.13$	$3.0 \pm 0.2$	$0.5 \pm 0.2$	$< 1.1$	$1.8 \pm 0.4$
$^{12}\text{B}$	$30.1 \pm 0.7$	$29.7 \pm 0.7$	$28.8 \pm 1.9$	$56 \pm 3$	$42.9 \pm 3.3$
$^8\text{He}$	$< 0.04$	$0.18 \pm 0.05$	$0.30 \pm 0.15$	$< 1.5$	$0.7 \pm 0.4$
$^9\text{Li}$	$0.6 \pm 0.1$	$1.68 \pm 0.16$	$3.1 \pm 0.4$	$2.9 \pm 0.3$	$2.2 \pm 0.2$
$^8\text{B}$	$0.52 \pm 0.09$	$1.44 \pm 0.15$	$6.6 \pm 0.6$	$14 \pm 6$	$8.4 \pm 2.4$
$^6\text{He}$	$18.5 \pm 0.5$	$8.9 \pm 0.4$	$17.3 \pm 1.1$	$38 \pm 15$	not reported
$^8\text{Li}$	$27.7 \pm 0.7$	$7.8 \pm 0.4$	$28.8 \pm 1.0$	$7 \pm 7$	$12.2 \pm 2.6$
$^9\text{C}$	$0.16 \pm 0.05$	$0.99 \pm 0.13$	$0.91 \pm 0.10$	$< 16$	$3.0 \pm 1.2$
$^{11}\text{Be}$	$0.24 \pm 0.06$	$0.45 \pm 0.09$	$0.59 \pm 0.12$	$< 7.0$	$1.1 \pm 0.2$
$^{10}\text{C}$	$15.0 \pm 0.5$	$41.1 \pm 0.8$	$14.1 \pm 0.7$	$18 \pm 5$	$16.5 \pm 1.9$
$^{11}\text{C}$	$315 \pm 2$	$415 \pm 3$	$467 \pm 23$	$886 \pm 115$	$866 \pm 153$
<b>Neutrons</b>	Yield $[10^{-4} (\mu \text{ g/cm}^2)^{-1}]$				
	$3.01 \pm 0.05$	$2.99 \pm 0.03$	$2.46 \pm 0.12$	$3.10 \pm 0.11$	$2.79 \pm 0.31$



# Comparing n multiplicity



# Comparing lateral distance



# Laboratory needs

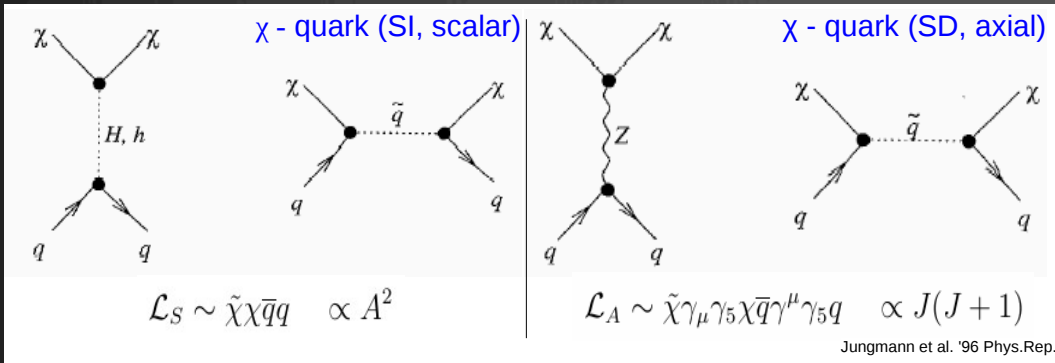
- ⊗ Service lines: cooling, network,...
- ⊗ Standard laboratory services
- ⊗ Machine shop, chemistry lab, electronics lab,,computing.
- ⊗ Desiderata:
  - ⊗ Radon free clean room
  - ⊗ PMT test facility (above ground)

# Conclusions

- ⊗ Noble gases are and will be driving dark matter searches at large masses (above LHC limit).
- ⊗ LXe and (depleted) LAr will both be pursued as complementary approaches.
- ⊗ 2014: G1 projects coming to a conclusion.
- ⊗ 2017: G2 projects should perform physics runs.
- ⊗ 2020: G3 projects at multi-ton scales plan to converge.

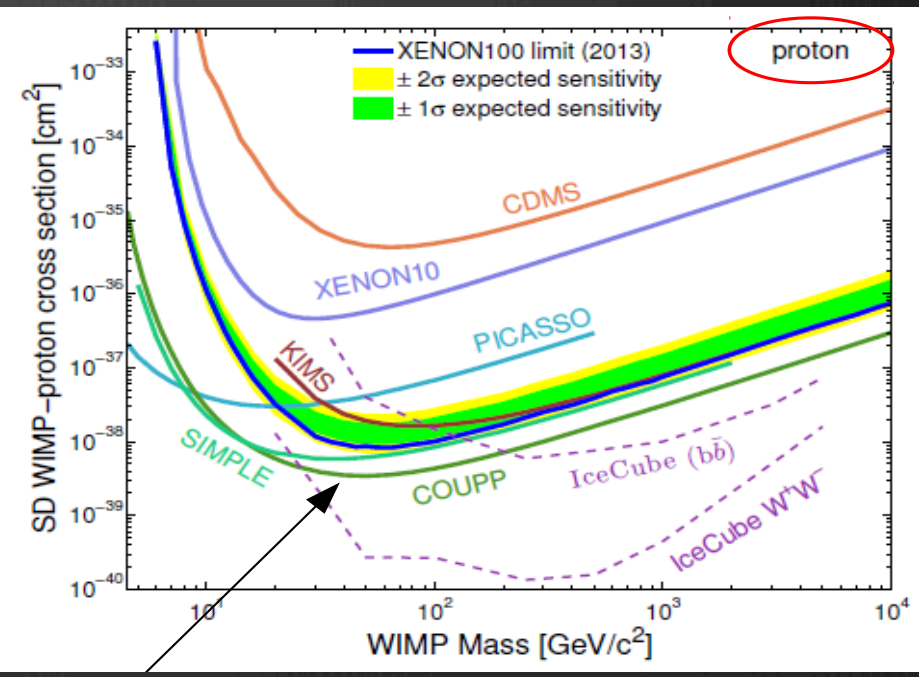
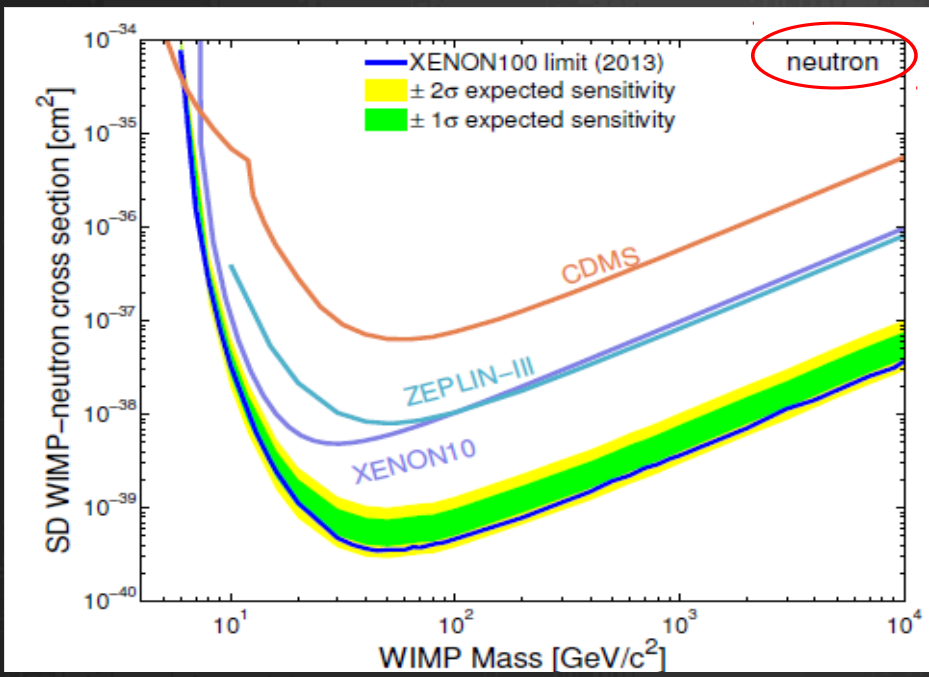
thanks for material to Marc Schumann, Laura Baudis, Cristiano Galbiati

# Xenon 100 – Spin Dependant



$$\frac{d\sigma}{d|\mathbf{q}|^2} = \frac{C_{spin}}{v^2} G_F^2 \frac{S(|\mathbf{q}|)}{S(0)}$$

$$C_{spin} = \frac{8}{\pi} [a_p \langle S_p \rangle + a_n \langle S_n \rangle]^2 \frac{J+1}{J}$$



# Geant4 models

<b>Model I</b>	<b>HP</b>	<b>Binary</b>	<b>Bertini</b>	<b>FTF</b>
Protons		$0 \rightarrow 5 \text{ GeV}$		$4 \text{ GeV} \rightarrow 100 \text{ TeV}$
Neutrons	$0 \rightarrow 20 \text{ MeV}$	$19.9 \text{ MeV} \rightarrow 5 \text{ GeV}$		$4 \text{ GeV} \rightarrow 100 \text{ TeV}$
$\pi$		$0 \rightarrow 5 \text{ GeV}$		$4 \text{ GeV} \rightarrow 100 \text{ TeV}$
K			$0 \rightarrow 5 \text{ GeV}$	$4 \text{ GeV} \rightarrow 100 \text{ TeV}$
<b>Model II</b>	<b>HP</b>	<b>Bertini</b>	<b>FTF</b>	
Protons		$0 \rightarrow 5 \text{ GeV}$	$4 \text{ GeV} \rightarrow 100 \text{ TeV}$	
Neutrons	$0 \rightarrow 20 \text{ MeV}$	$19.9 \text{ MeV} \rightarrow 5 \text{ GeV}$	$4 \text{ GeV} \rightarrow 100 \text{ TeV}$	
$\pi, \text{ K}$		$0 \rightarrow 5 \text{ GeV}$	$4 \text{ GeV} \rightarrow 100 \text{ TeV}$	
<b>Model III</b>	<b>HP</b>	<b>Binary</b>	<b>LEP</b>	<b>QGS</b>
Protons		$0 \rightarrow 9.9 \text{ GeV}$	$9.5 \rightarrow 25 \text{ GeV}$	$12 \text{ GeV} \rightarrow 100 \text{ TeV}$
Neutrons	$0 \rightarrow 20 \text{ MeV}$	$19.9 \text{ MeV} \rightarrow 9.9 \text{ GeV}$	$9.5 \rightarrow 25 \text{ GeV}$	$12 \text{ GeV} \rightarrow 100 \text{ TeV}$
$\pi, \text{ K}$		$0 \rightarrow 9.9 \text{ GeV}$	$9.5 \rightarrow 25 \text{ GeV}$	$12 \text{ GeV} \rightarrow 100 \text{ TeV}$
<b>Model IV</b>	<b>HP</b>	<b>Bertini</b>	<b>LEP</b>	<b>QGS</b>
Protons		$0 \rightarrow 9.9 \text{ GeV}$	$9.5 \rightarrow 25 \text{ GeV}$	$12 \text{ GeV} \rightarrow 100 \text{ TeV}$
Neutrons	$0 \rightarrow 20 \text{ MeV}$	$19.9 \text{ MeV} \rightarrow 9.9 \text{ GeV}$	$9.5 \rightarrow 25 \text{ GeV}$	$12 \text{ GeV} \rightarrow 100 \text{ TeV}$
$\pi, \text{ K}$		$0 \rightarrow 9.9 \text{ GeV}$	$9.5 \rightarrow 25 \text{ GeV}$	$12 \text{ GeV} \rightarrow 100 \text{ TeV}$