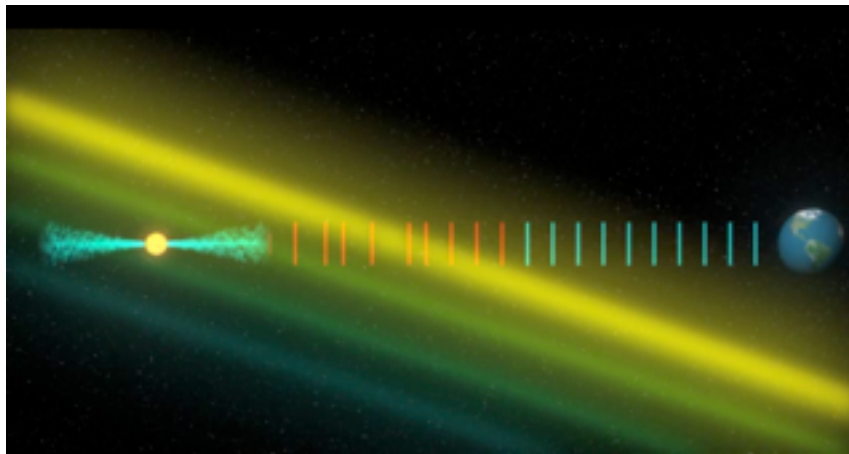
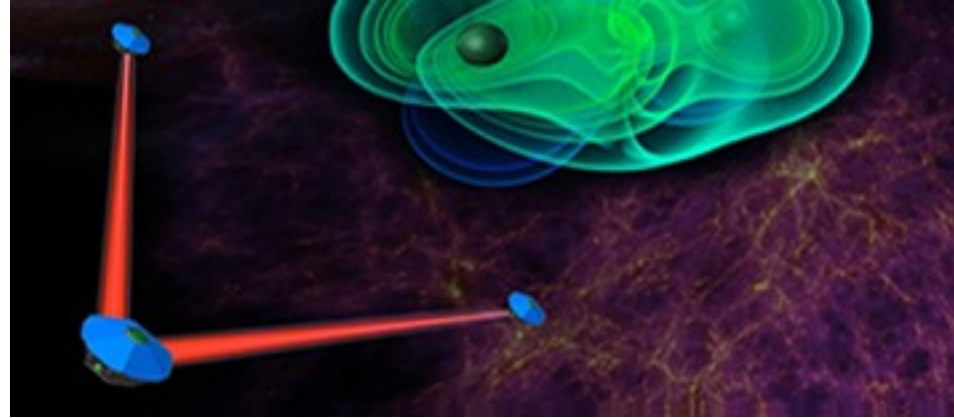
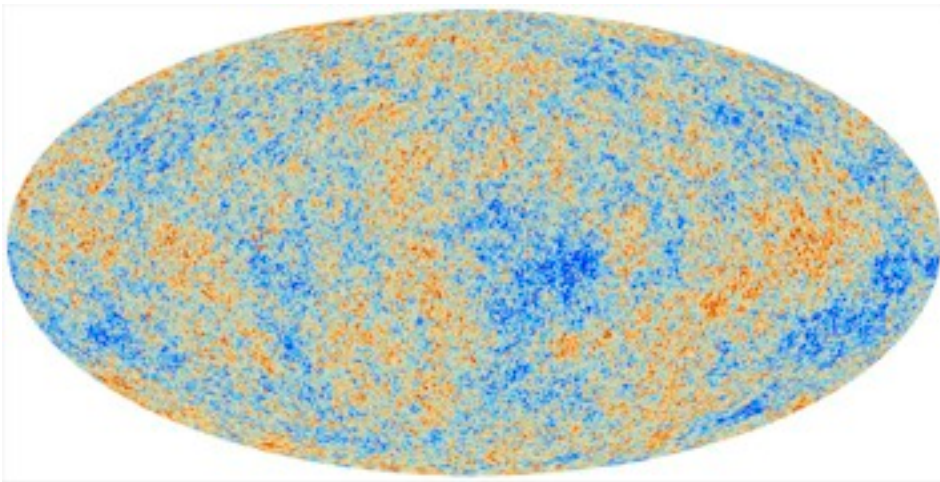


# Gravitational Wave Cosmology



How will we be able to exploit direct gravitational wave measurements for cosmology? What will this bring us?

# Outline

- Basics: What gravitational waves are and how to measure them
- Why: The potential importance of GWs for astronomy and cosmology, broadly speaking
- How: Ongoing and upcoming efforts to measure GWs
- Specifics: Several ways in which GWs can bring us cosmologically important data.
  - Relic waves (direct imprint of inflation)
  - Precise distances (“standard sirens”)
  - Early growth of black holes (tracer of early structure)

# Basic basics

Gravitational radiation *necessary* in any relativistic gravity theory: Must causally communicate changes in the gravitational field.

GR: Tides (“curvature”) play role similar to electric and magnetic fields in E&M ... radiation takes form of propagating tidal gravitational force.

Leading radiation *quadrupolar*: monopole protected by energy conservation; dipole protected by conservation of momentum.

$$h = \frac{2G}{c^4} \frac{1}{r} \frac{d^2 Q}{dt^2}$$
$$\simeq \frac{2G}{c^4} \frac{1}{r} \times mv^2$$

# Indirect measurement

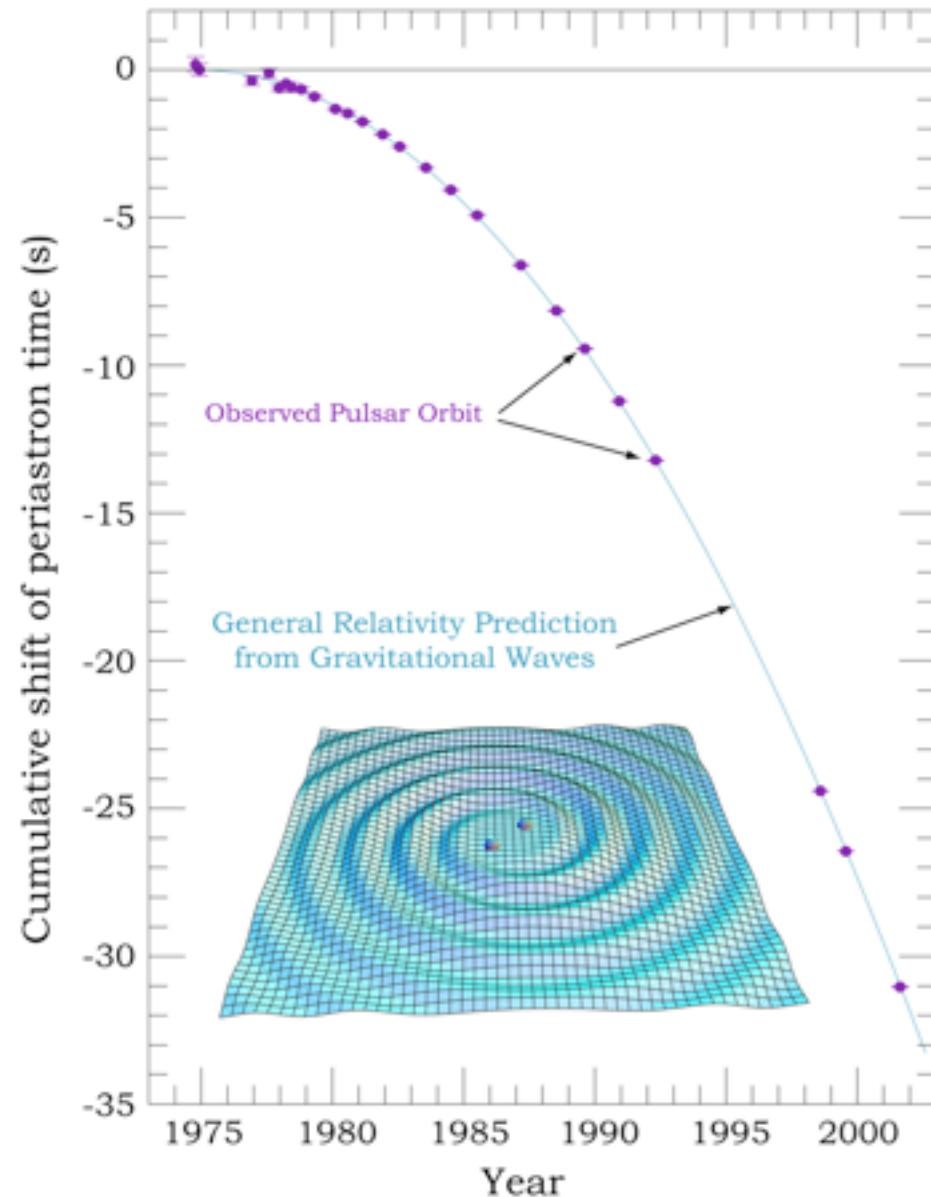
Binary stars with rapidly varying quadrupole moment lose energy due to GWs.

First one discovered in 1975; detailed study over decades showed orbit decay at

***\*exactly\****

the rate predicted for GW emission.

Several such systems now known, all agree with GWs.



# Direct measurement

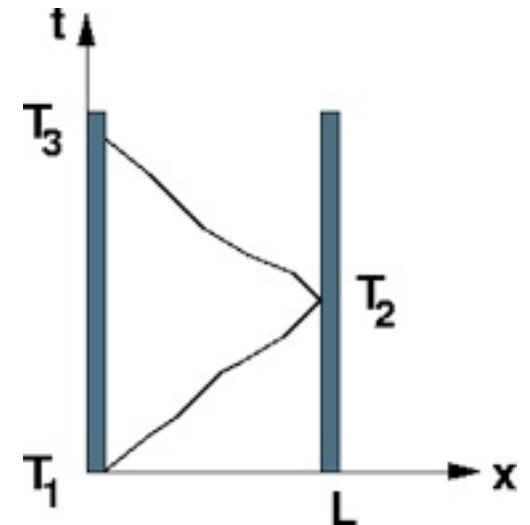
The GW is an oscillation in spacetime, has an impact on propagation of light:

$$ds^2 = -c^2 dt^2 + [1 + h(t, x)] dx^2 = 0$$

Speed of light in this coordinate system:

$$\frac{dx}{dt} = \frac{c}{\sqrt{1 + h(t, x)}}$$

Imagine mirrors that fall freely in this spacetime. Bounce light, record time between bounces.




# Direct measurement

The GW  $h$  is an oscillation in spacetime, has an impact on propagation of light:

$$ds^2 = -c^2 dt^2 + [1 + h(t, x)] dx^2 = 0$$

Interval between bounces:

$$\Delta T = \int \frac{dx}{dx/dt} \simeq \frac{1}{c} \int \left[ 1 - \frac{1}{2} h(t, x) \right] dx$$


GW enters as oscillation in interval  
(Bondi 1957).



# Magnitude of effect

Size of effect for interesting astrophysical sources can be estimated using

$$h \simeq \frac{G}{c^4} \frac{2mv^2}{r}$$

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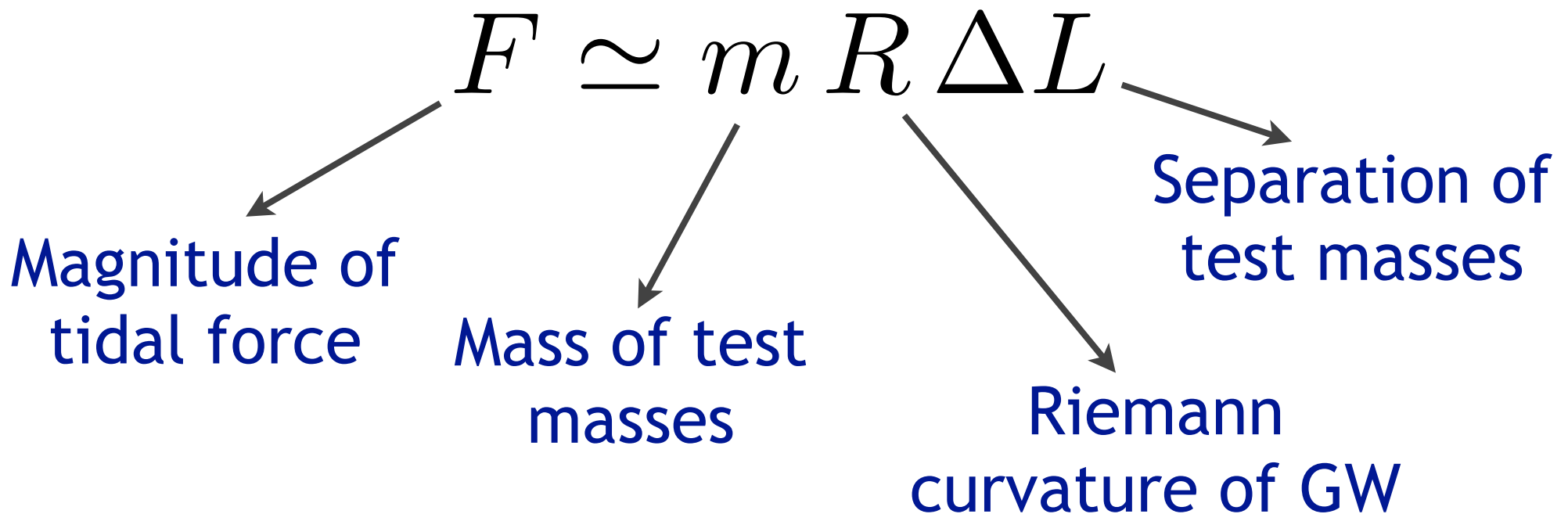
$$h \sim 10^{-21} \text{ — } 10^{-23}$$

# Not as bad as you might guess

Recall GW acts as a *tide*: Can convert GW *strain* to tidal *force*. Gives a good sense of challenge for isolating from noise:

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Recall GW acts as a *tide*: Can convert GW *strain* to tidal *force*. Gives a good sense of challenge for isolating from noise:

$$F \simeq m R \Delta L$$

Plug in

$$R \simeq \omega^2 h$$

# Not as bad as you might guess

Recall GW acts as a *tide*: Can convert GW *strain* to tidal *force*. Gives a good sense of challenge for isolating from noise:

$$F \approx 1 \text{ piconewton} \left( \frac{m}{10 \text{ kg}} \right) \left( \frac{f}{100 \text{ Hz}} \right)^2 \left( \frac{4000 \text{ m}}{\Delta L} \right) \left( \frac{h}{10^{-22}} \right)$$

... small, but not ridiculous!

Comparable to weight of an animal cell.

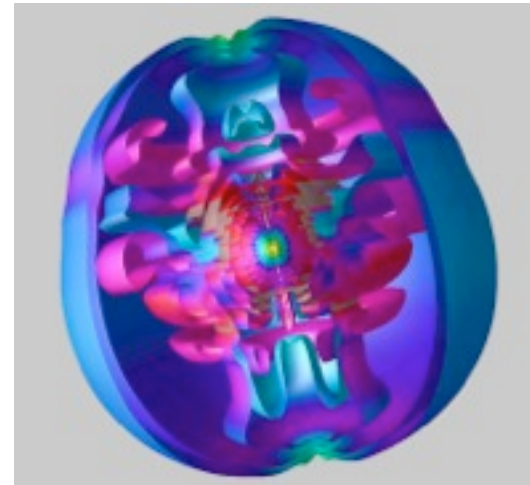
Measuring GWs requires isolating from forces of this magnitude in chosen frequency band.

# What we gain

Weakness of GWs is a curse as we try to measure them ... but it becomes a *blessing* when we begin to interpret the information that a measured wave carries.

Reason: Waves barely interact with matter as they propagate from their source.

Carry a “pristine” map of source dynamics.



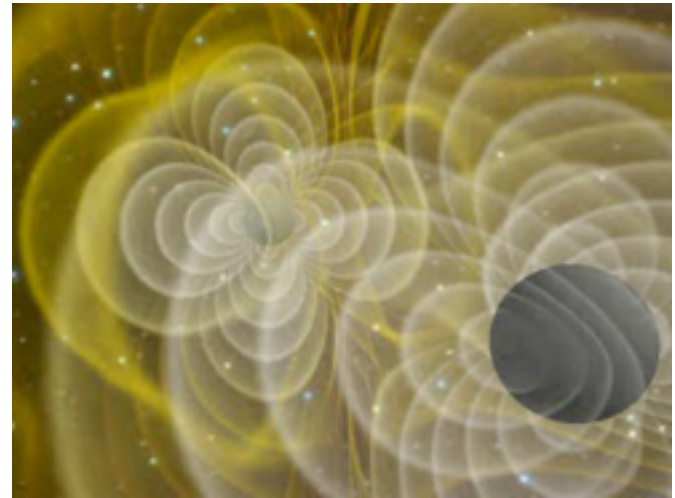
Inner engine of supernovae:  
Directly imprinted on core  
collapse waveform

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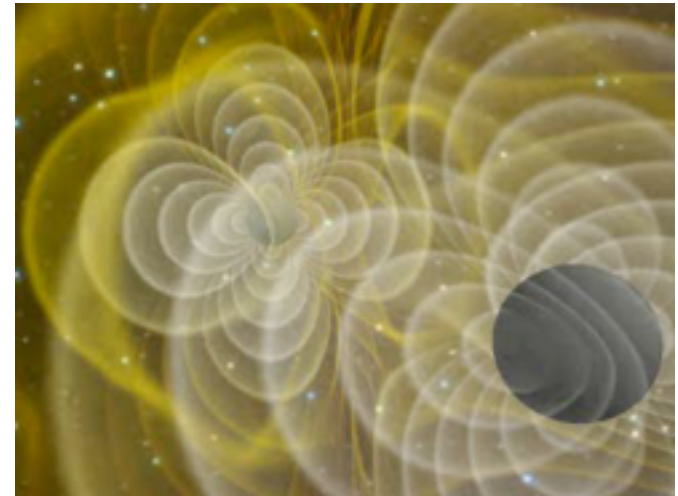
Gravitational dynamics of interacting black holes likewise imprinted on GWs.



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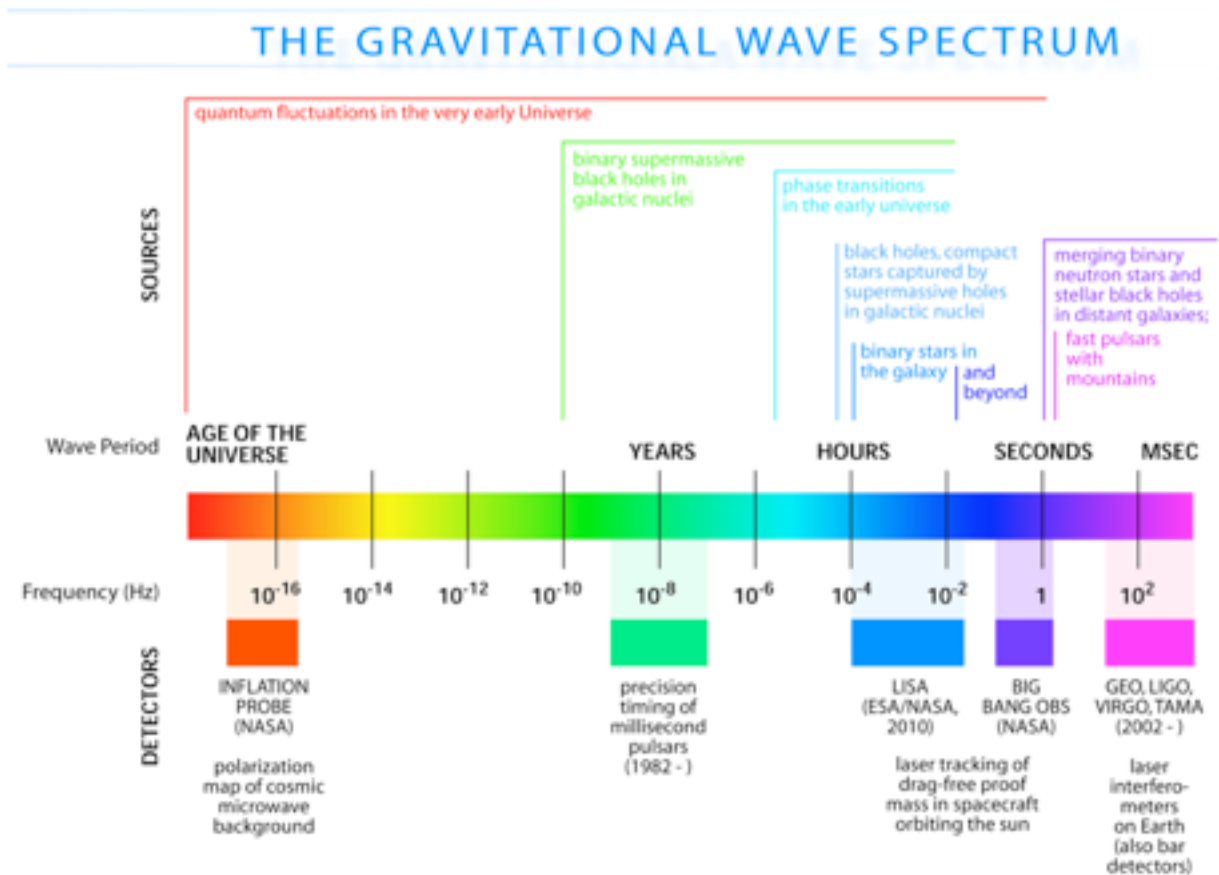
For cosmology, only strong effect on waves is gravitational lensing ... propagate unimpeded from very early redshifts to our detectors.



Gravitational dynamics of interacting black holes likewise imprinted on GWs.

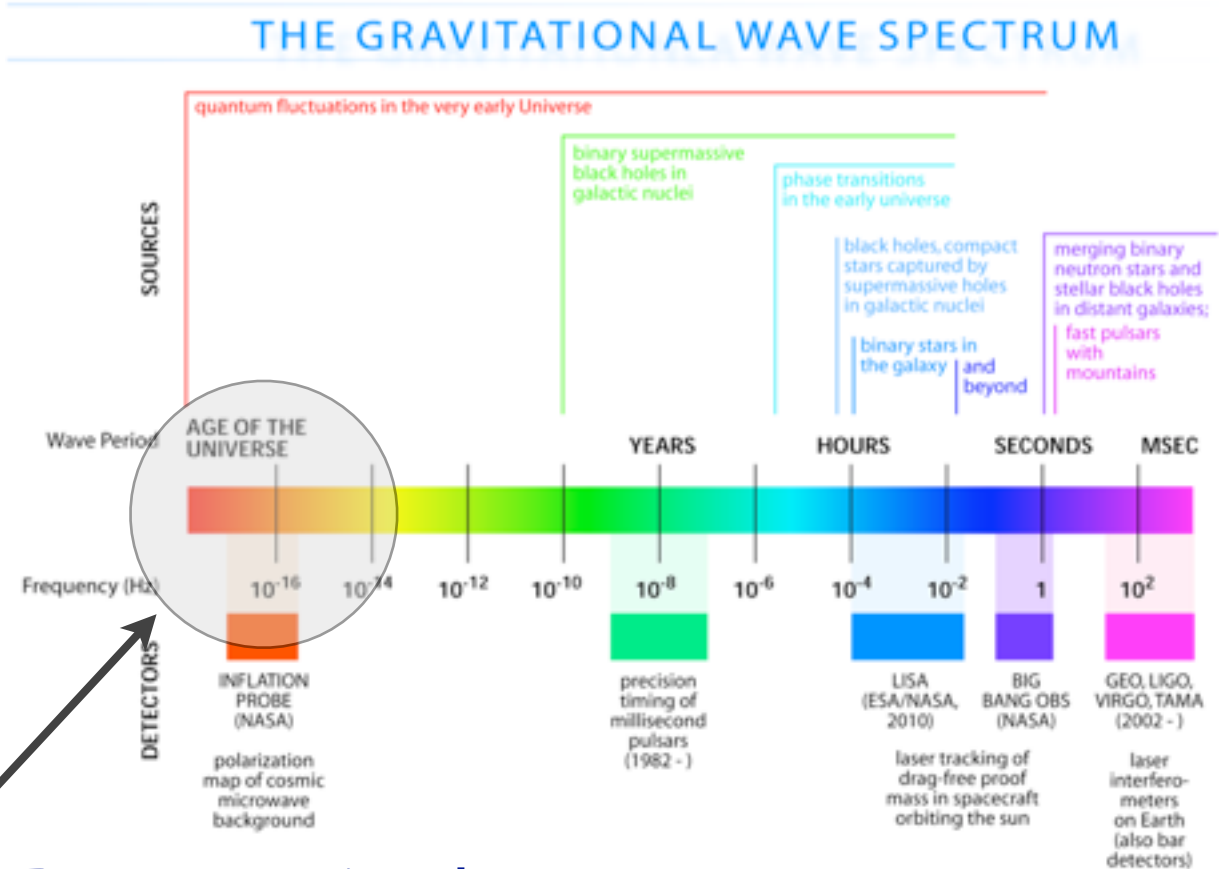
# Programs to measure GWs

How you measure waves depends on where in spectrum you are probing.

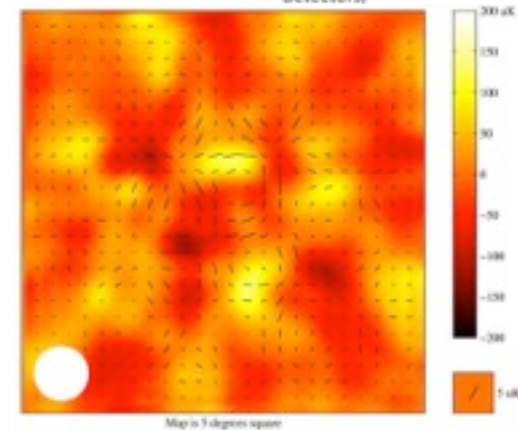


# Programs to measure GWs

How you measure waves depends on where in spectrum you are probing.



Lowest frequencies: Detector is plasma at recombination. Tidal GWs imprint unique signature in polarization of photons that begin free-streaming at that time.



# Programs to measure GWs

More specifically, use the fact that CMB polarization can be decomposed by parity:

Image by Seljak and Zaldarriaga

<http://www.phy.princeton.edu/cosmology/capmap/polscience.html>

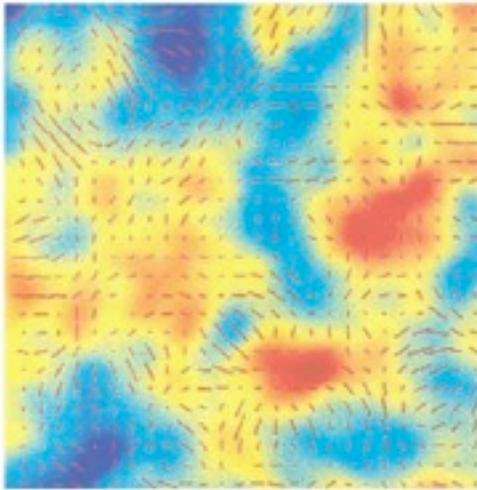
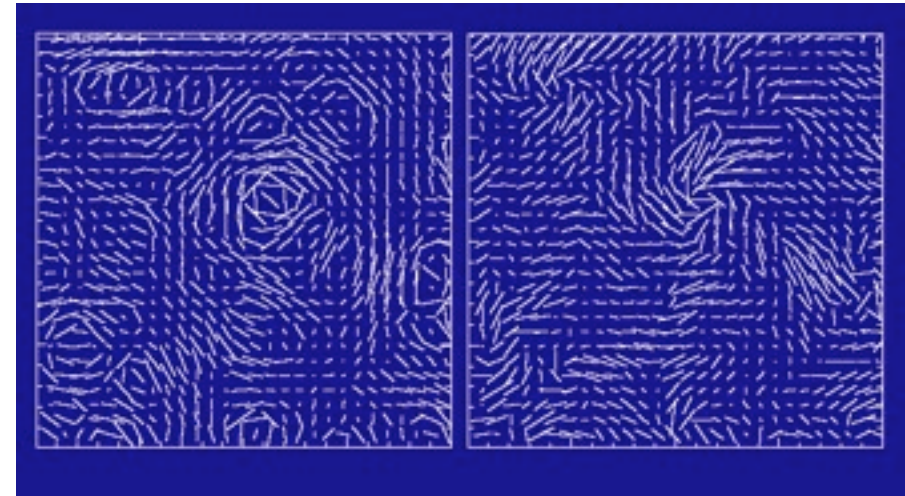


Image by Wayne Hu

<http://background.uchicago.edu/~whu/intermediate/Polarization/polar5.html>



Even parity polarization modes

Odd parity polarization modes



# Programs to measure GWs

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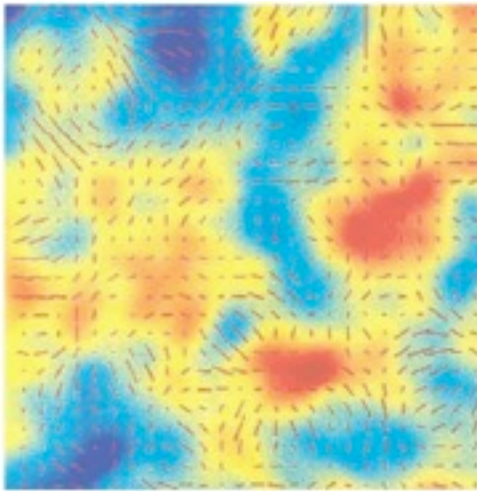
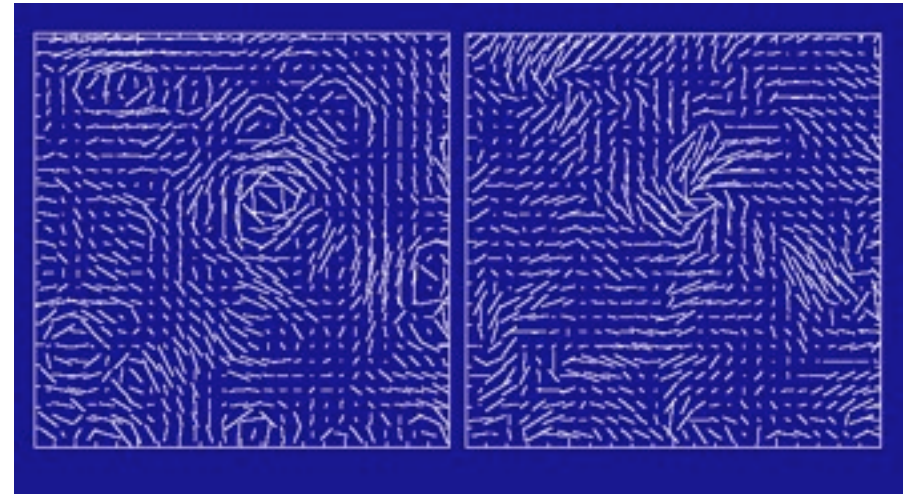


Image by Wayne Hu

<http://background.uchicago.edu/~whu/intermediate/Polarization/polar5.html>



Even parity ( $E$ -modes): Sourced by fluctuations in inflation field (with a small contribution from spacetime fluctuations – ie, GWs).

# Programs to measure GWs

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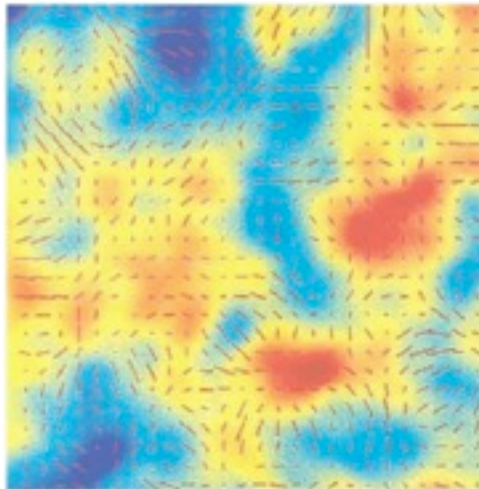
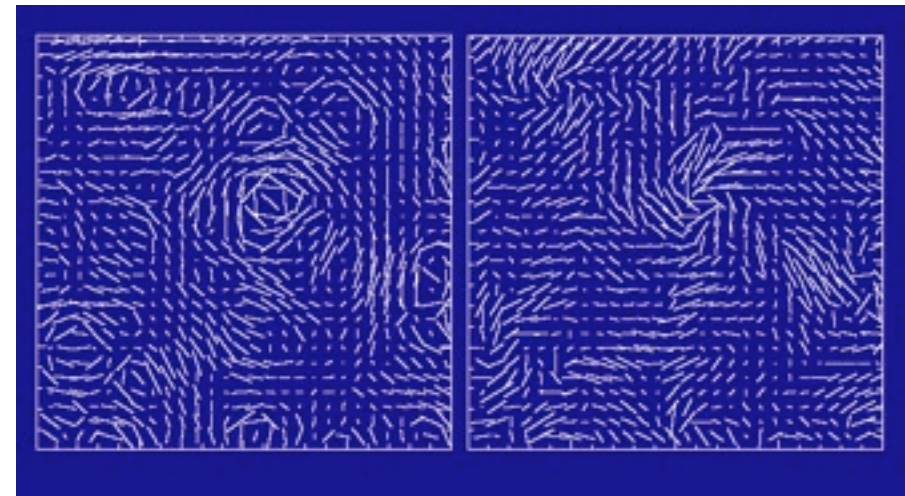


Image by Wayne Hu

<http://background.uchicago.edu/~whu/intermediate/Polarization/polar5.html>



Odd parity (*B*-modes): Modes fundamentally arise *only* from spacetime fluctuations – GWs!

(Plus foreground “noise” from gravitational lensing: Turns *E*-modes into *B*-modes. Signal describing mass distribution ... but noise for GWs.)

# Programs to measure GWs

More specifically, use the fact that CMB polarization can be decomposed by parity:

Image by Seljak and Zaldarriaga

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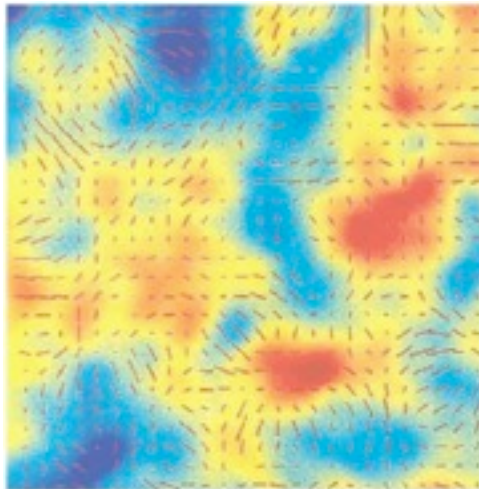
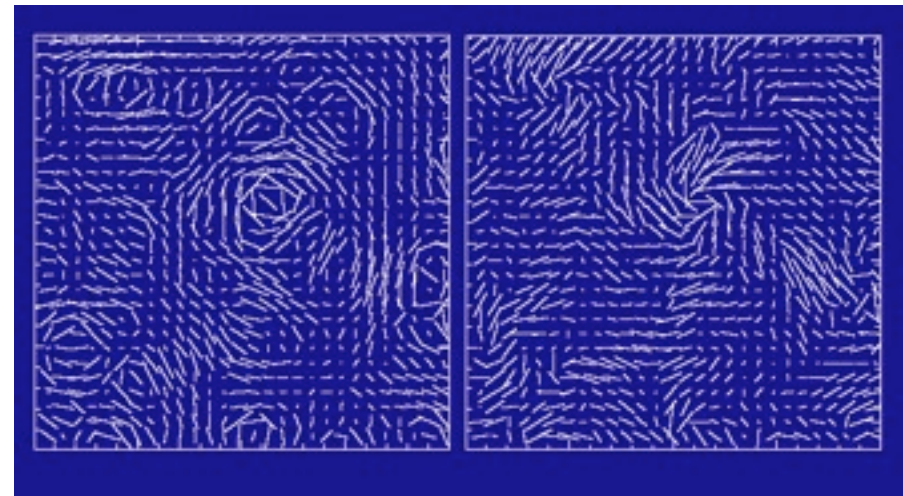


Image by Wayne Hu

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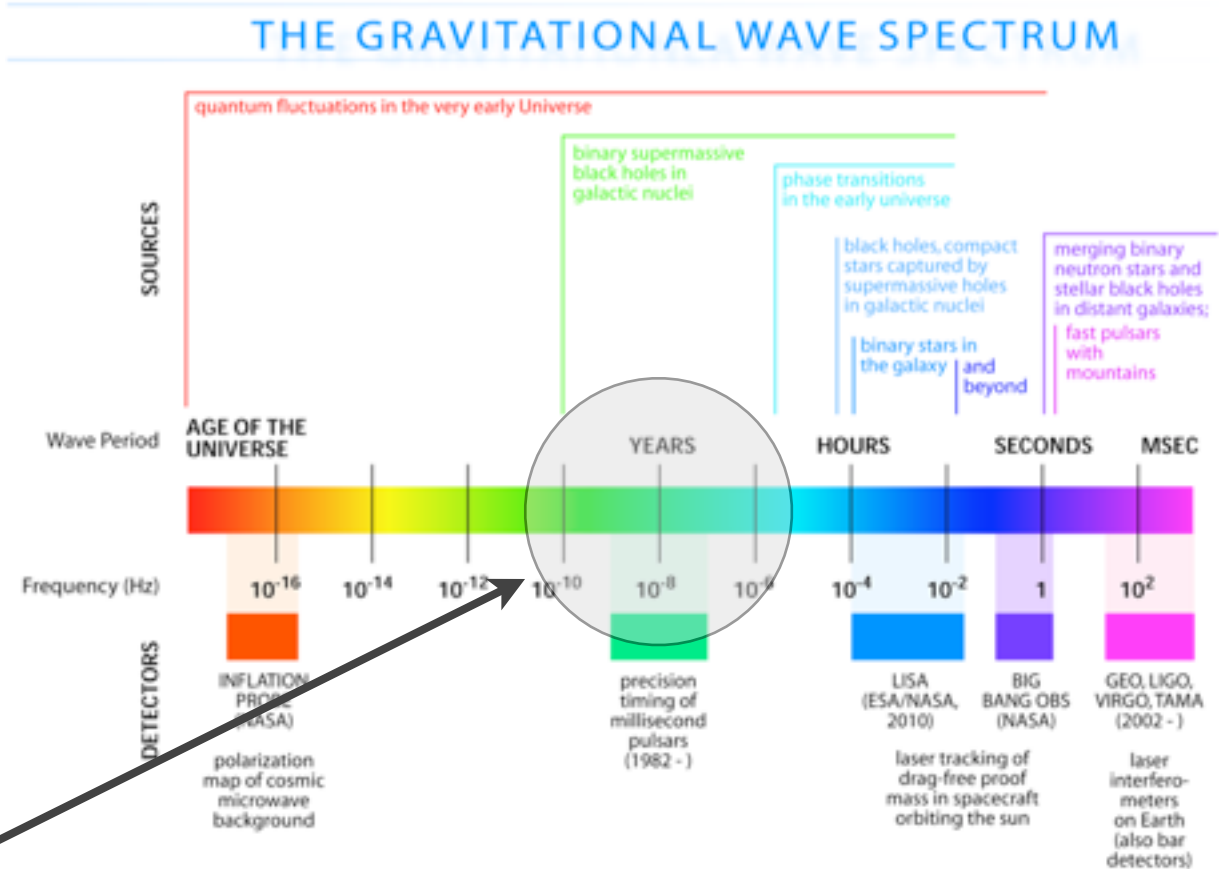
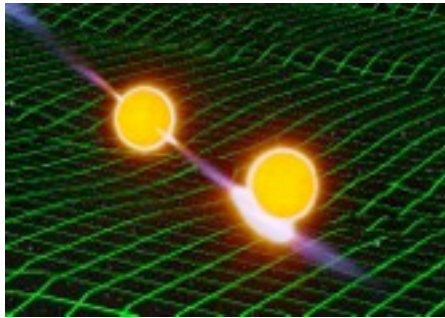


**Direct detection of  $B$ -modes – plus detailed understanding of foregrounds from lensing – measures GWs on longest length scales.**



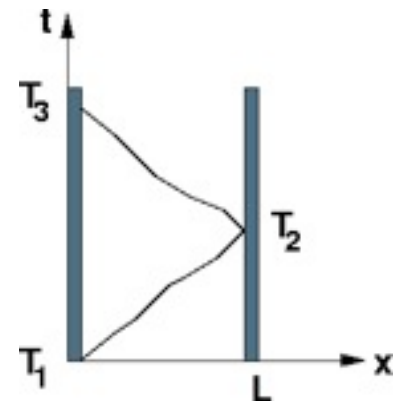
# Programs to measure GWs

How you measure waves depends on where in spectrum you are probing.



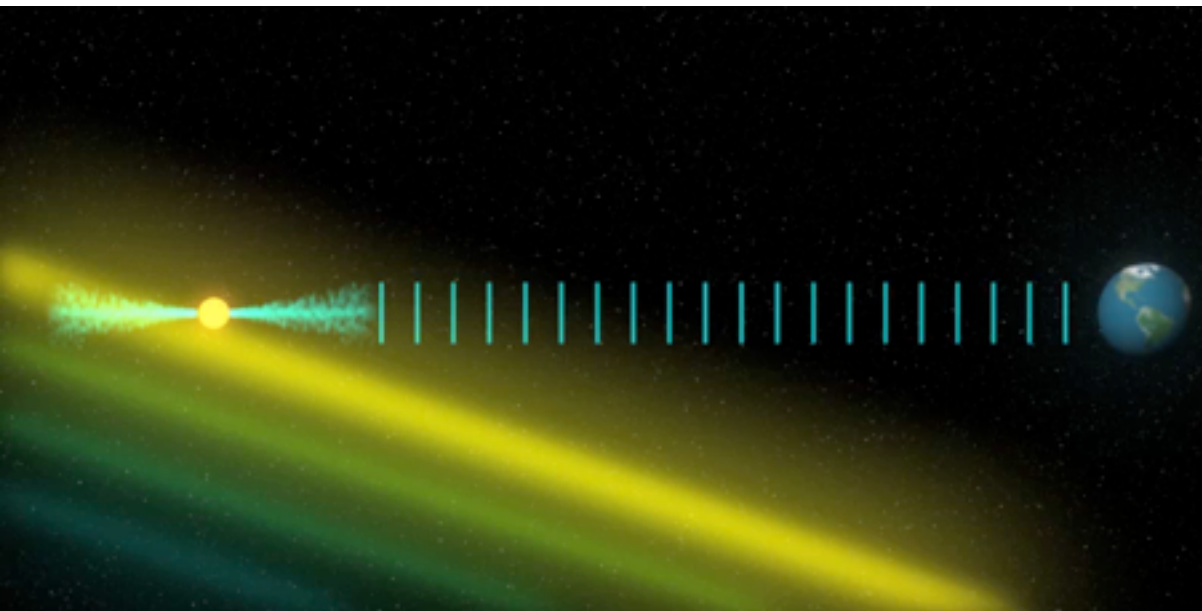
Year periods: Millisecond pulsars as light source, radio telescope as receiver. Enough pulsars & control of timing noise, can detect backgrounds!

***Currently sets best limit.***



# NANOGrav (nanograv.org)

Developing network of pulsars with “nice” properties that can be used as clocks to detect GWs with periods of months to years.



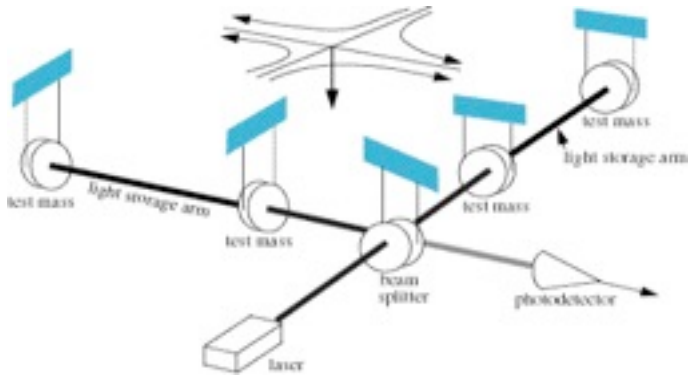
Presently: ~30 pulsars in network; set upper limit on a “stochastic background” of waves in this band.

Movie courtesy Penn State Gravitational Wave Astronomy Group,  
<http://gwastro.org>

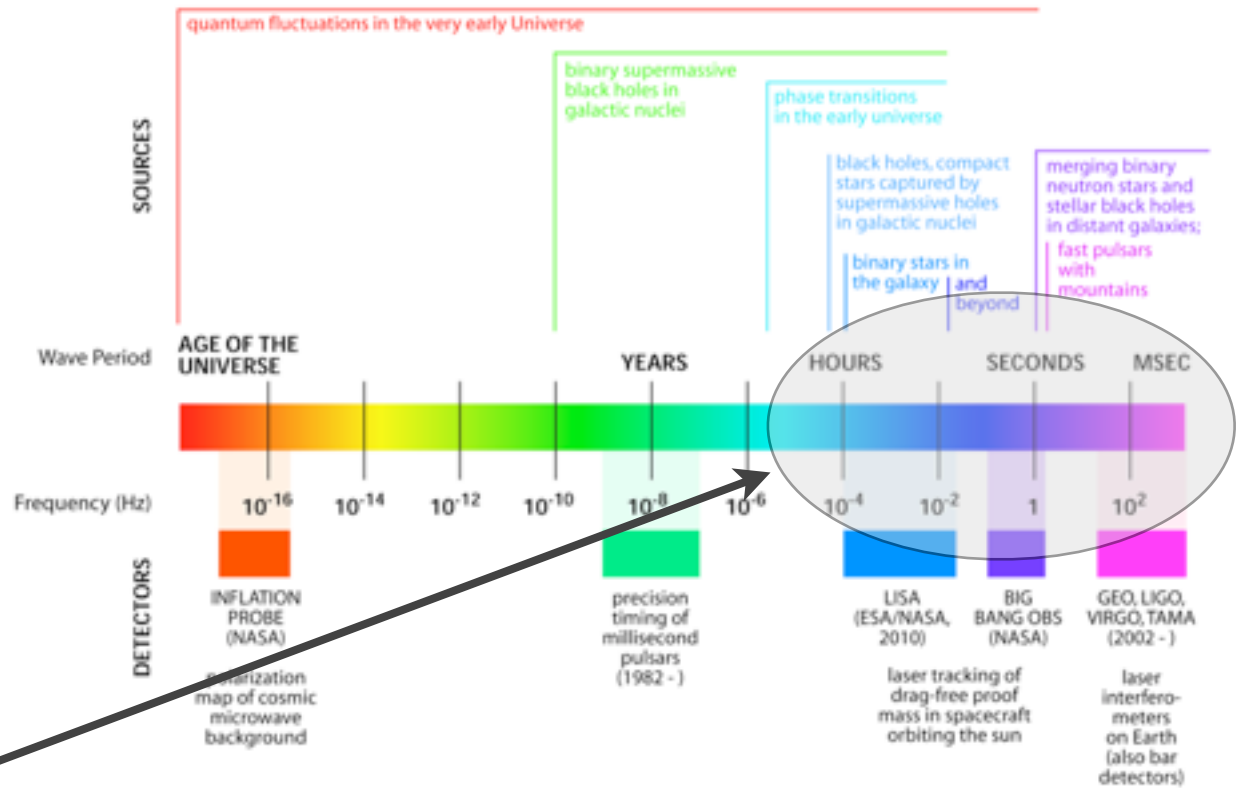
Close to predictions of background from a population of cosmological black hole binaries.

# Programs to measure GWs

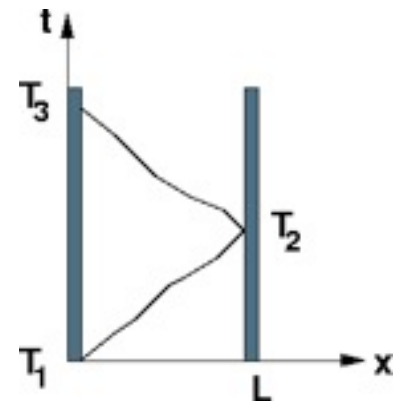
How you measure waves depends on where in spectrum you are probing.



## THE GRAVITATIONAL WAVE SPECTRUM



Hours to msec periods: Direct implementation of Bondi's freely falling mirrors using laser interferometry.



# Ground-based detectors

Three large-scale facilities now operating: Hanford, WA & Livingston, LA (LIGO); and Pisa, Italy (Virgo).



Arms of length 3 km (Virgo) or 4 km (LIGO). Sensitive in band  $\sim 10 \text{ Hz} < f < (\text{a few}) \text{ kHz}$ .

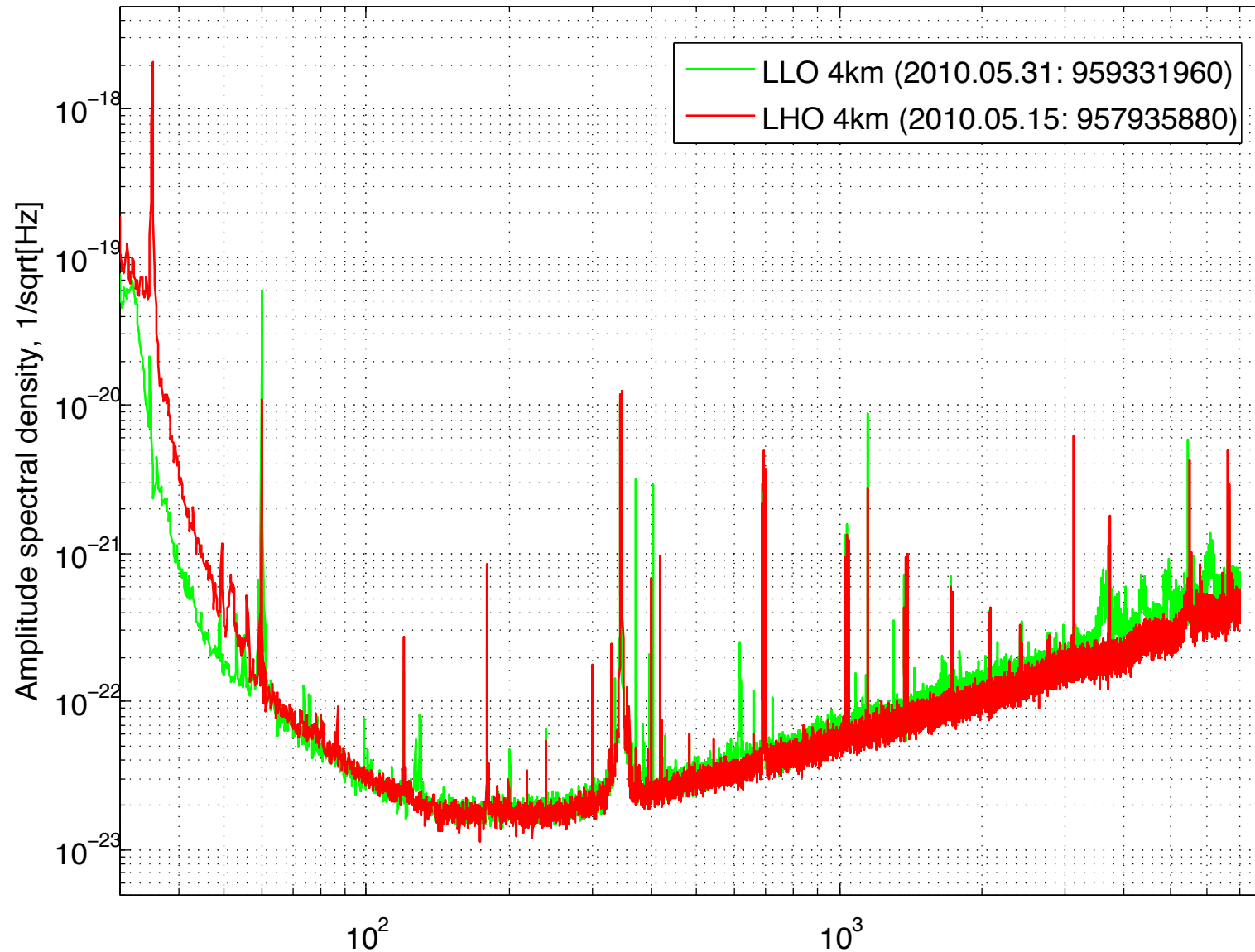


Recently completed initial runs ... undergoing upgrades to “advanced” sensitivity, to begin operations in 2015.



# Initial detectors

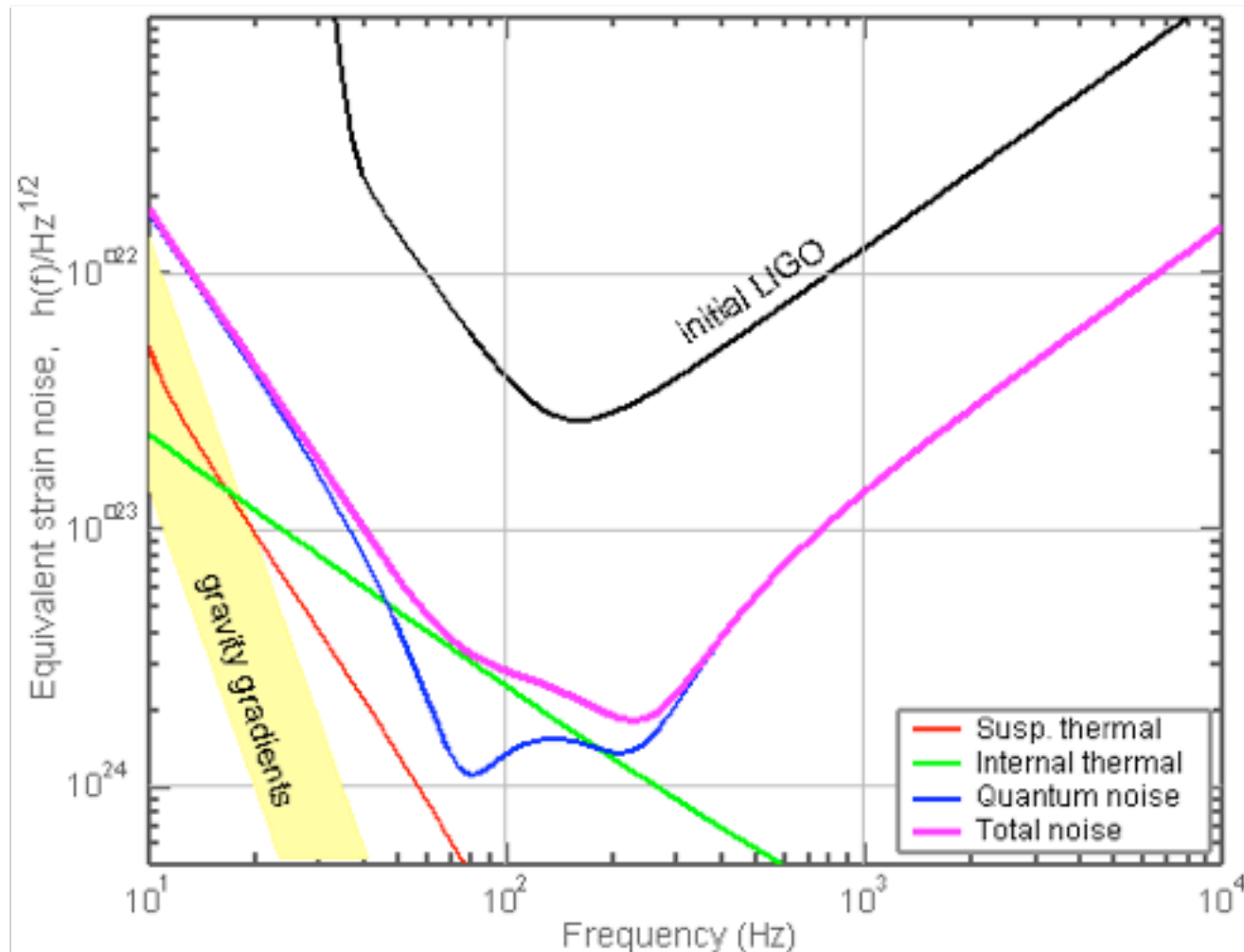
Strain Sensivities From  $h(t)$  For The LIGO S6 Interferometers



Sensitive to binary inspiral to ~20 Mpc.

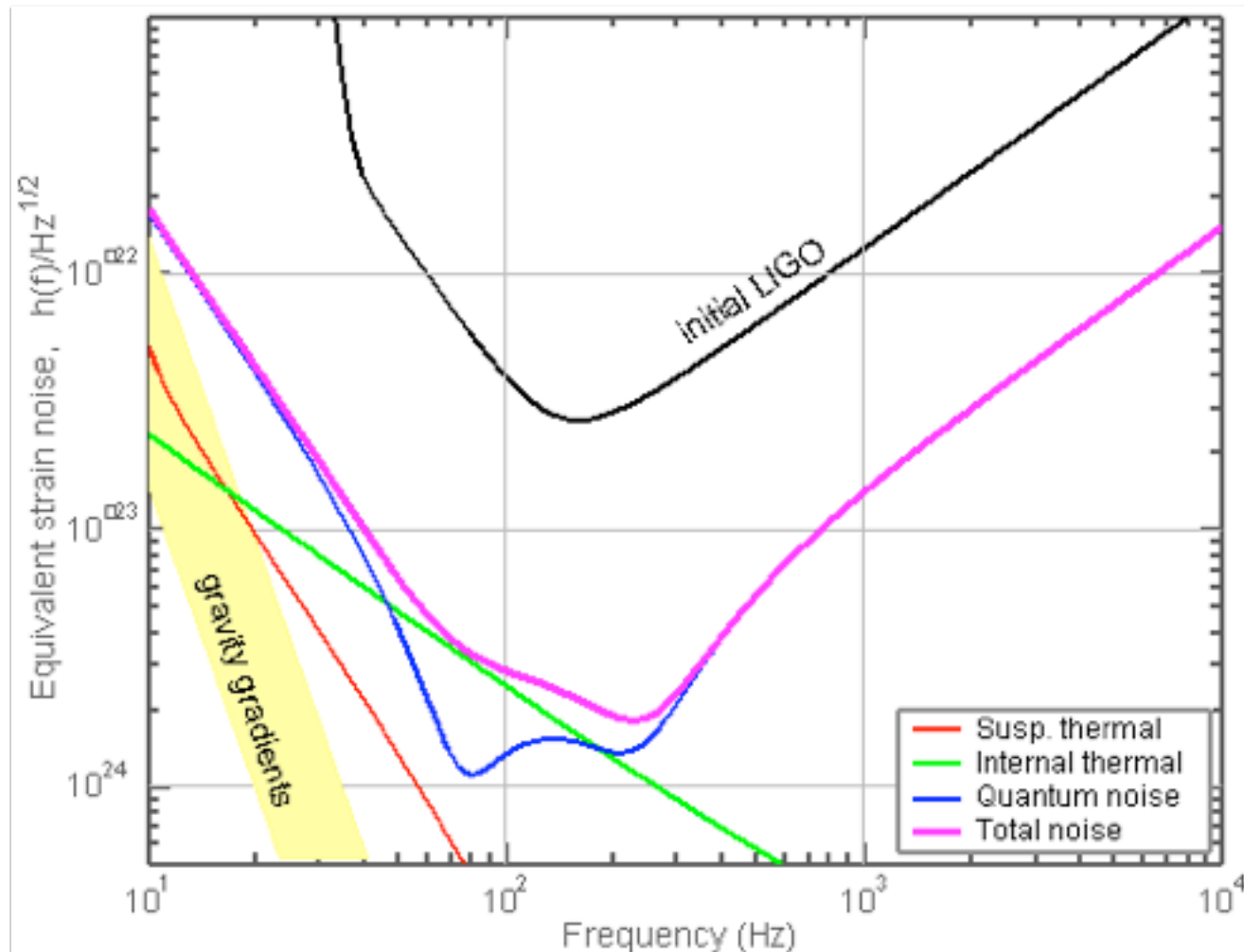


# Advanced detectors (2015)



By increasing laser power and mirror masses, can reach a detector with sensitivity essentially limited by the uncertainty principle.

# Advanced detectors (2015)

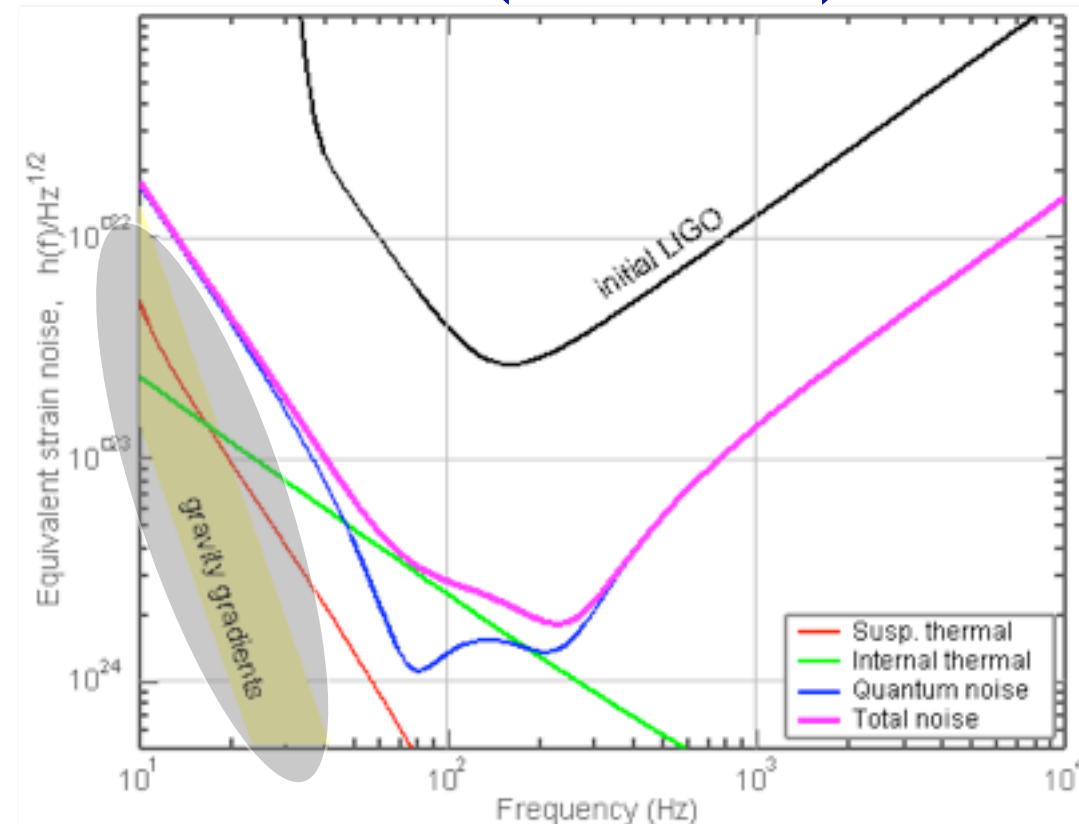


Reach to binary inspiral: A few hundred Mpc.  
***At this sensitivity, detections are expected.***



# Advanced detectors (2015)

Lowest frequency sensitivity limited by gravitational couplings to mass fluctuations in the local environment: “Newtonian noise.”



Part of the cure: **Go underground!**

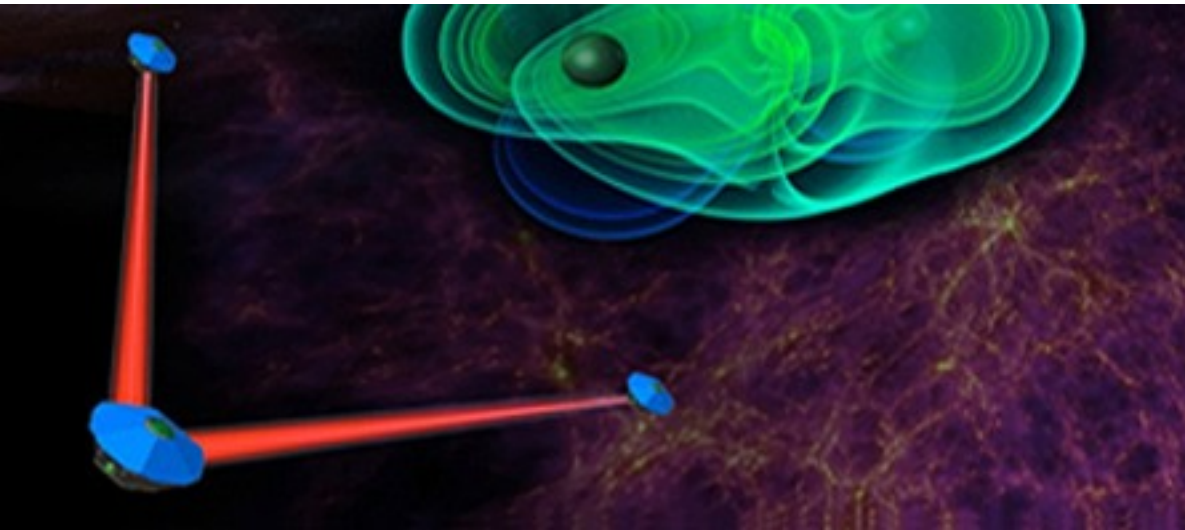
Major sources of this noise are surface seismic modes, which sharply attenuate with depth.

Detailed discussion: Harms et al, arXiv:1308.2074

# Worldwide network



# eLISA

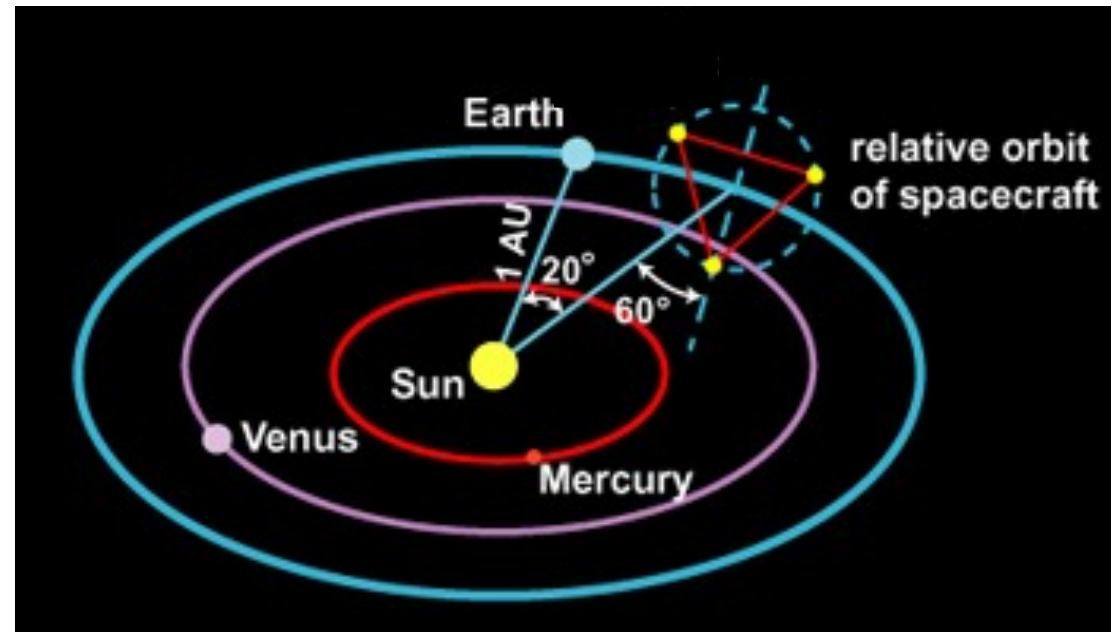


10<sup>6</sup> kilometer space-based interferometer. ESA mission (?) for next decade, evolved from LISA concept.

Go to space to escape low-frequency noise: sensitive in band

$$\sim 10^{-4} \text{ Hz} < f < 0.1 \text{ Hz}$$

Largely targets processes involving massive black holes.



# Astrophysics and Cosmology

# I: Relics from the early universe

Early universe “seeded” with spectrum of GWs ...  
essentially zero-point fluctuations of spacetime.

Fluctuations evolve according to wave equation

$$\frac{d^2 \phi}{d\eta^2} + \frac{2}{a} \frac{da}{d\eta} \frac{d\phi}{d\eta} + k^2 \phi = 0$$

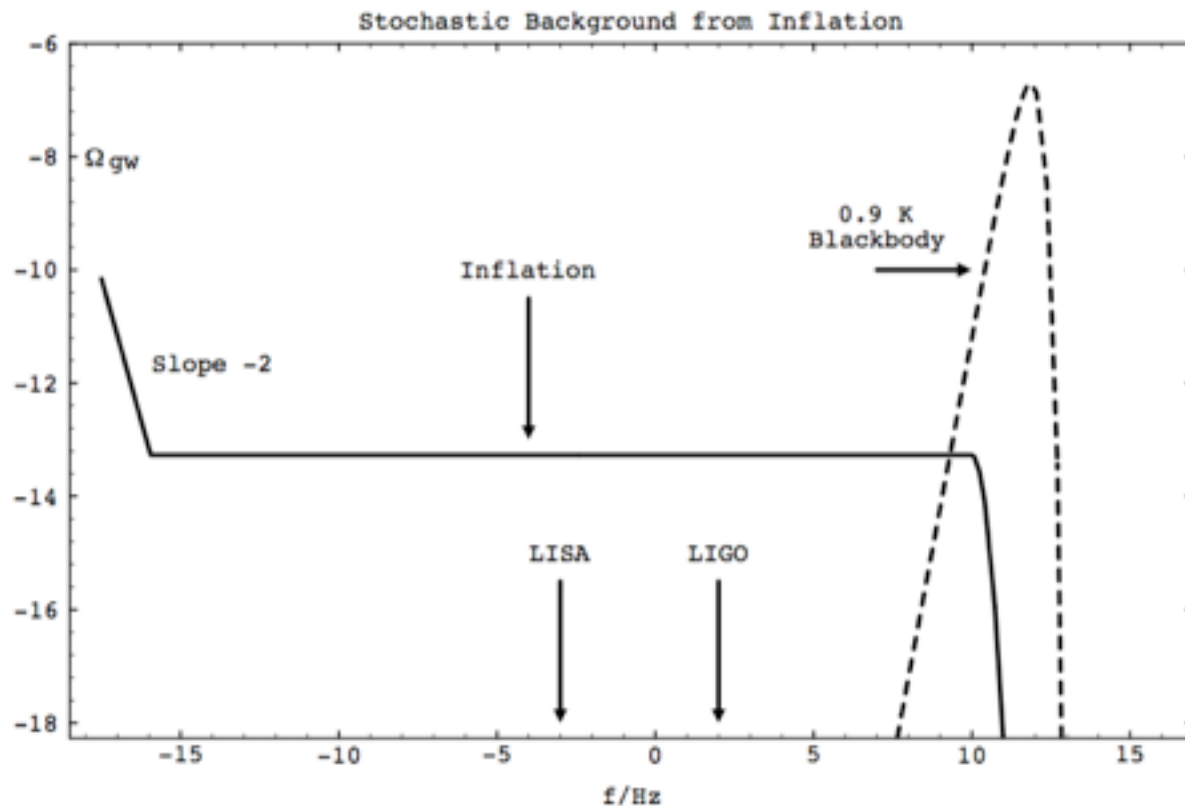
where  $\phi$  parameterizes amplitude,  $a$  is universe's scale factor,  $k$  is wavenumber  $2\pi/\lambda$ , and  $\eta$  is a time variable.

Evolution quite interesting in inflationary universe:  
Mode wavelength inflates while Hubble scale  $a/(da/dt)$   
is constant. Mode amplitude is parametrically  
amplified until  $\lambda$  exceeds Hubble scale, then freezes.



# I: Relics from the early universe

Start with a spectrum of zero-point fluctuations,  
end with a spectrum whose features encode  
properties of inflationary potential!

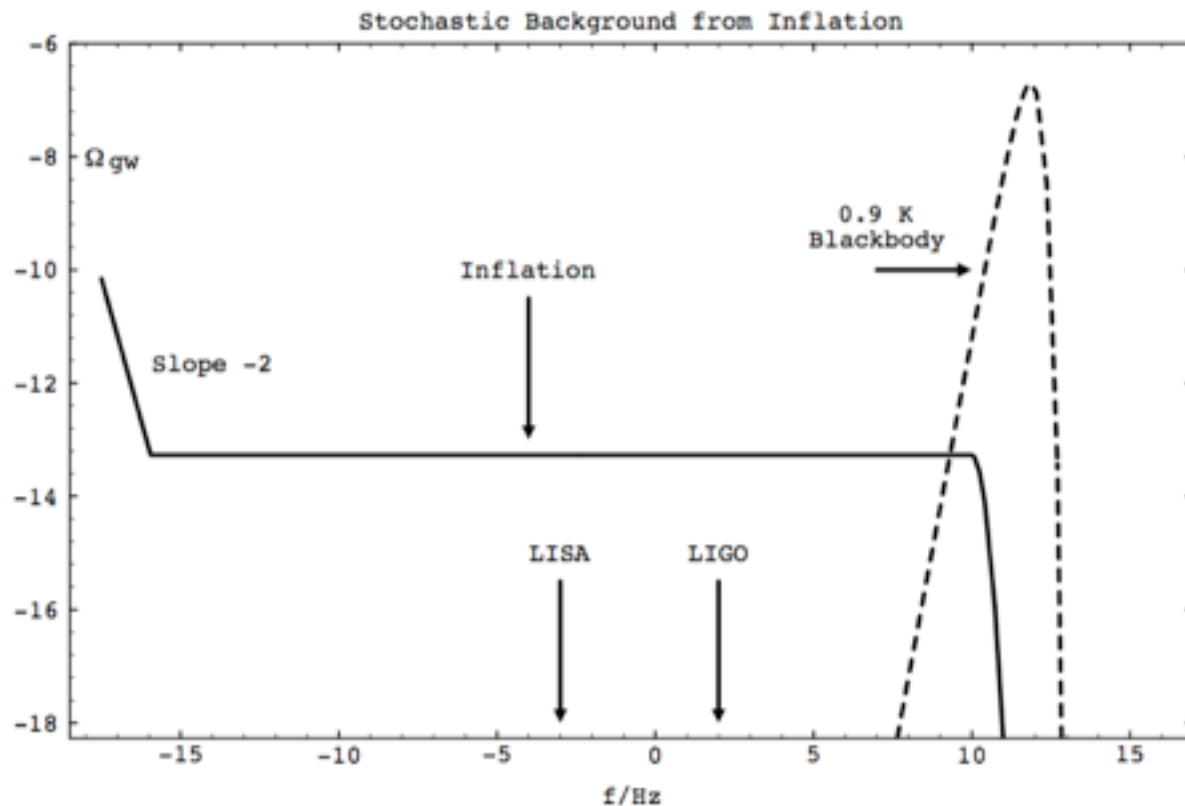


Typical spectrum of  
inflationary waves:  
Rises as  $f^{-2}$  at low freq  
(waves that re-enter  
Hubble volume in  
matter dominated era),  
and is flat elsewhere.

From B. Allen, gr-qc/9604033 (Proceedings of Les Houche School:  
Astrophysical sources of Gravitational Radiation)

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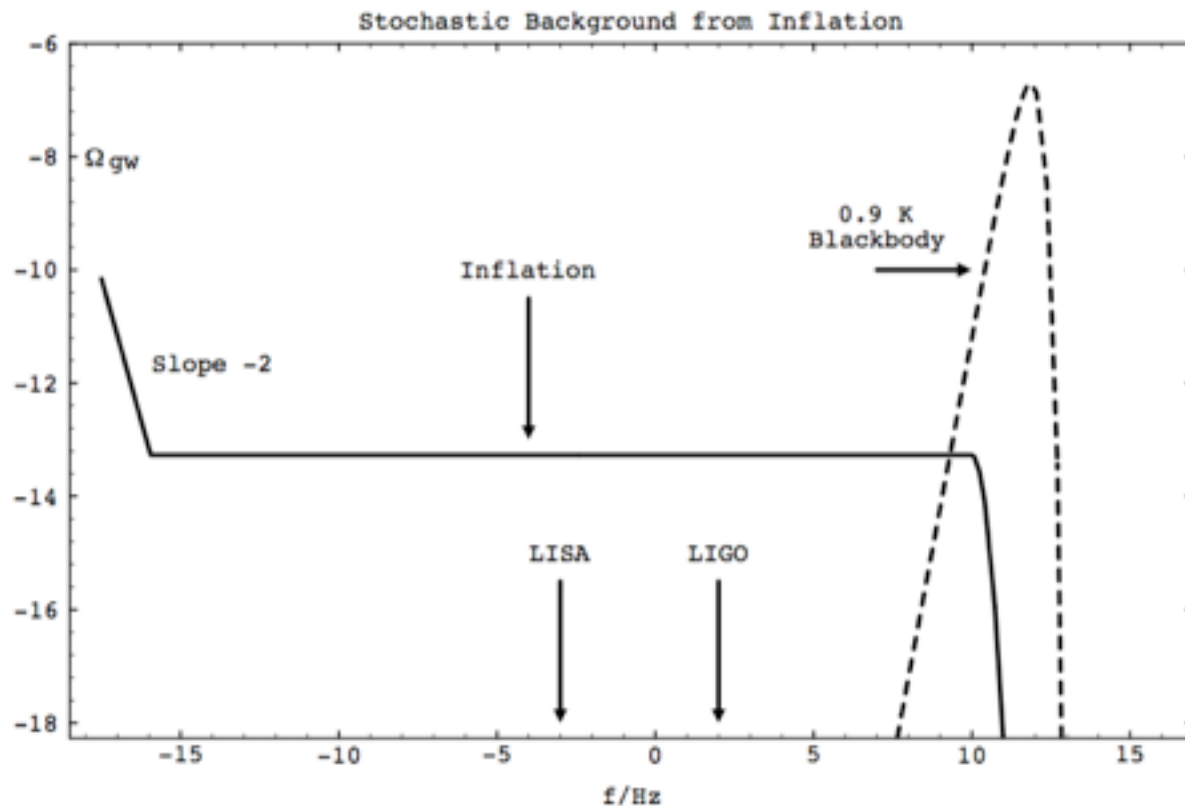
*Level of the spectrum  
directly encodes the  
inflationary potential!*

Measurement of these  
waves called “smoking  
gun” of inflation,  
especially if it can be  
done at multiple  $f$ .



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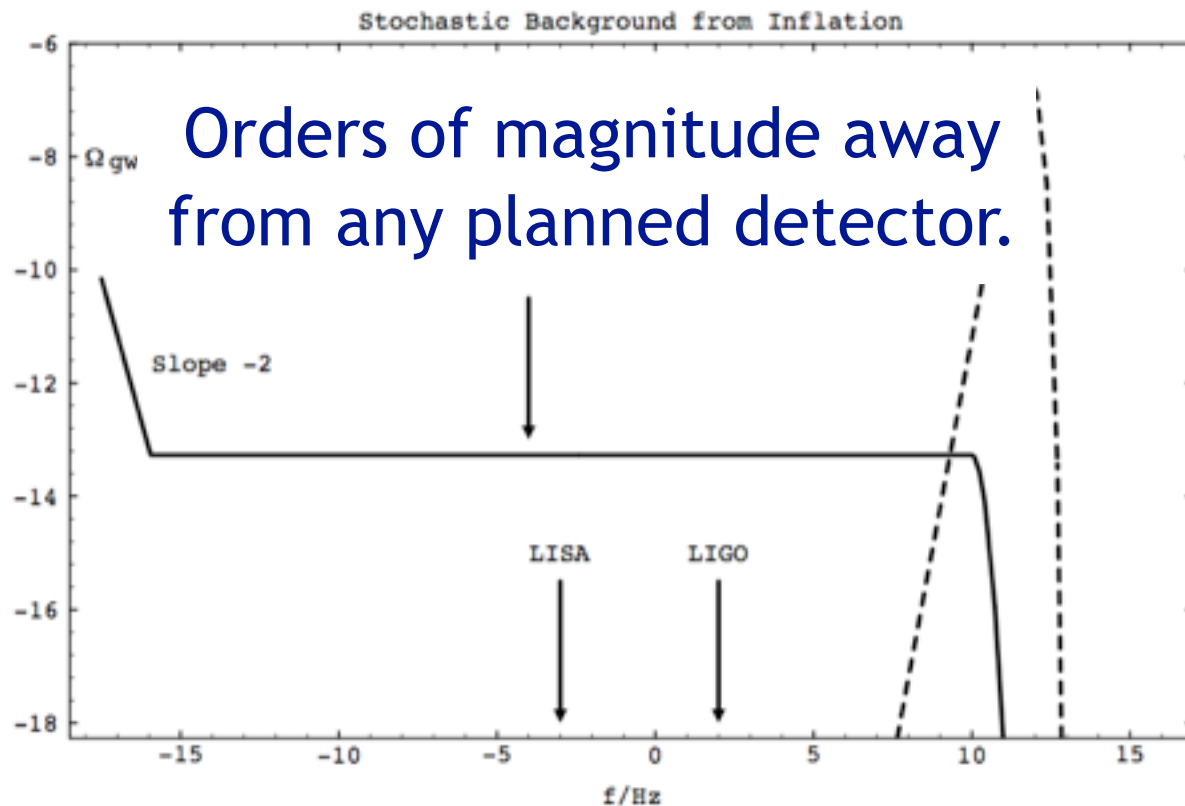
*Level of the spectrum  
directly encodes the  
inflationary potential!*

**Extremely challenging.**

At lowest frequencies,  
requires detangling  
lensed  $E$  modes from  
“primordial”  $B$  modes

# I: Relics from the early universe

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*Level of the spectrum  
directly encodes the  
inflationary potential!*

**Extremely challenging.**

Higher  $f$ : must measure  
weak stochastic GWs ...  
typically masked by  
more prosaic sources.

# II: Precision distances

Distances in astronomy often determined using *standard candles*: Sources with known (empirically calibrated) luminosity. Compare measured brightness with intrinsic luminosity, infer distance.

Perfect candle: Simple radiator (e.g., dipole) in which the radiative moment evolves in a slow, predictable way.

$$\frac{dE}{dA dt} = \frac{p(t)^2 \omega^4 \sin^2 \theta}{8c^2 r^2}$$

Read off  $\omega$  from radiation. If we could read off time-changing dipole moment, easy to get distance.

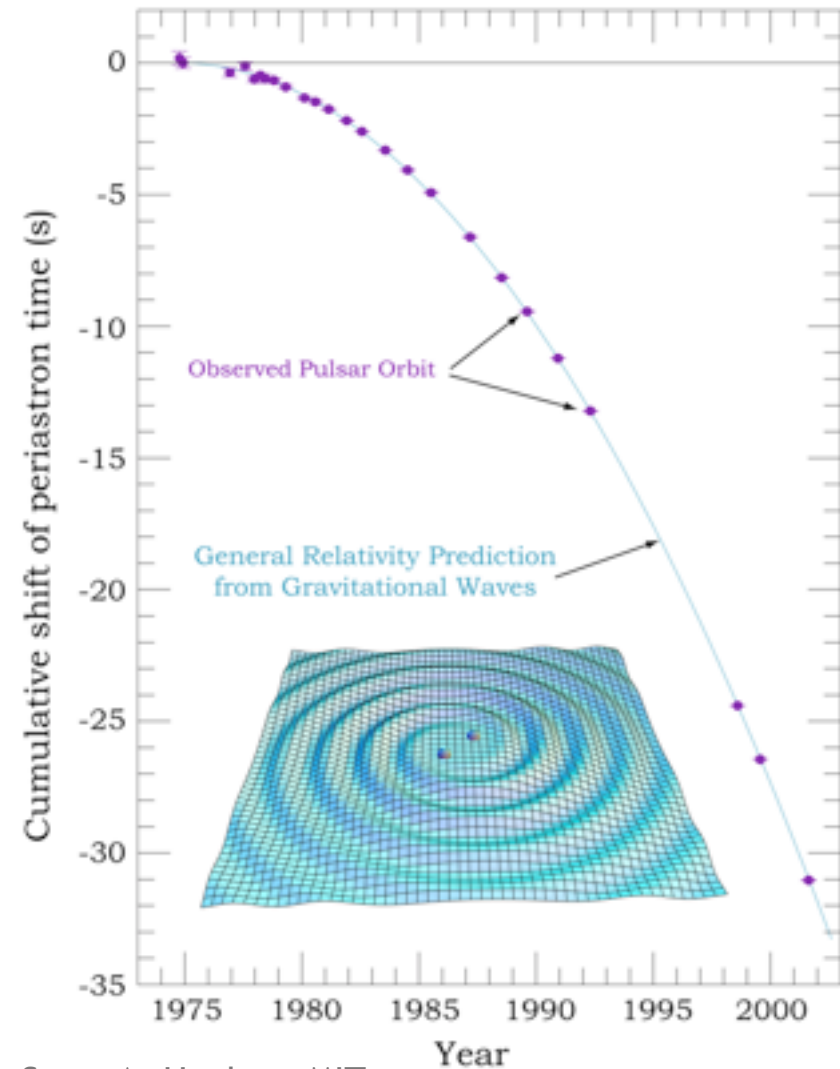
# II: Precision distances

Binary coalescence *is* this “perfect” standard candle!

Rate at which frequency changes determined by binary’s mass quadrupole ... observing “chirp” measures this moment.

Measuring both GW polarizations determines angular factors.

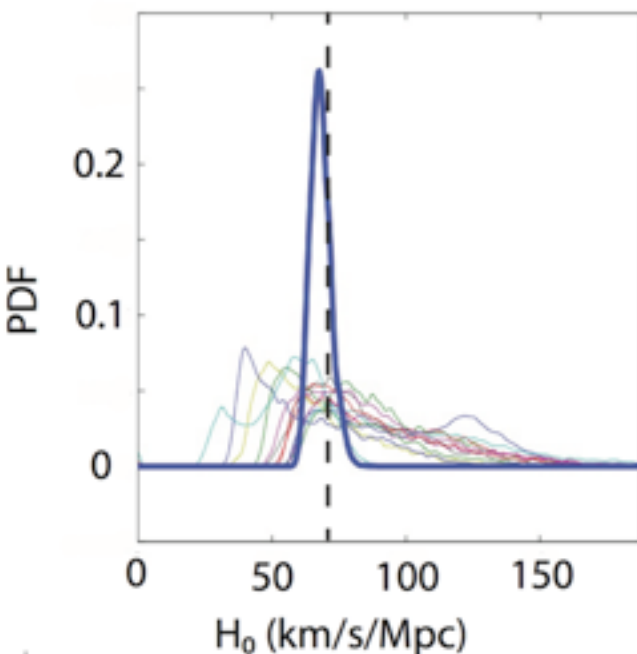
***Distance to binary is then fixed by measured amplitude of the wave.***



# II: Precision distances

Binary coalescence *is* this “perfect” standard candle!

GW distance plus “electromagnetic” redshift allows us to determine cosmology ... with *very* different systematics from other techniques.



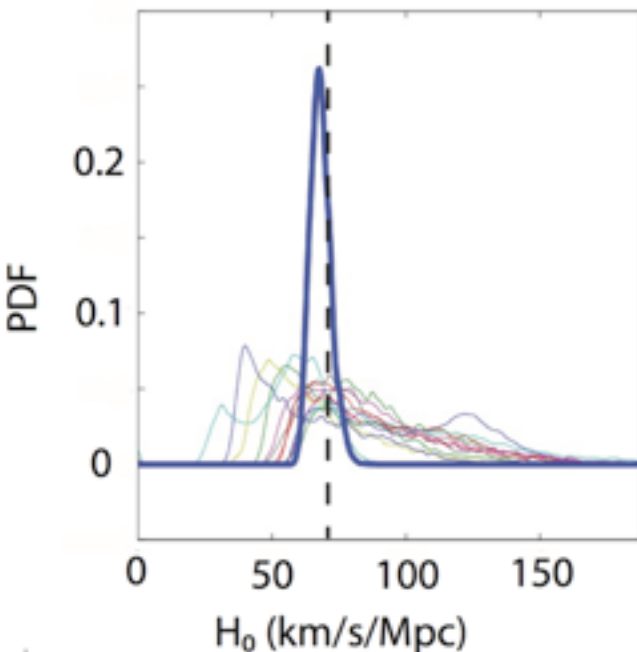
Recent work (Nissanke et al, arXiv: 1307.2638) examines how well GW plus EM counterpart determines Hubble:

About 10 events needed for  $H_0$  to be competitive with other methods ... could help resolve tension between methods.

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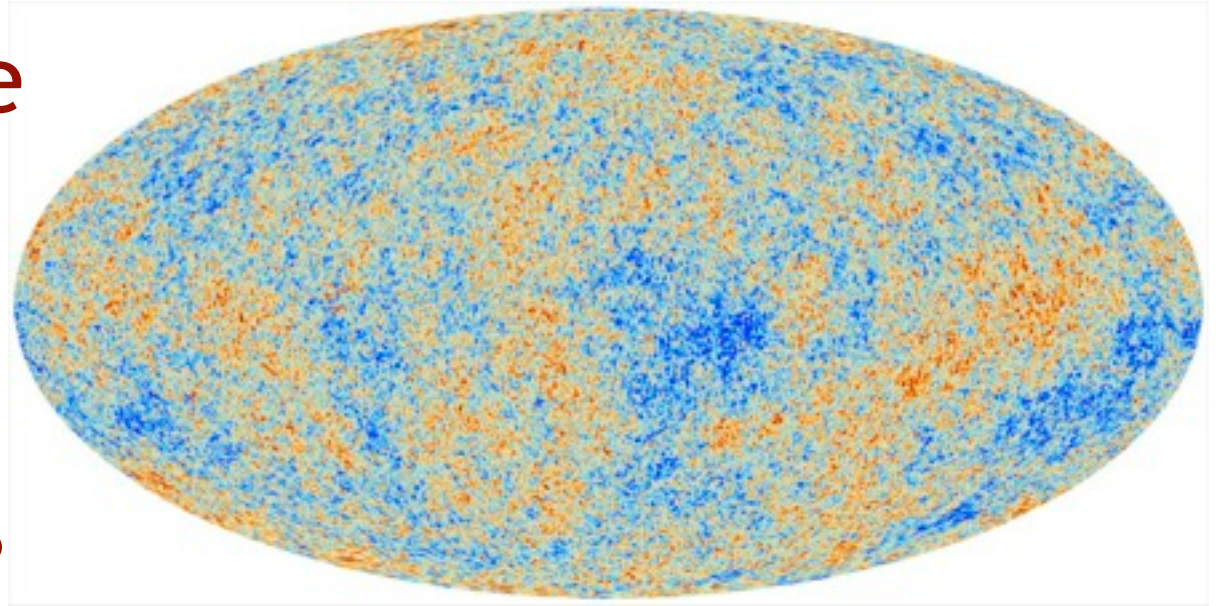


Recent work (Nissanke et al, arXiv: 1307.2638) examines how well GW plus EM counterpart determines Hubble:  
**Need close coordination between GW facilities and (wide spectrum) electromagnetic telescopes.**



# III: The growth of cosmic structure

Cosmic microwave background gives first glimpse of the universe's largest structures

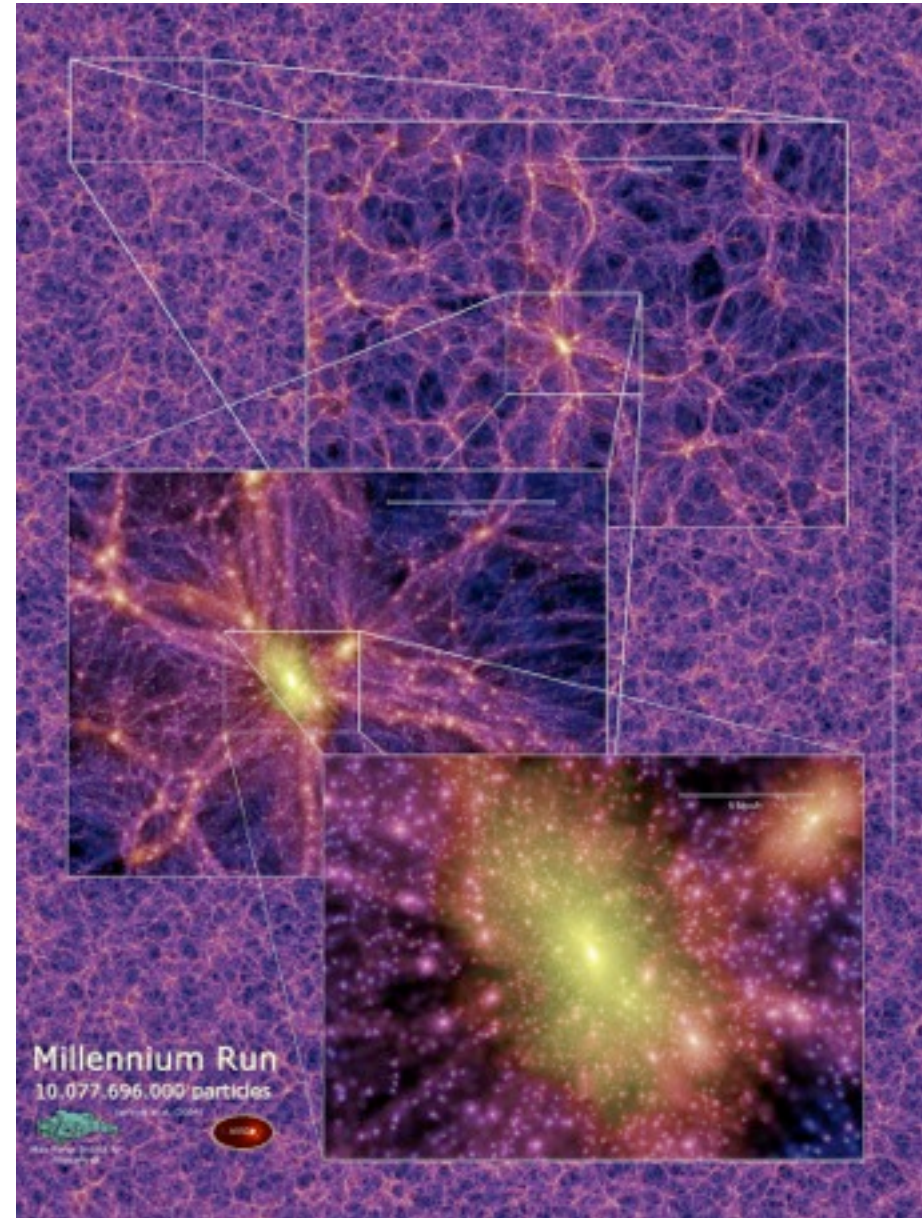


Gravity grows overdensities: A slight overdensity at  $z = 1100$  will become progressively more dense as that region attracts more matter to itself.

# III: The growth of cosmic structure

As overdensities become massive, they attract other overdensities into themselves ... find a hierarchical network of *mergers* building the first galaxies and clusters.

**Galaxies and their host halos merge often, especially at moderate to high redshift.**

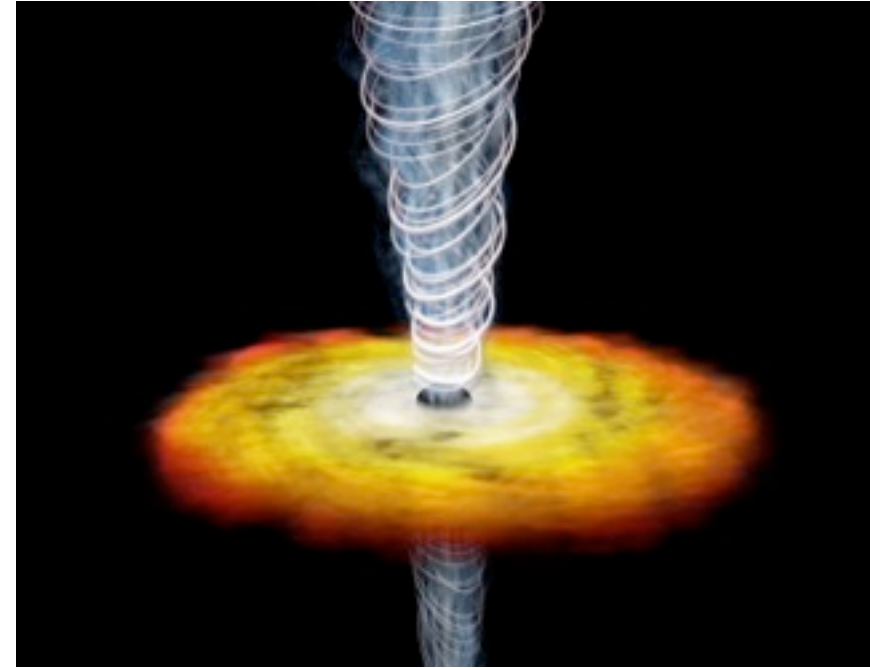


<http://www.mpa-garching.mpg.de/galform/virgo>



# III: The growth of cosmic structure

High redshift quasars show that massive black holes have existed in merging structures from early in universe's history.

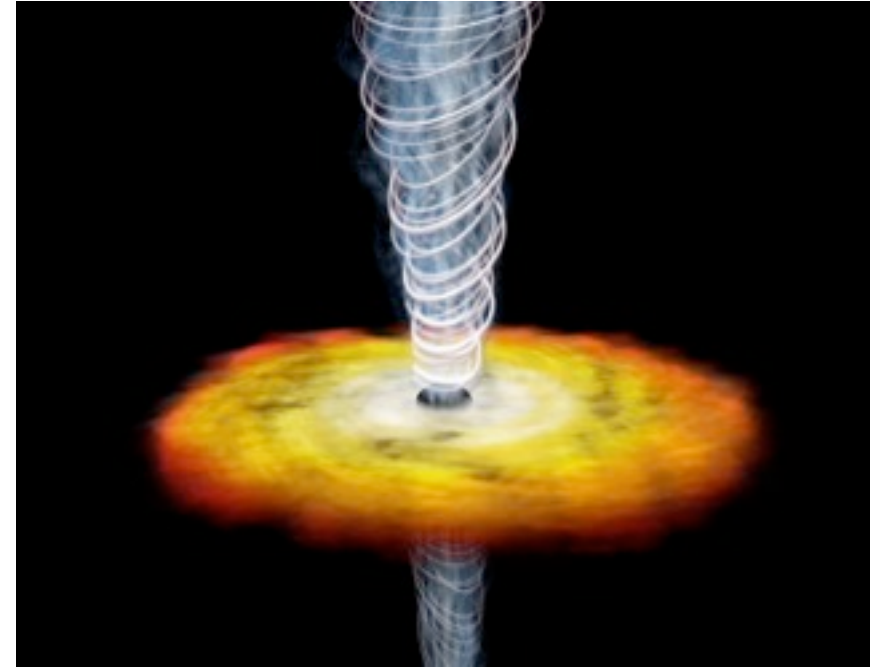


Most extreme example known:  
ULAS J1120+0641 at  $z = 7.085$  ... luminosity  
and line widths imply  $M_{\text{BH}} \sim 5 \times 10^9 M_{\odot}$ .

Early structures host BHs; structures  
merge; BHs come together, forming  
binaries ... strong GW radiators.

# III: The growth of cosmic structure

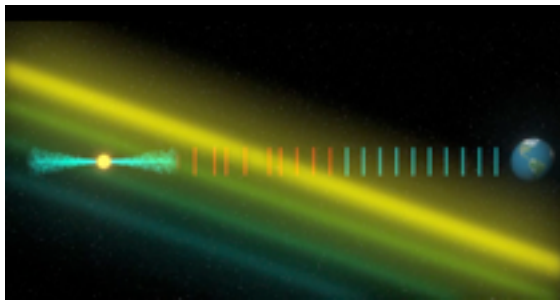
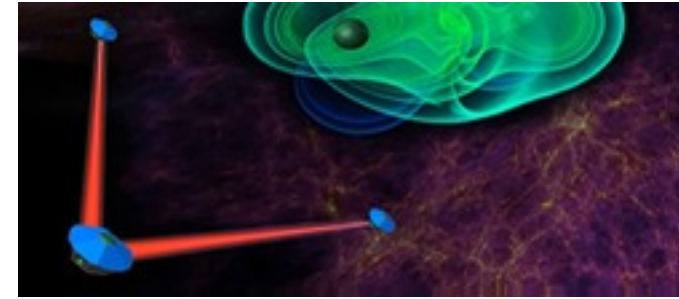
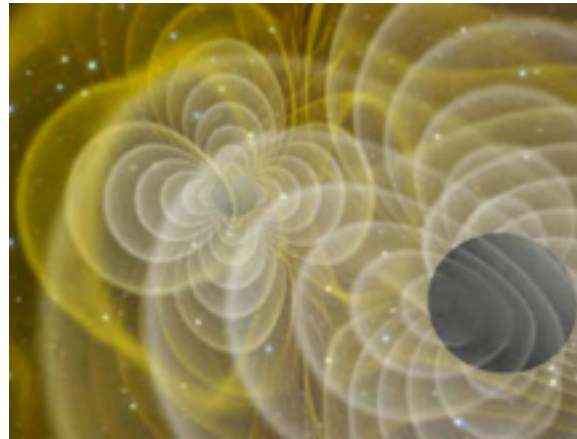
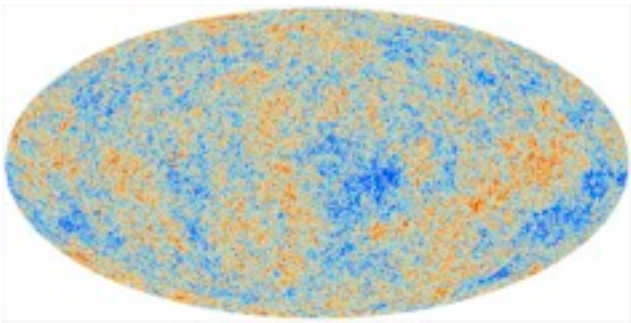
High redshift quasars show that massive black holes have existed in merging structures from early in universe's history.



Most extreme example known:  
ULAS J1120+0641 at  $z = 7.085$  ... luminosity  
and line widths imply  $M_{\text{BH}} \sim 5 \times 10^9 M_{\odot}$ .

Binaries formed this way targets for space detectors (eLISA) ... measuring their GWs will let us directly track mergers and growth of structure at high redshift.

# Conclusion



Gravitational waves: On cusp of inaugurating new tools for astronomy and astrophysics.

Operations of advanced ground-based detectors begins in 2015 ... expect the fun to begin in earnest in the years to follow.