

GLOBAL ANALYSES OF
OSCILLATION NEUTRINO
EXPERIMENTS

Concha Gonzalez-Garcia

(ICREA U. Barcelona & YITP Stony Brook)

TAUP 2013, September 12th, 2013

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OUTLINE

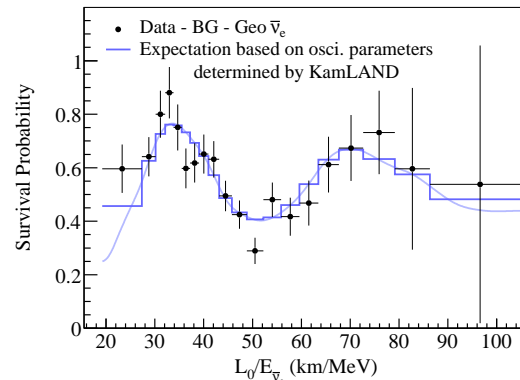
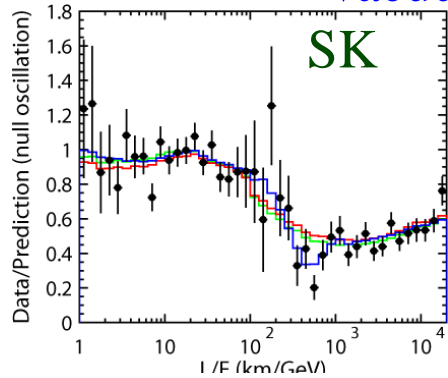
Determination of 3ν Lepton Flavour Parameters

Light Sterile Neutrinos

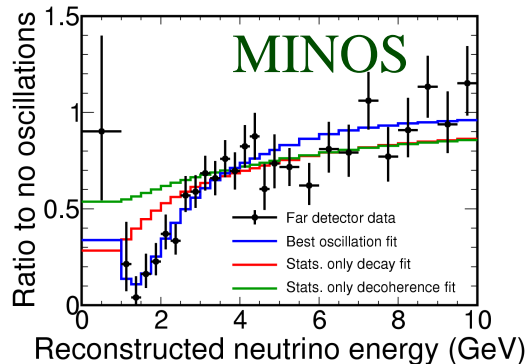
Matter Potential/Non-standard Neutrino Interactions

- By 2013 we have observed with high (or good) precision:
 - * Solar ν_e convert to ν_μ/ν_τ (Cl, Ga, **SK, SNO, Borexino**)
 - * Reactor $\bar{\nu}_e$ disappear at $L \sim 200$ Km (**KamLAND**)
 - * Atmospheric ν_μ & $\bar{\nu}_\mu$ disappear most likely to ν_τ (**SK, MINOS**)
 - * Accelerator ν_μ & $\bar{\nu}_\mu$ disappear at $L \sim 250[700]$ Km (K2K, T2K, [**MINOS**])
 - * Some accel ν_μ appear as ν_e at $L \sim 250[700]$ Km (**T2K (NEW 2013)**, [**MINOS**])
 - * Reactor $\bar{\nu}_e$ disappear at $L \sim 1$ Km (D-Chooz, **Daya-Bay, Reno**) (**NEW 2012**)

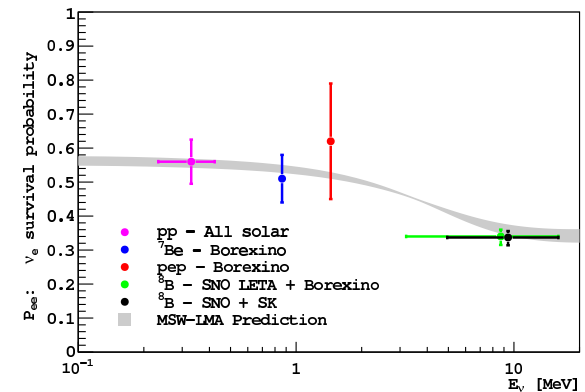
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- We have confirmed:
 - Vacuum oscillation L/E pattern



KamLAND



MSW conversion in Sun



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All this implies that neutrinos are massive

and There is Physics Beyond SM

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All this implies that neutrinos are massive
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- The *important* question:

What is the BSM theory?

- The *difficult* path:

Detailed determination of the new low energy parametrization

The New Minimal Standard Model

- Minimal Extensions to give Mass to the Neutrino:

- * Introduce ν_R AND impose L conservation \Rightarrow Dirac $\nu \neq \nu^c$:

$$\mathcal{L} = \mathcal{L}_{SM} - M_\nu \bar{\nu}_L \nu_R + h.c.$$

- * NOT impose L conservation \Rightarrow Majorana $\nu = \nu^c$

$$\mathcal{L} = \mathcal{L}_{SM} - \frac{1}{2} M_\nu \bar{\nu}_L \nu_L^C + h.c.$$

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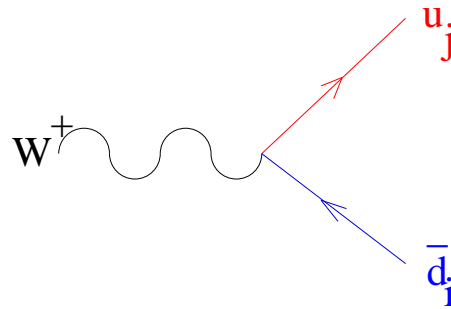
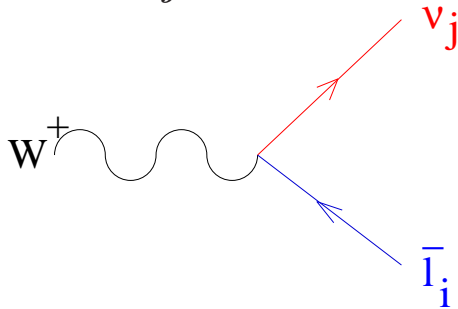
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- The charged current interactions of leptons are not diagonal (same as quarks)

$$\frac{g}{\sqrt{2}} W_\mu^+ \sum_{ij} (U_{LEP}^{ij} \bar{\ell}^i \gamma^\mu L \nu^j + U_{CKM}^{ij} \bar{U}^i \gamma^\mu L D^j) + h.c.$$



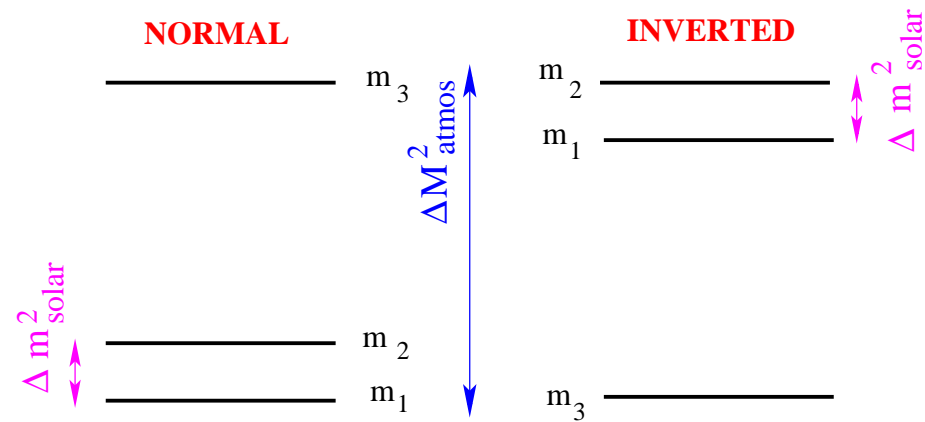
3ν Flavour Parameters

Concha Gonzalez-Garcia

- For 3 ν's : 3 Mixing angles + 1 Dirac Phase + 2 Majorana Phases

$$U_{\text{LEP}} = \begin{pmatrix} 1 & 0 & 0 \\ 0 & c_{23} & s_{23} \\ 0 & -s_{23} & c_{23} \end{pmatrix} \begin{pmatrix} c_{13} & 0 & s_{13}e^{i\delta_{\text{CP}}} \\ 0 & 1 & 0 \\ -s_{13}e^{-i\delta_{\text{CP}}} & 0 & c_{13} \end{pmatrix} \begin{pmatrix} c_{21} & s_{12} & 0 \\ -s_{12} & c_{12} & 0 \\ 0 & 0 & 1 \end{pmatrix} \begin{pmatrix} e^{i\eta_1} & 0 & 0 \\ 0 & e^{i\eta_2} & 0 \\ 0 & 0 & 1 \end{pmatrix}$$

- Two Possible Orderings



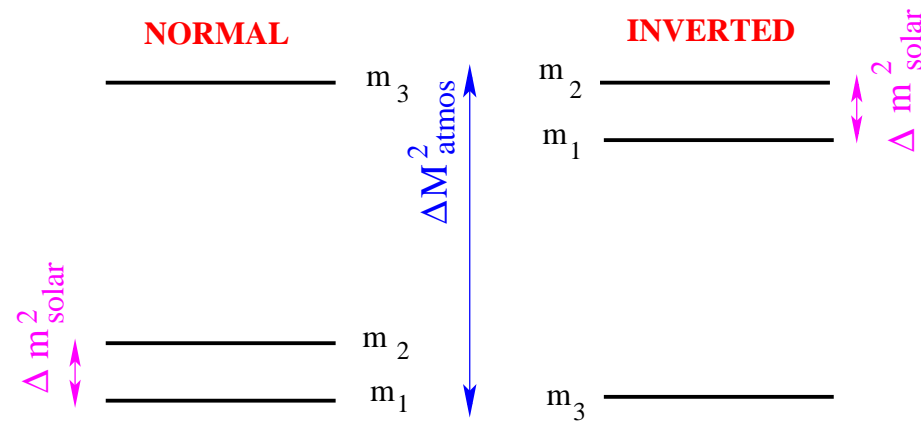
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- Two Possible Orderings



Experiment

Dominant Dependence

Important Dependence

Solar Experiments

→ θ_{12}

Δm_{21}^2 , θ_{13}

Reactor LBL (KamLAND)

→ Δm_{21}^2

θ_{12} , θ_{13}

Reactor MBL (Daya-Bay, Reno, D-Chooz)

→ θ_{13}

Δm_{atm}^2

Atmospheric Experiments

→ θ_{23}

Δm_{atm}^2 , θ_{13} , δ_{CP}

Accelerator LBL ν_{μ} Disapp (Minos)

→ Δm_{atm}^2

θ_{23}

Accelerator LBL ν_e App (Minos, T2K)

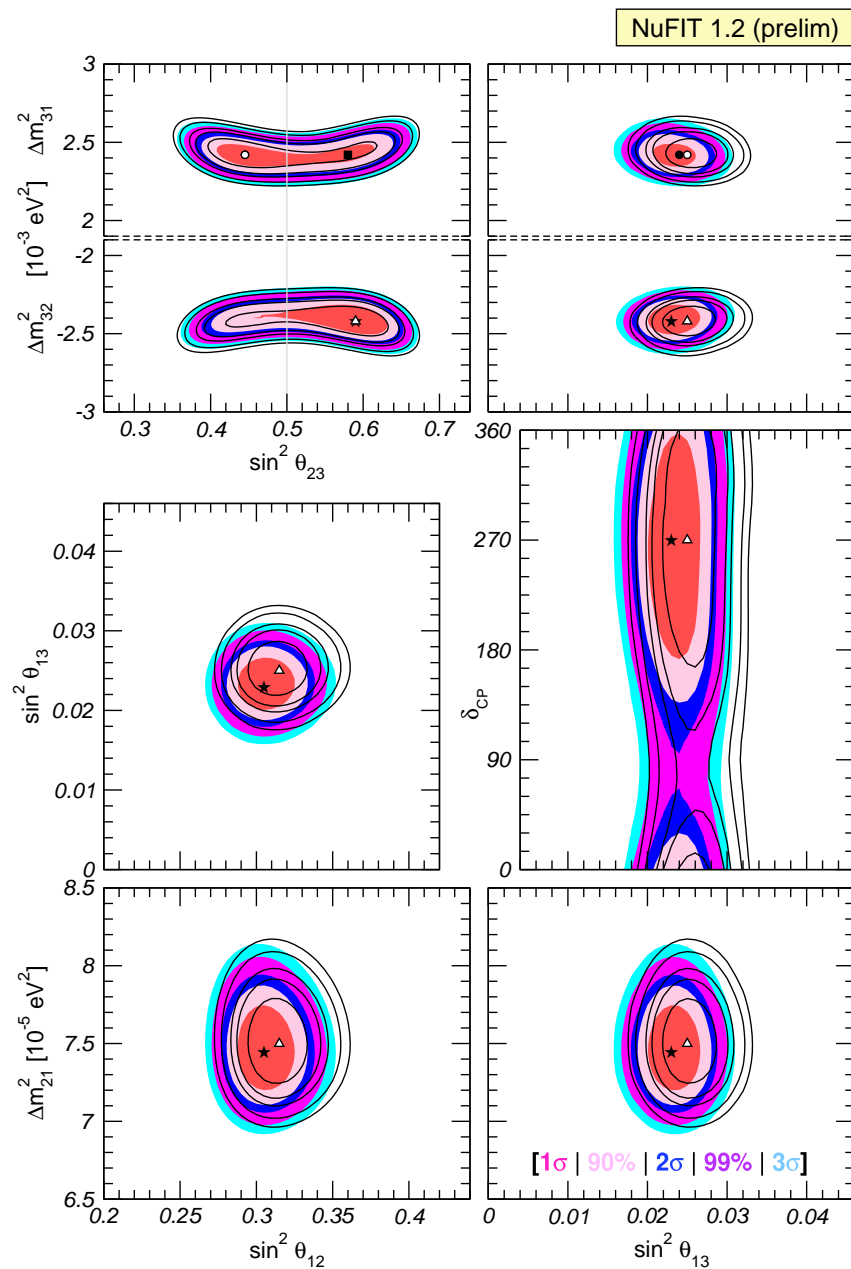
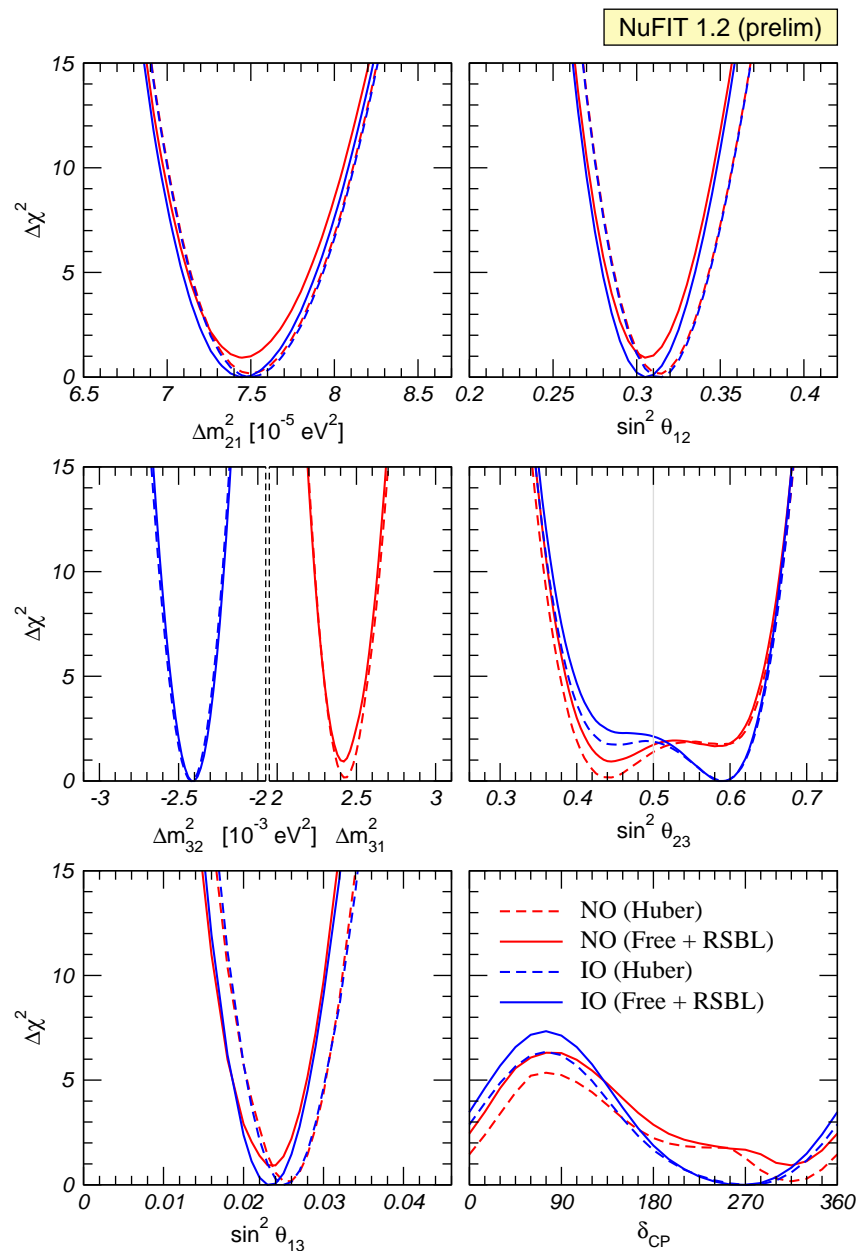
→ θ_{13}

δ_{CP} , θ_{23}

3 ν Flavour Parameters: Present Status

Maltoni, Schwetz, Salvado, MCGG

Global 6-parameter fit <http://www.nu-fit.org>
 Maltoni, Schwetz, Salvado, MCGG

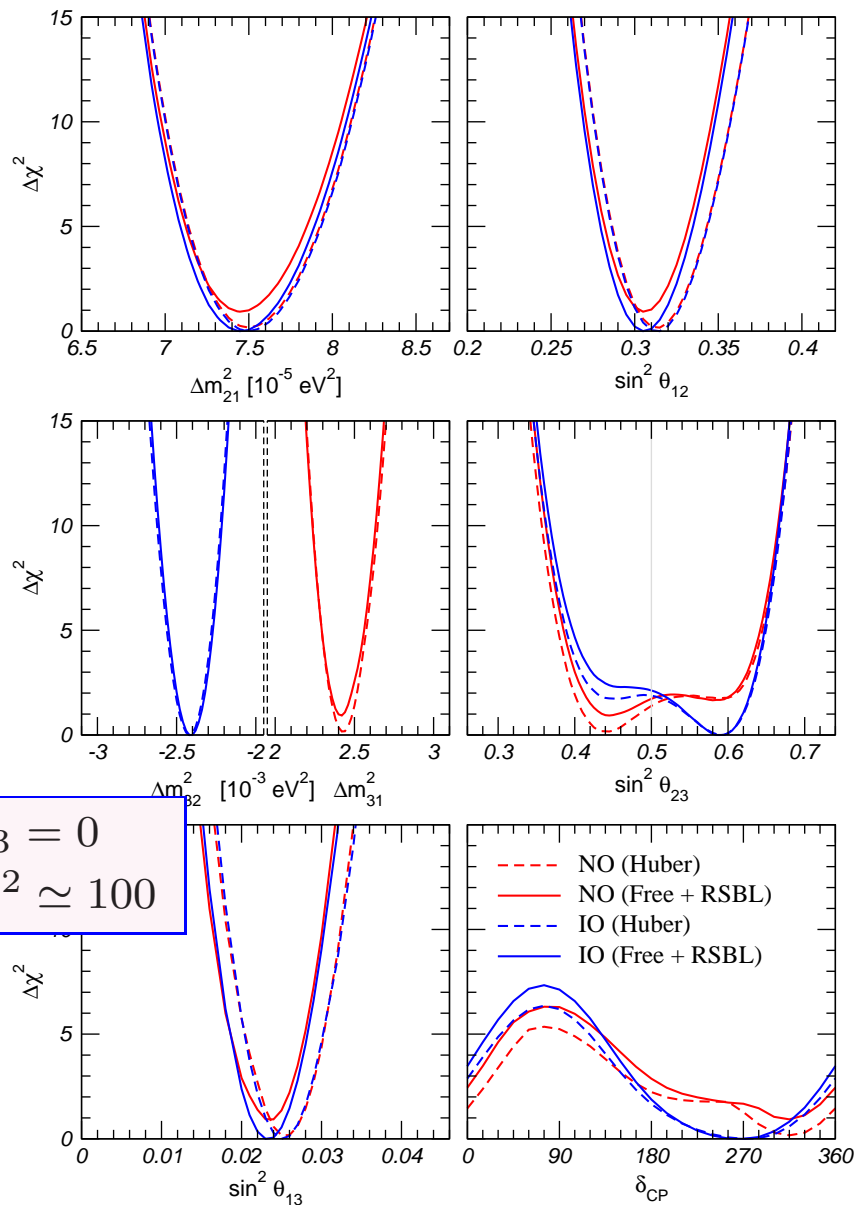


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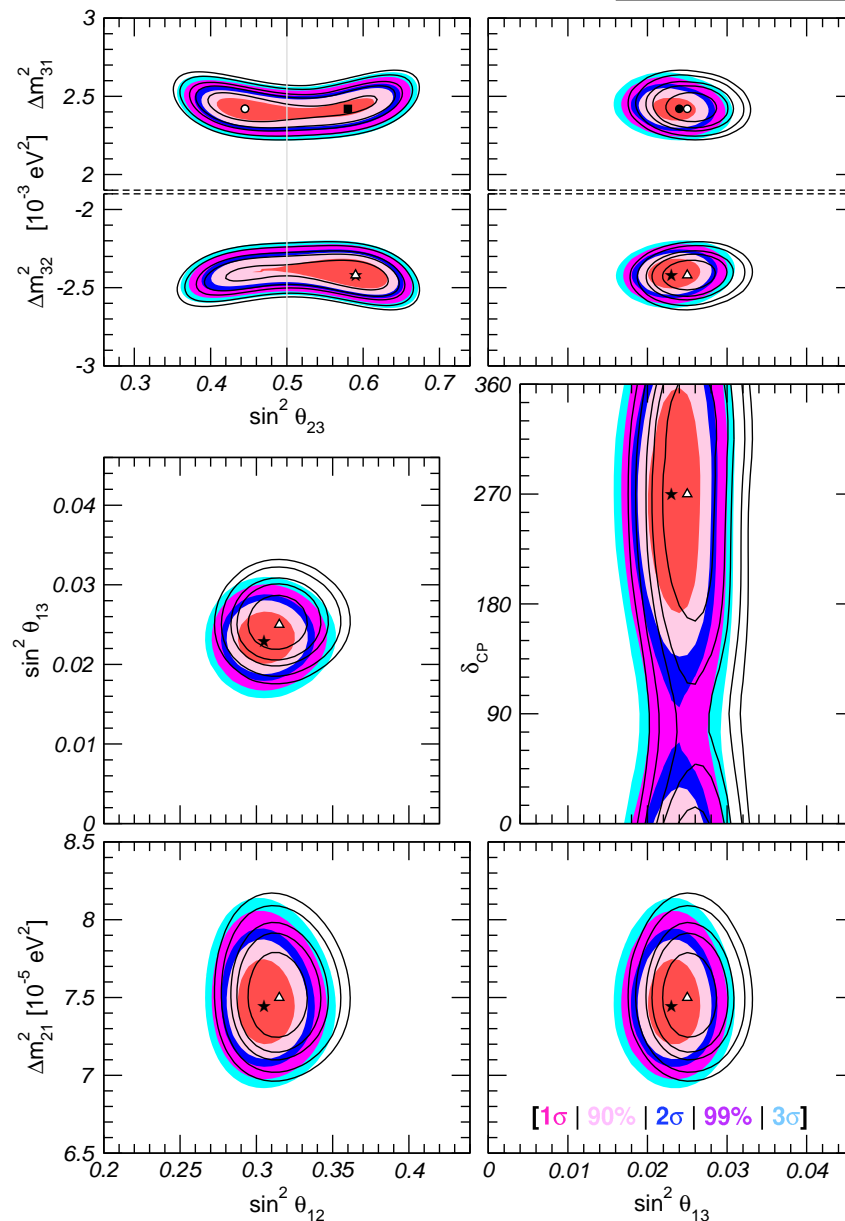
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NuFIT 1.2 (prelim)



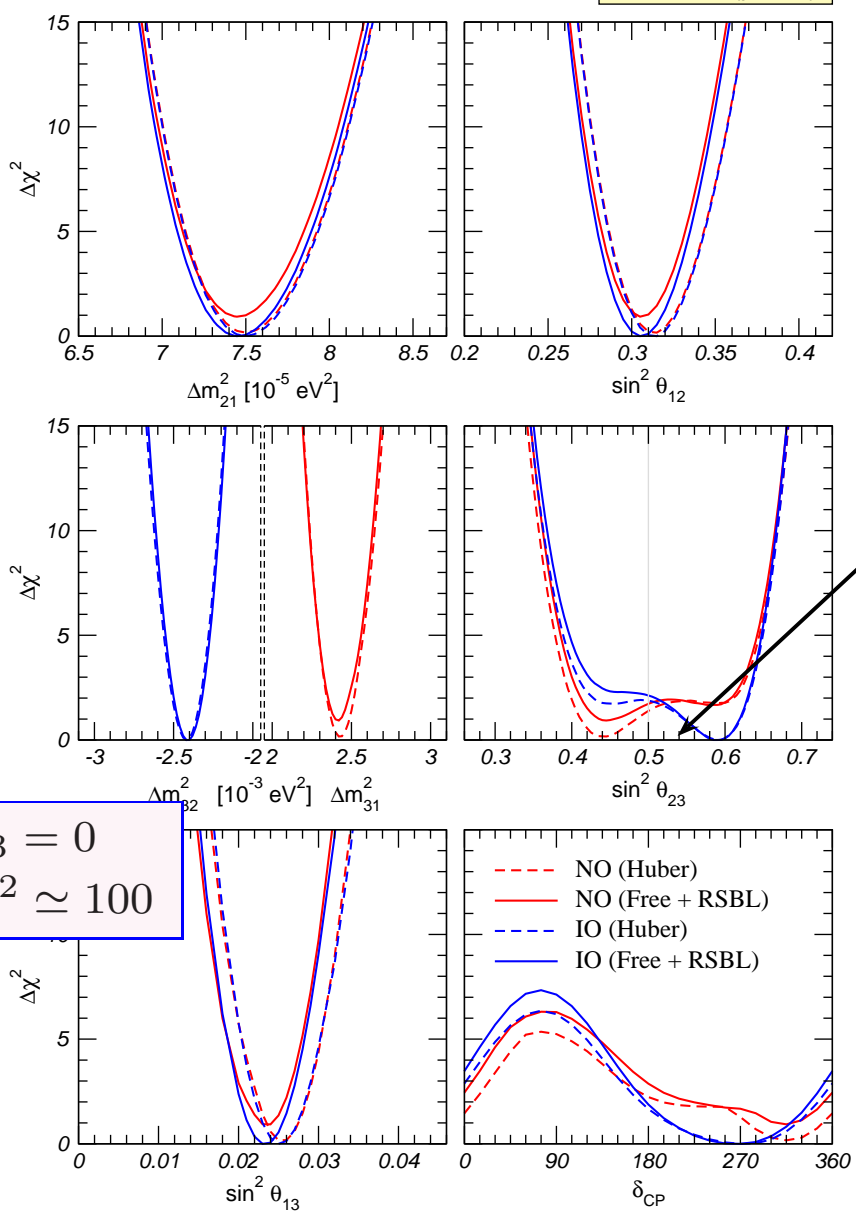
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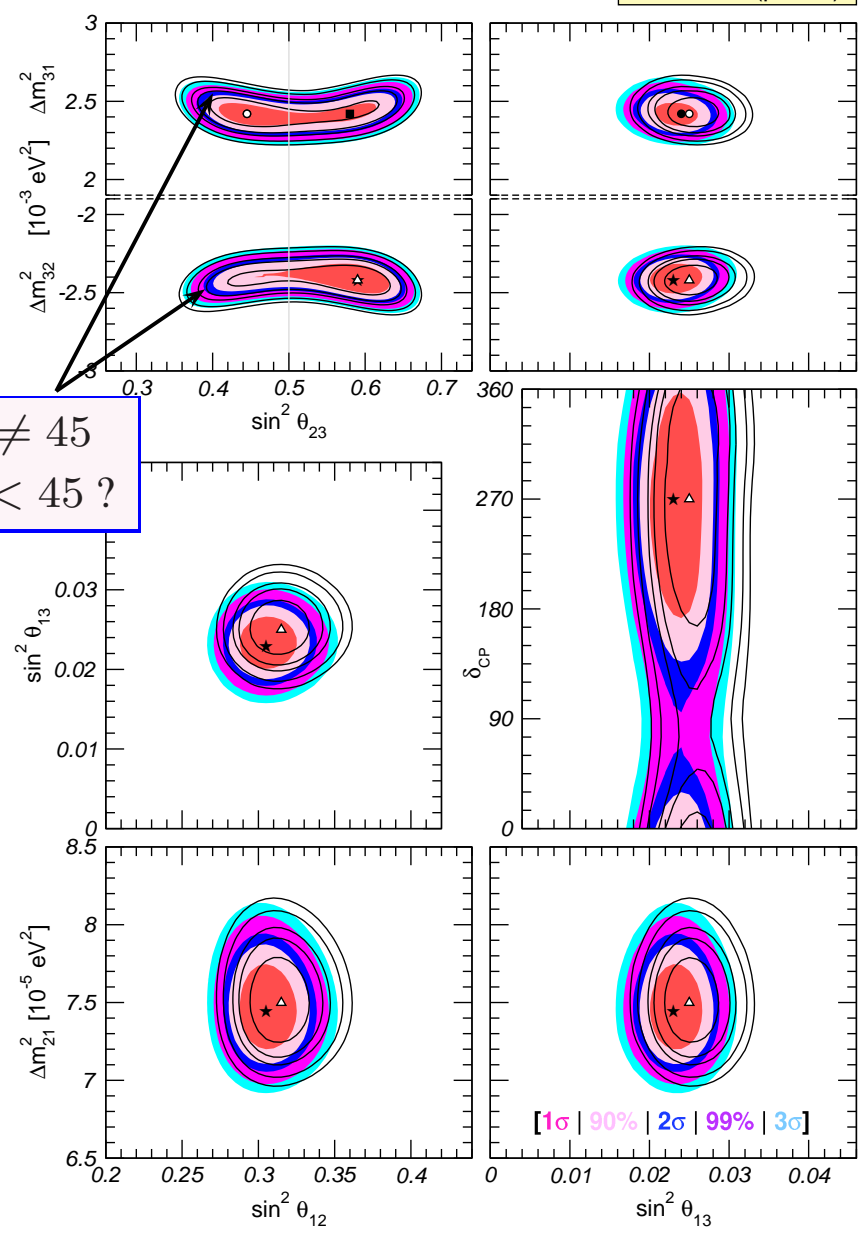
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$\theta_{23} \neq 45$
 $\theta_{23} < 45 ?$

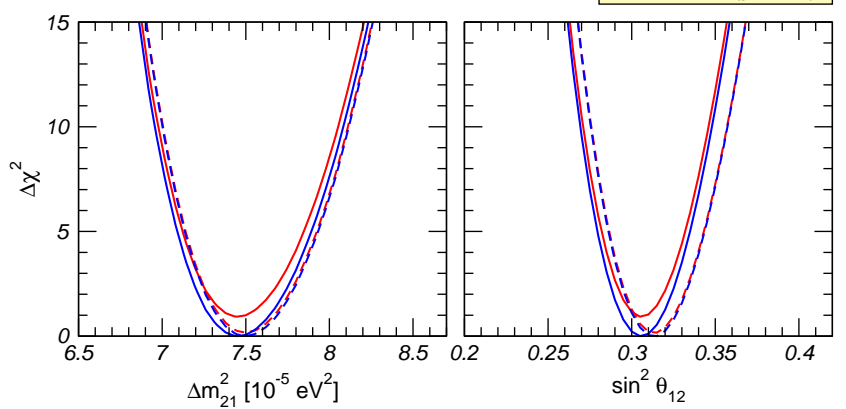
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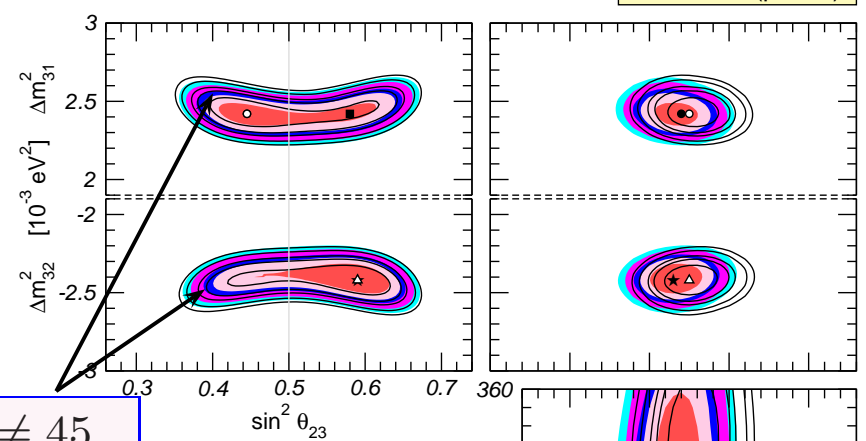
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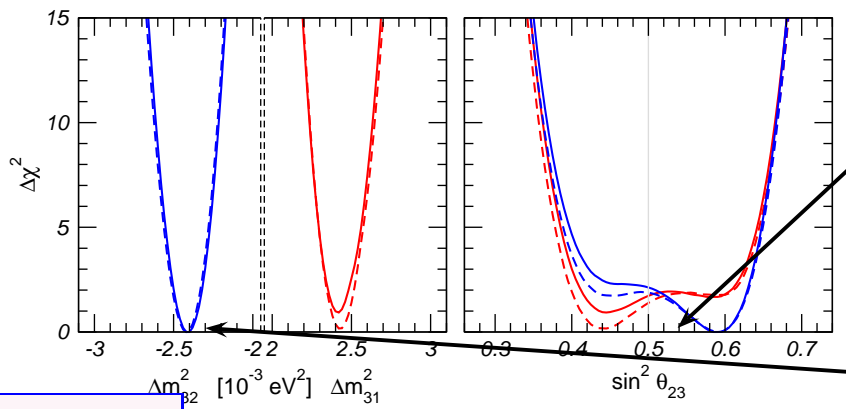


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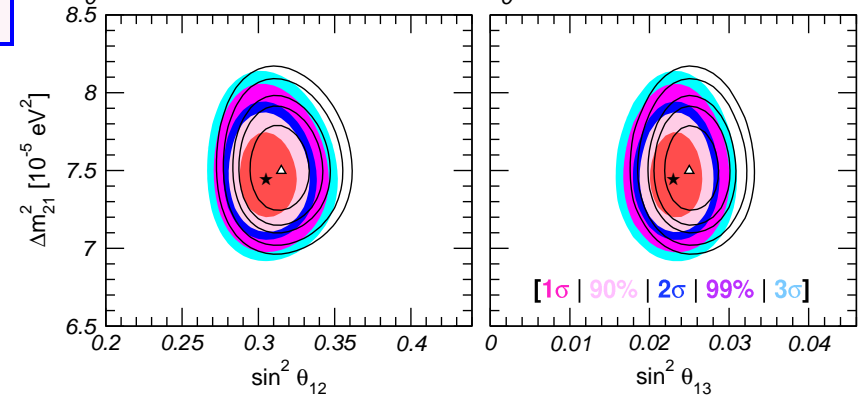
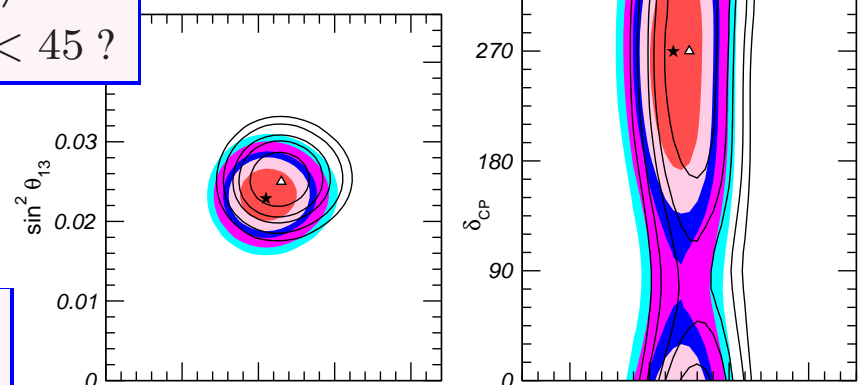
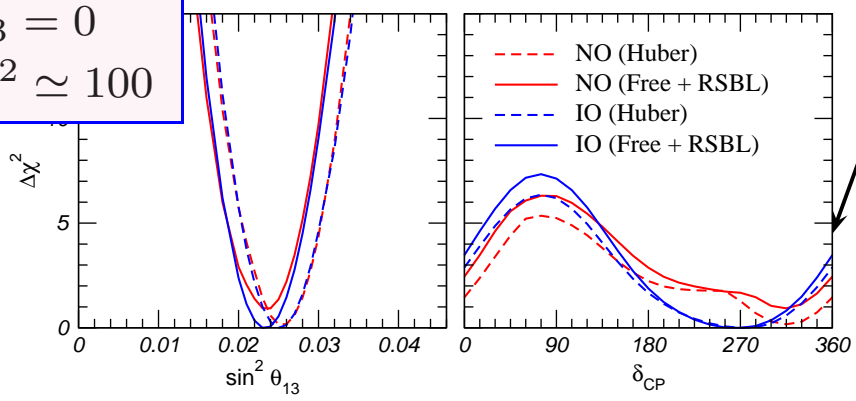


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N/I
 δ_{CP}



$\theta_{13} = 0$
 $\Delta\chi^2 \simeq 100$



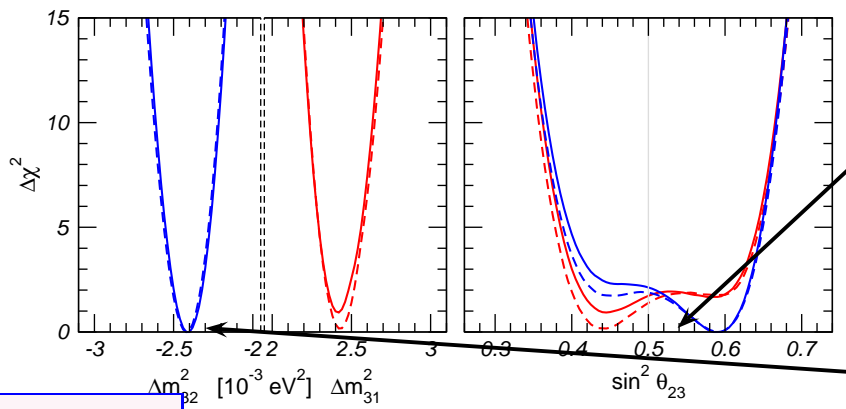
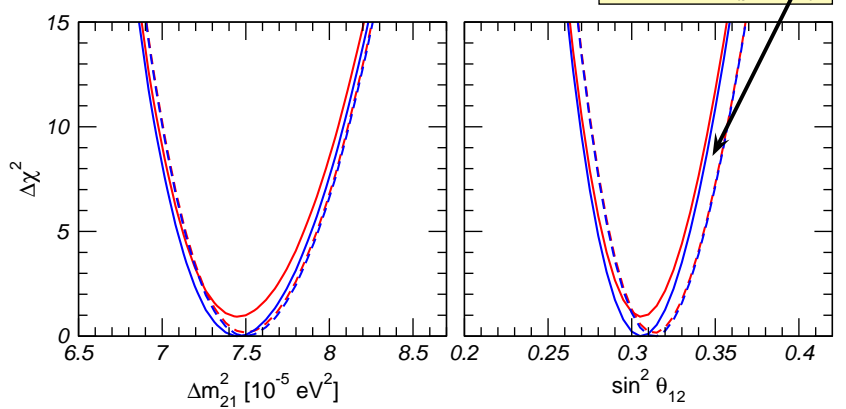
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Curves = uncertainty on reactor fluxes

NuFIT 1.2 (prelim)

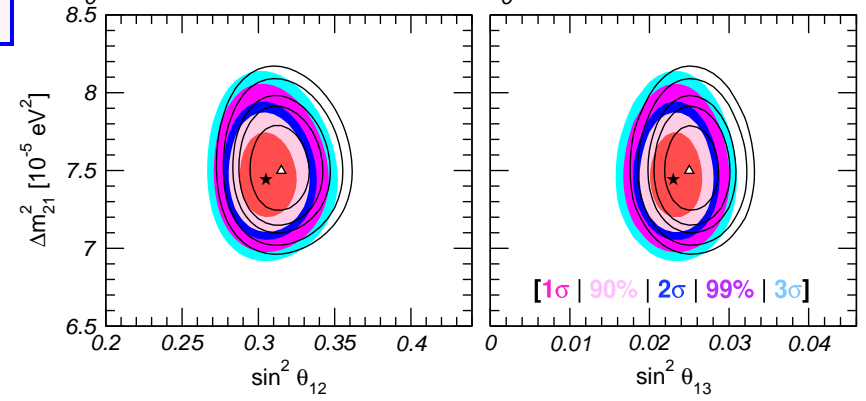
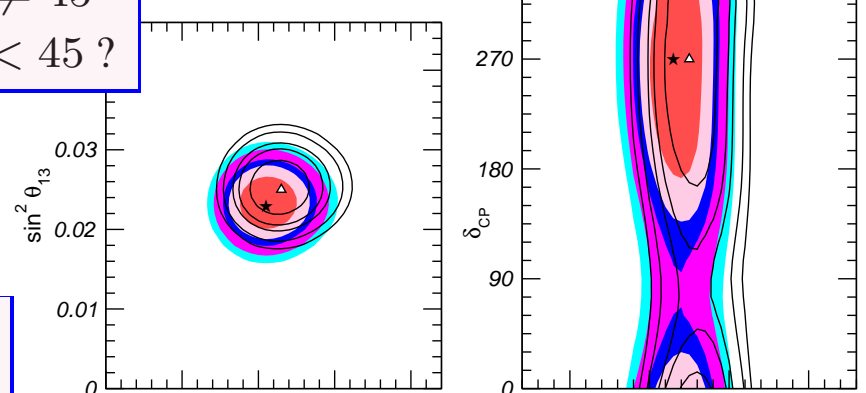
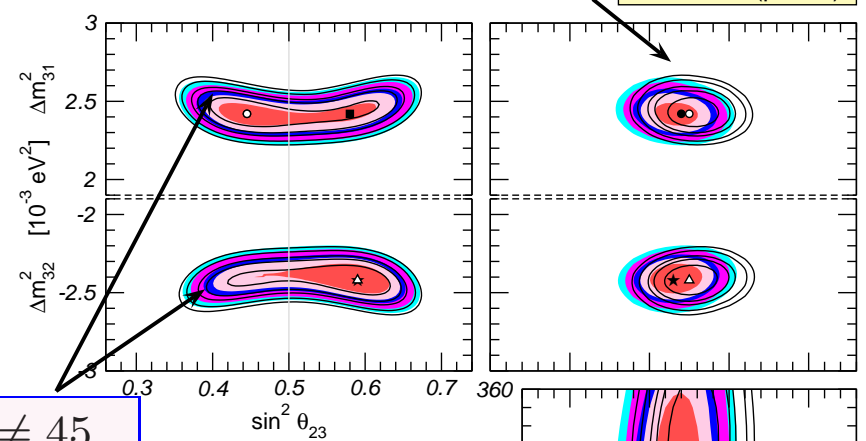
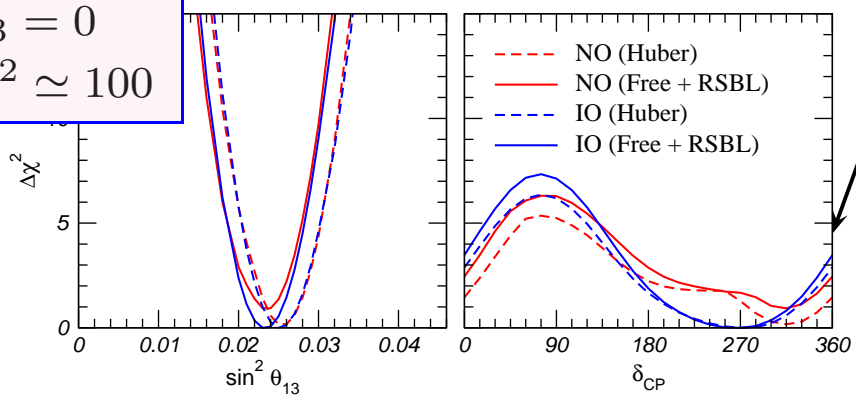
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3 ν Analysis: “12” Sector

- $\Delta m_{13}^2 \gg E/L \Rightarrow P_{ee}^{3\nu} = c_{13}^4 P_{2\nu} + s_{13}^4$

$$i \frac{d}{dt} \begin{pmatrix} \nu_e \\ \nu_a \end{pmatrix} = \left[\frac{\Delta m_{21}^2}{4E} \begin{pmatrix} -\cos 2\theta_{12} & \sin 2\theta_{12} \\ \sin 2\theta_{12} & \cos 2\theta_{12} \end{pmatrix} \pm \sqrt{2} G_F N_e \begin{pmatrix} c_{13}^2 & 0 \\ 0 & 0 \end{pmatrix} \right] \begin{pmatrix} \nu_e \\ \nu_a \end{pmatrix}$$

$$P_{ee} \simeq \begin{cases} \text{Solar High E : } c_{13}^4 \sin^2 2\theta_{12} \\ \text{Solar Low E : } c_{13}^4 \left(1 - \sin^2 2\theta_{12}/2 \right) \\ \text{Kam : } c_{13}^4 \left(1 - \sin^2 2\theta_{12} \sin^2 \frac{\Delta m_{21}^2 L}{4E} \right) \end{cases}$$

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With $\theta_{13} = 0$

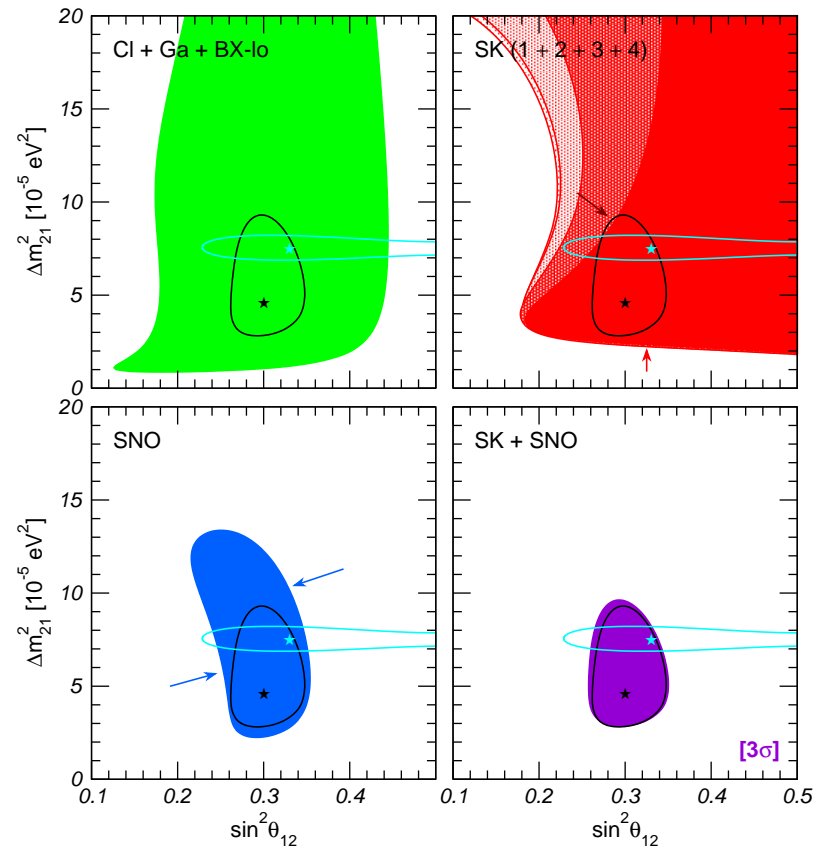
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* Solar region determined by High E data

* Param's $\begin{cases} \theta_{12} \text{ SNO most sensitivity} \\ \Delta m_{21}^2 \text{ by KamLAND} \end{cases}$

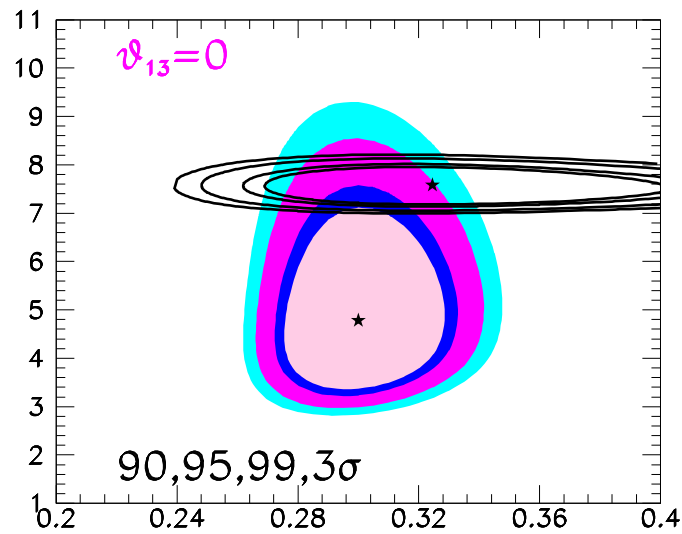
* Tension in best fit between

Solar and KamLAND $\Rightarrow \theta_{13}$ and ...?



3 ν Analysis: “12” Sector and θ_{13}

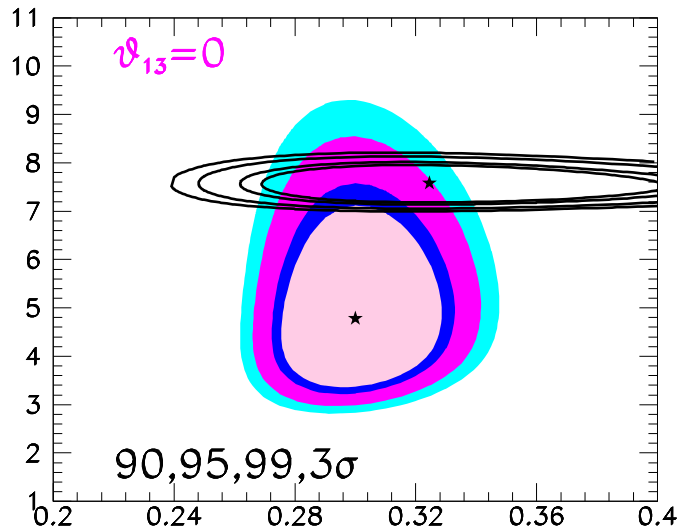
- For $\theta_{13} = 0$



$$\sin^2 \theta_{12} = \begin{cases} 0.3 & \text{From Solar} \\ 0.325 & \text{From KLAND} \end{cases}$$

3 ν Analysis: “12” Sector and θ_{13}

- For $\theta_{13} = 0$



- When θ_{13} increases

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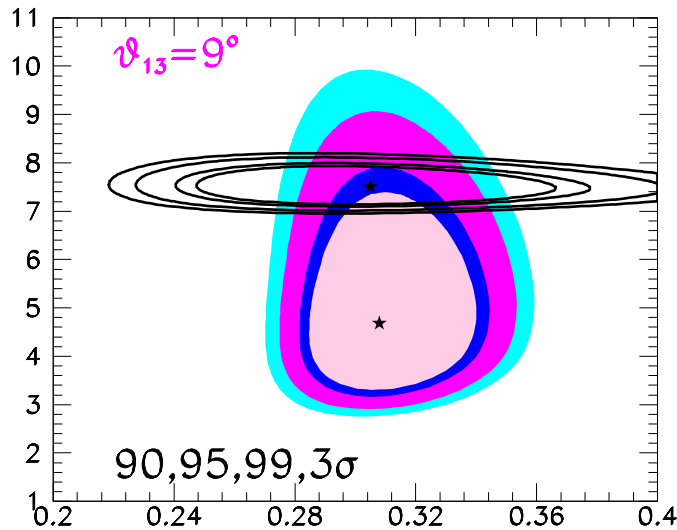
\Rightarrow KamLAND region shifts left

\Rightarrow Solar slight shifts right (due to High E)

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3 ν Analysis: “12” Sector and θ_{13}

- For $\theta_{13} \simeq 9^\circ$

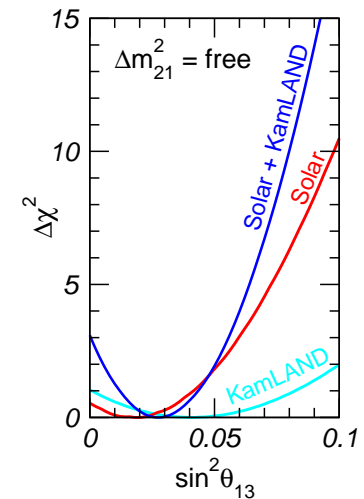
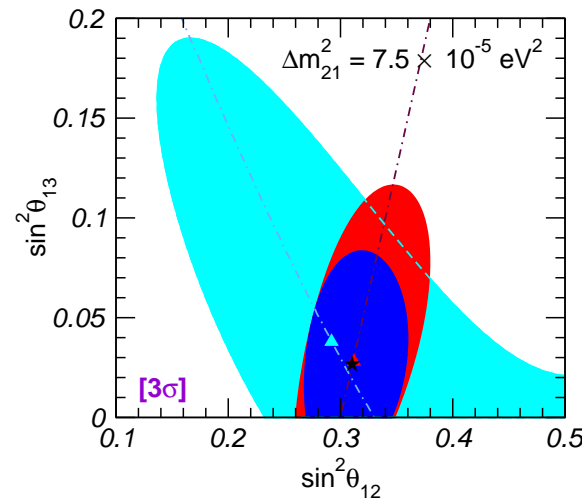


- When θ_{13} increases

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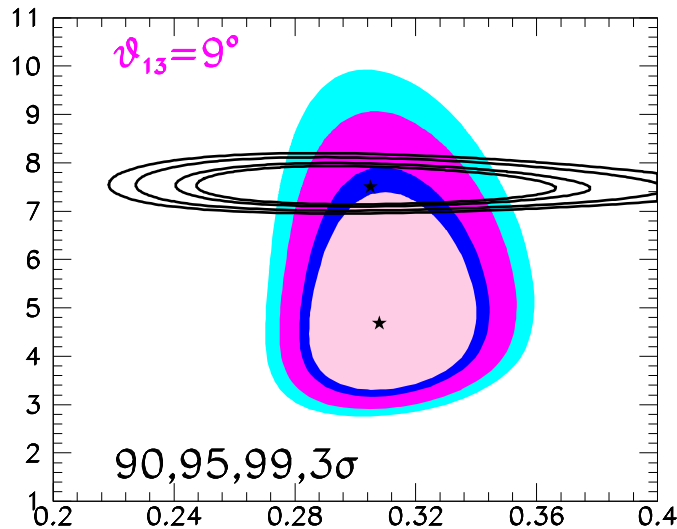
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⇒ Solar slight shifts right (due to High E)



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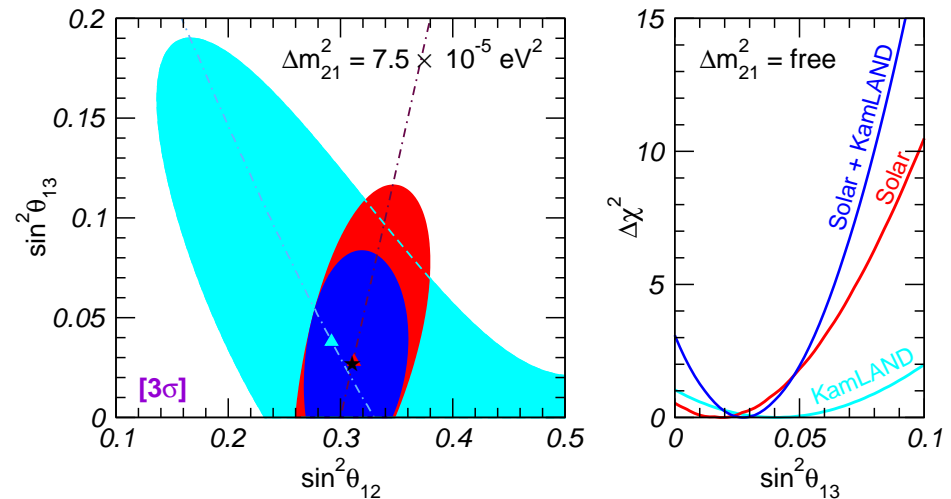


- ⇒ Good match of best fit θ_{12}
- ⇒ Residual tension on Δm_{21}^2

- When θ_{13} increases

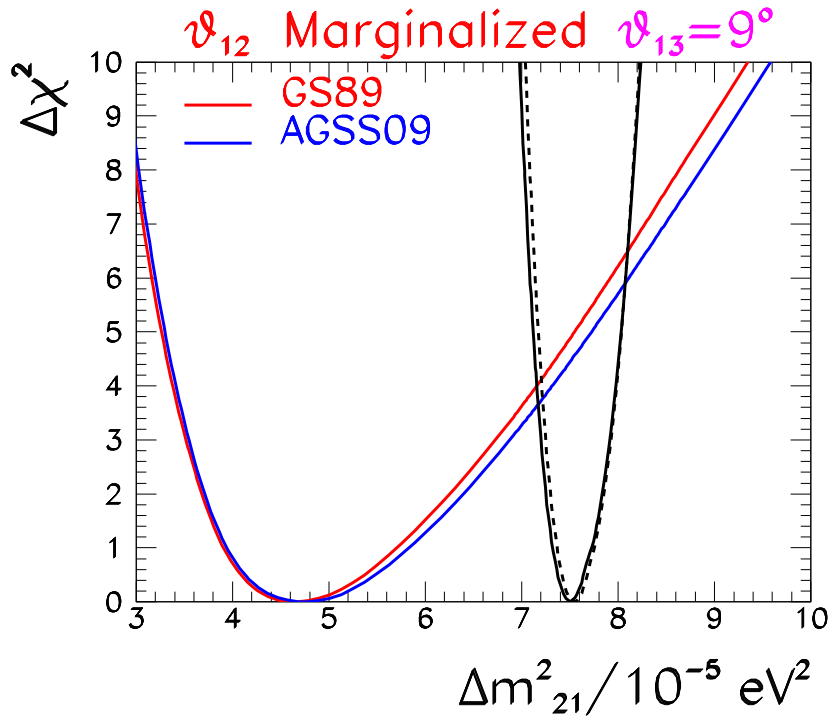
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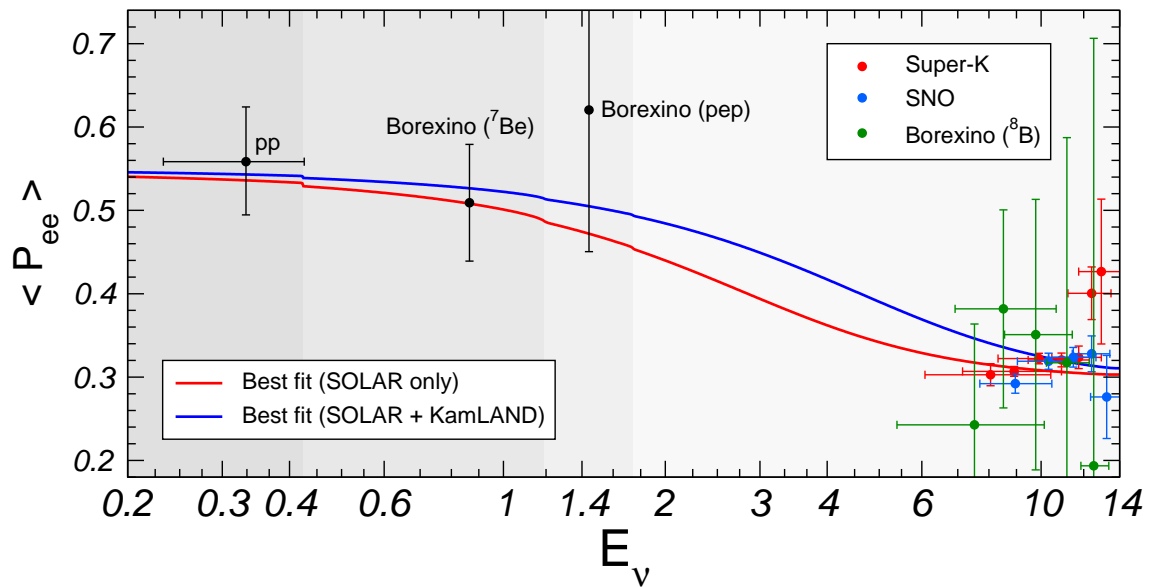


3 ν Analysis: “12” Sector Δm_{21}^2

- Residual tension on Δm_{21}^2 between Solar and KamLAND



- Tension related to smaller-than-expected low-E turn up from MSW at best global fit



Talk by A. Renshaw

3 ν Analysis: “12” Sector and the Solar Fluxes

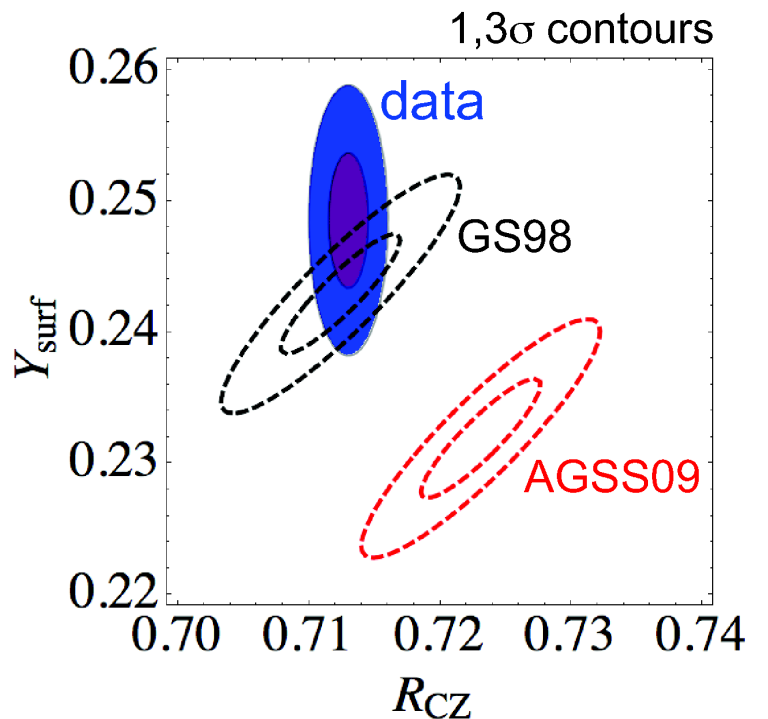
- Newer determination of abundance of heavy elements in solar surface give lower values
- Solar Models with these lower metallicities fail in reproducing helioseismology data

- Two sets of SSM:

Starting from Bahcall *etal* 05, Serenelli *etal* 0909.2668

GS98 uses older metallicities

AGSXX uses newer metallicities



Flux $\text{cm}^{-2} \text{s}^{-1}$	GS98	AGSS09
pp/ 10^{10}	5.97 (1 ± 0.006)	6.03 (1 ± 0.005)
pep/ 10^8	1.41 (1 ± 0.011)	1.44 (1 ± 0.010)
hep/ 10^3	7.91 (1 ± 0.15)	8.18 (1 ± 0.15)
$^7\text{Be}/10^9$	5.08 (1 ± 0.06)	4.64 (1 ± 0.06)
$^8\text{B}/10^6$	5.88 (1 ± 0.11)	4.85 (1 ± 0.12)
$^{13}\text{N}/10^8$	2.82 (1 ± 0.14)	2.07 ($1^{+0.14}_{-0.13}$)
$^{15}\text{O}/10^8$	2.09 ($1^{+0.16}_{-0.15}$)	1.47 ($1^{+0.16}_{-0.15}$)
$^{17}\text{F}/10^{16}$	5.65 ($1^{+0.17}_{-0.16}$)	3.48 ($1^{+0.17}_{-0.16}$)

Fig. courtesy of Aldo Ianni

Talk by F. Villante

3 ν Analysis: “12” Sector and the Solar Fluxes

– Two sets of SSM:

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3 ν Analysis: “12” Sector and the Solar Fluxes

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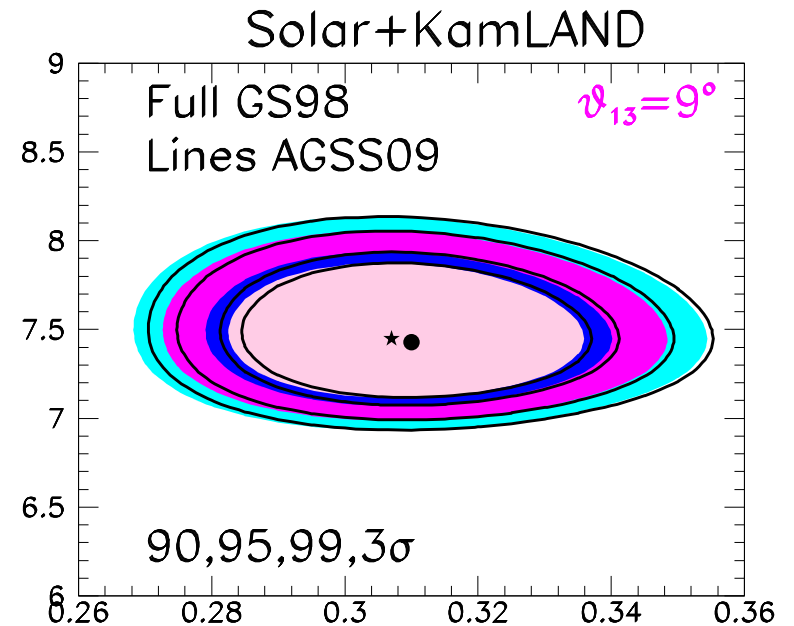
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* What is the effect on the determination of oscillation parameters?

Very small

Impact in Parameter Determination



3 ν Analysis: “12” Sector and the Solar Fluxes

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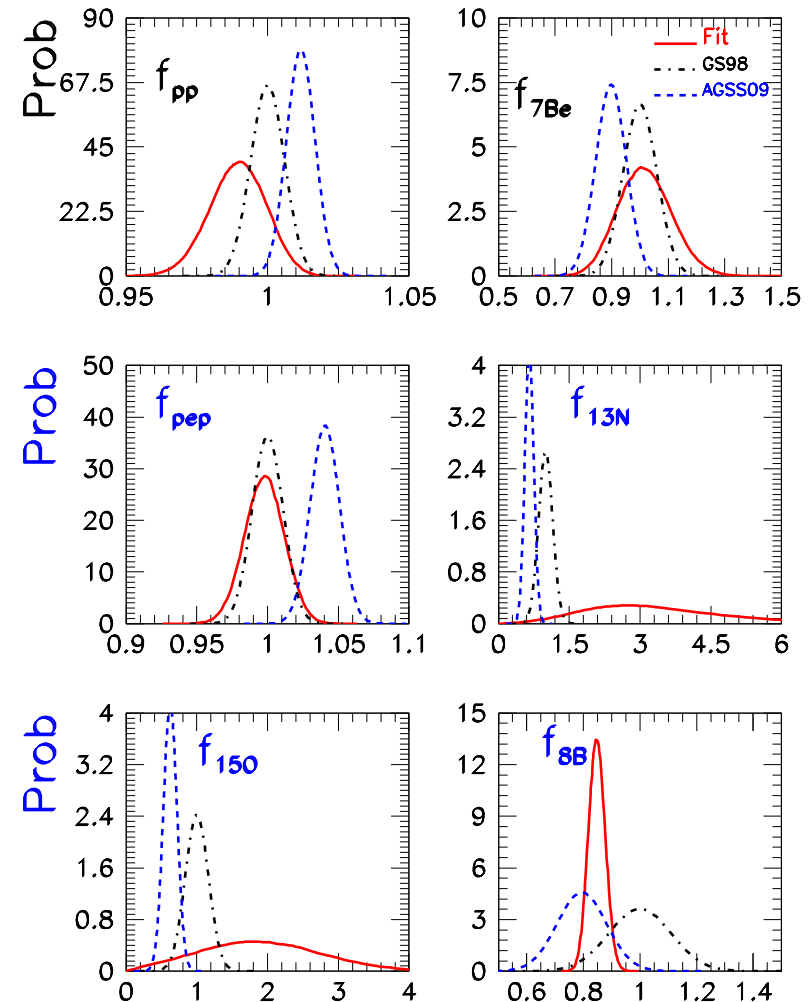
Very small

* Which SSM does the solar data favour?

Both model statistically equally prob

3 ν oscillation fit with solar fluxes free:
(within luminosity constraint)

Comparison with Models



3 ν Analysis: “12” Sector and the Solar Fluxes

– Two sets of SSM:

GS98 uses older metallicities

AGSXX uses newer metallicities

* What is the effect on the determination of oscillation parameters?

Very small

* Which SSM does the solar data favour?

Both model statistically equally prob

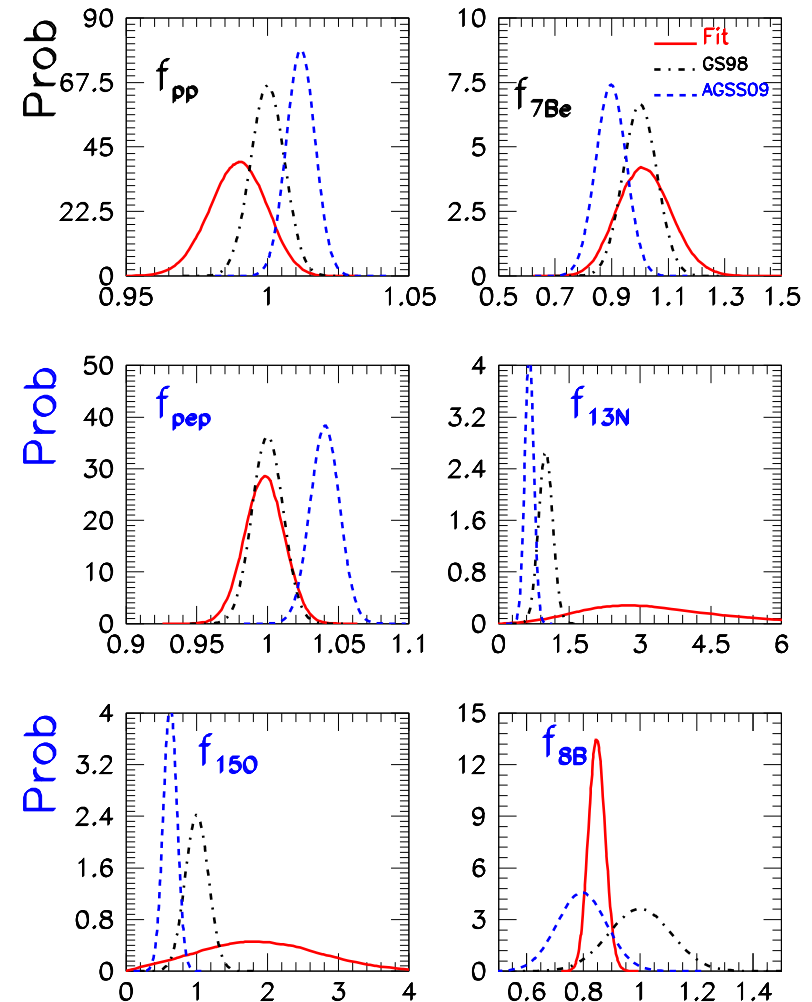
Some improvement if CNO determined:

Cleaner Borexino Talk by F. Calaprice

SNO+ Talk by J. Kaspar

3 ν oscillation fit with solar fluxes free:
(within luminosity constraint)

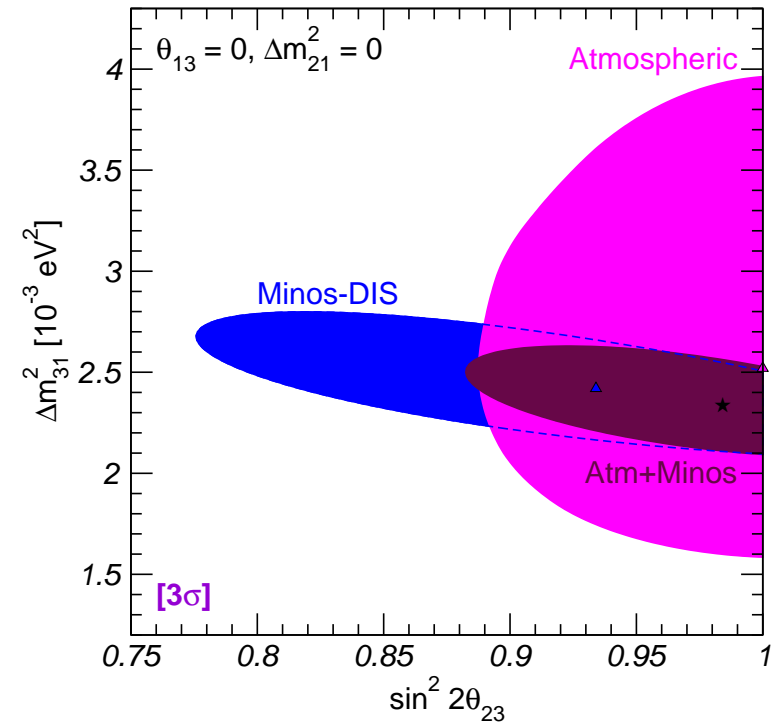
Comparison with Models



MCG-G, Maltoni, Salvado JHEP 2010

3 ν Analysis: “23” Sector ATM and LBL ν_μ Disapp

- Dominant Oscillations $\nu_\mu \rightarrow \nu_\tau$:
 - * Δm_{31}^2 is best determined
by **Minos-DIS** $\nu_\mu \rightarrow \nu_\mu$ data
 - * θ_{23} best determined by **SK**
 - * **Minos-DIS** favours non-maximal θ_{23}
- Talk by P. Vahle



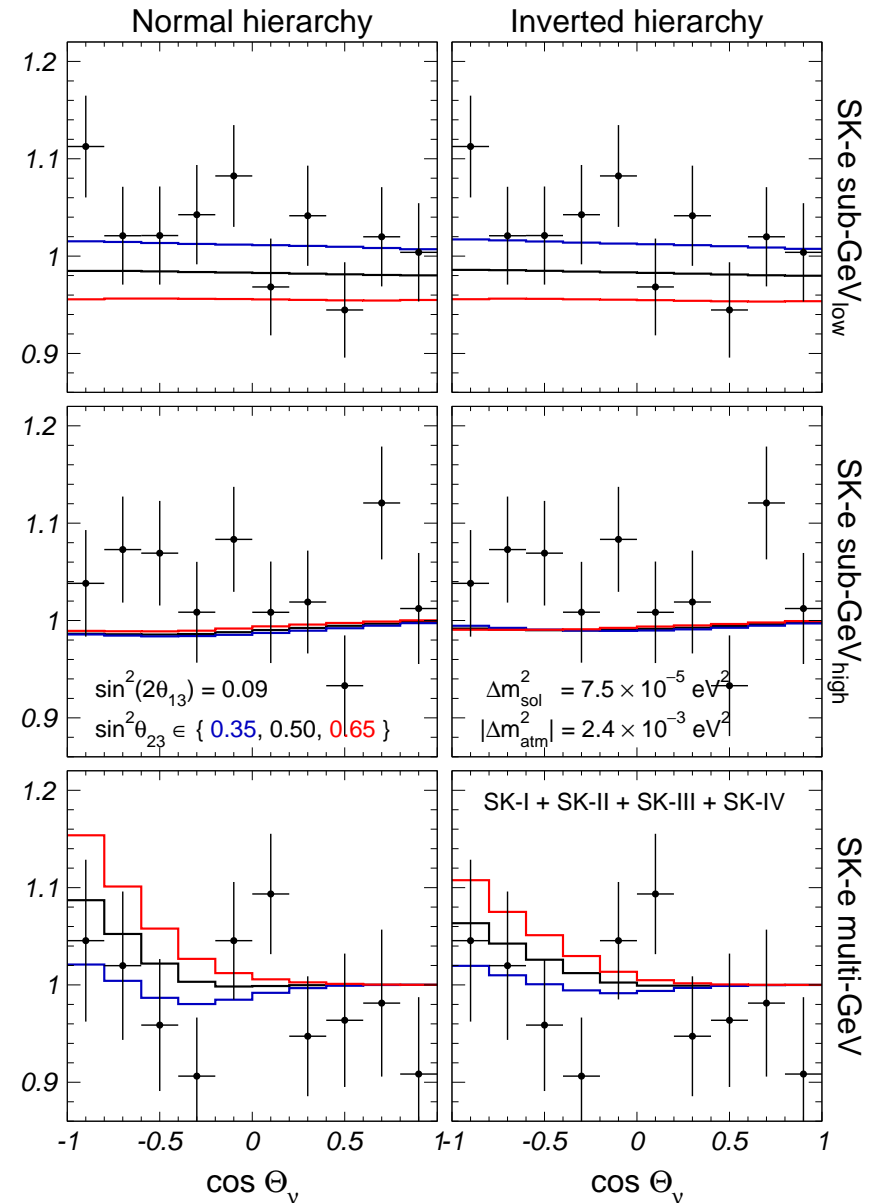
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 - * **Minos-DIS** slight favour non-maximal θ_{23}
 - Talk by P. Vahle

- For $\theta_{31} \neq 0$
 - * **ATM** sensitivity to octant θ_{23} & sign Δm_{31}^2

$$\begin{aligned} \frac{N_e}{N_e^0} - 1 &\simeq (\bar{r} c_{23}^2 - 1) P_{2\nu}(\Delta m_{21}^2, \theta_{12}) \quad [\Delta m_{21}^2 \text{ term}] \\ &+ (\bar{r} s_{23}^2 - 1) P_{2\nu}(\Delta m_{31}^2, \theta_{13}) \quad [\theta_{13} \text{ term}] \\ &- 2\bar{r} s_{13} s_{23} c_{23} \text{Re}(A_{ee}^* A_{\mu e}) \quad [\delta_{CP} \text{ term}] \end{aligned}$$

$$\bar{r} \equiv \Phi_\mu^0 / \Phi_e^0 \simeq 2(\text{subG}), 2.6\text{--}4.6(\text{multiG})$$



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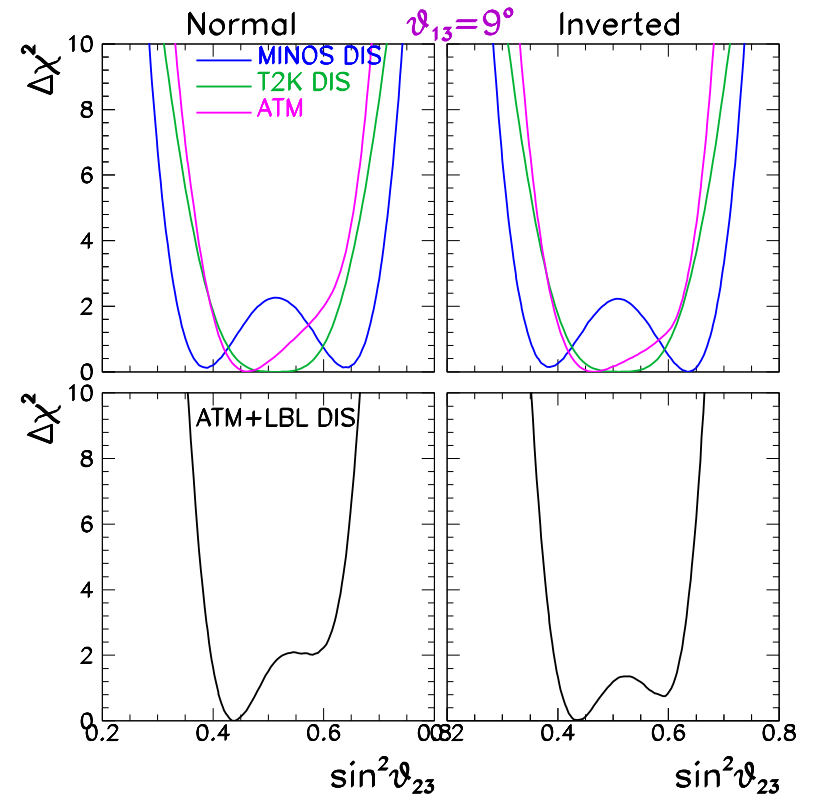
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- * In our analysis excess of sub-GeV e's
 \Rightarrow slight preference for $\theta_{13} < 45^\circ$ in **ATM**

Also analysis by Fogli et al 1205.5254

Not so clear in SK analysis

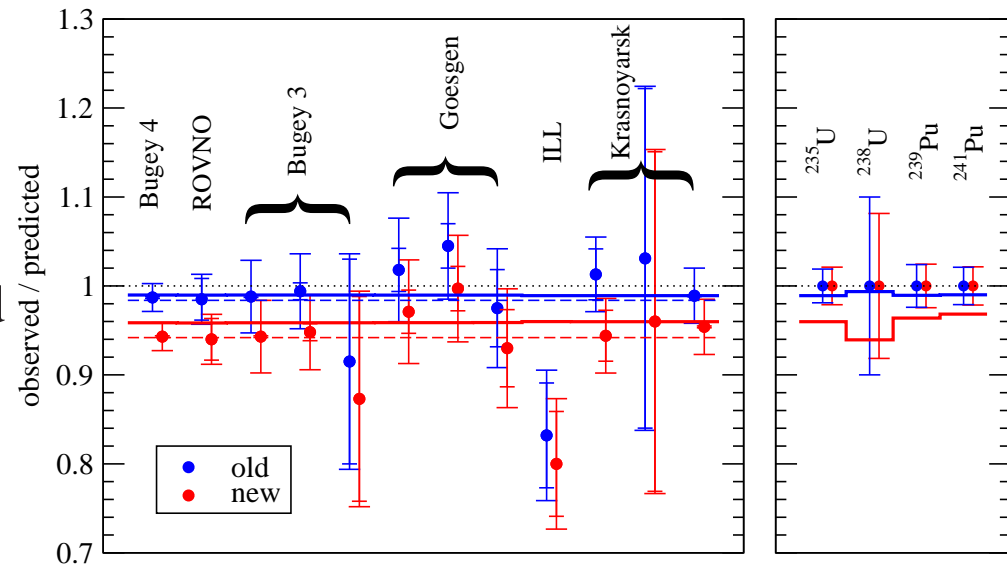
Talks by J. Kameda and K. Okumura



3 ν Analysis: θ_{13} from Reactors and Flux anomaly

- Recently the reactor $\bar{\nu}_e$ fluxes have been recalculated
T.A. Mueller et al., [arXiv:1101.2663].; P. Huber, [arXiv:1106.0687].
- Both reevaluations find higher fluxes by about 3.5 %

- So *negative* reactor experiments at short baselines (RSBL) indeed **observed a deficit**

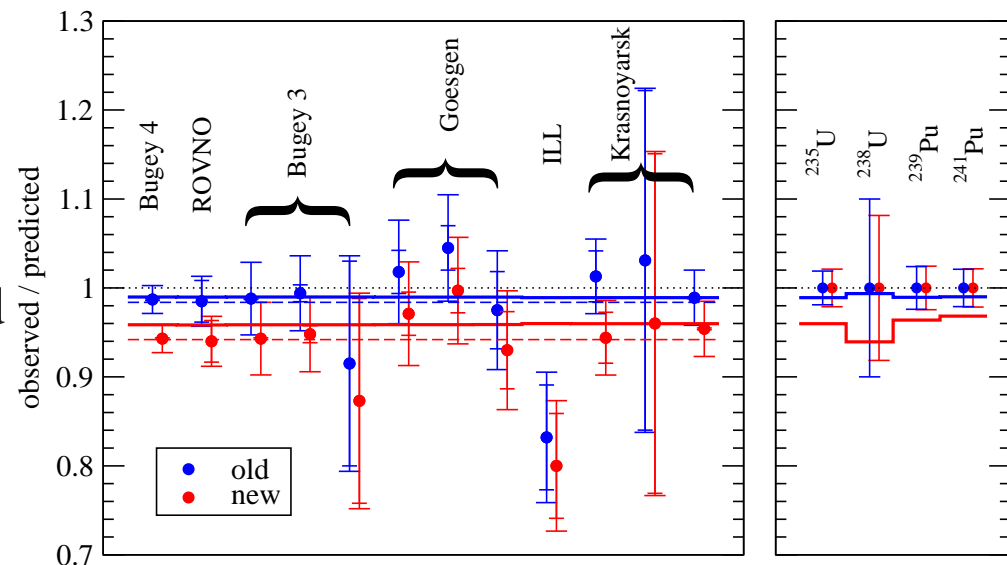


- If due to oscillations $\Delta m^2 \sim \text{eV}^2 \Rightarrow$ sterile ν 's (more soon)

3 ν Analysis: θ_{13} from Reactors and Flux anomaly

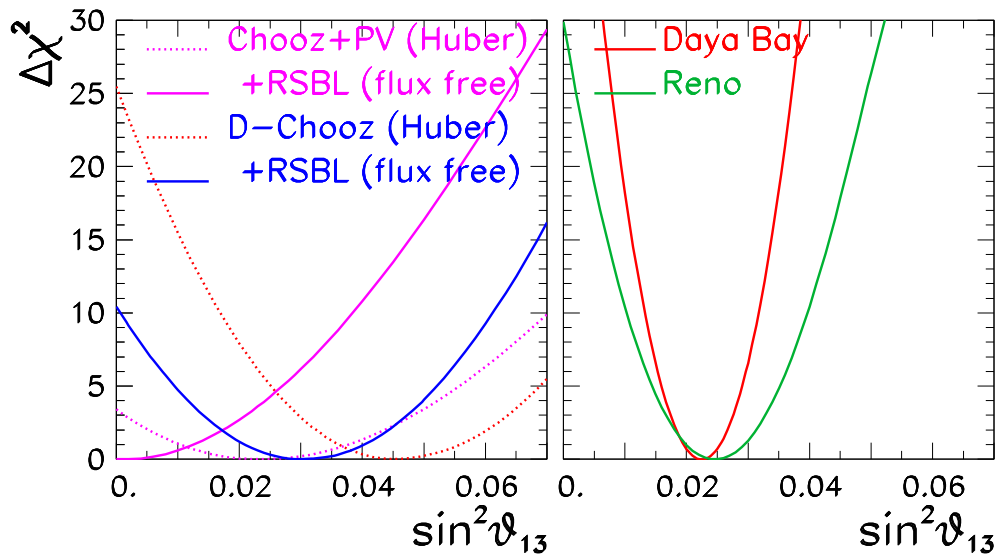
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- For 3ν analysis a consistent approach (T. Schwetz et. al. [arXiv:1103.0734]):
 - Fit oscillation parameters and reactor fluxes simultaneously
 - Use theoretical calculation and/or RSBL data as priors

3 ν Analysis: θ_{13} from Reactors and Flux anomaly



- Experiments without near detector (CHOOZ, Palo-Verde, D-CHOOZ) sensitive to the flux assumptions

- **DAYA-BAY** and **RENO**

Near-Far comparison

⇒ results flux independent

- Two extreme priors :

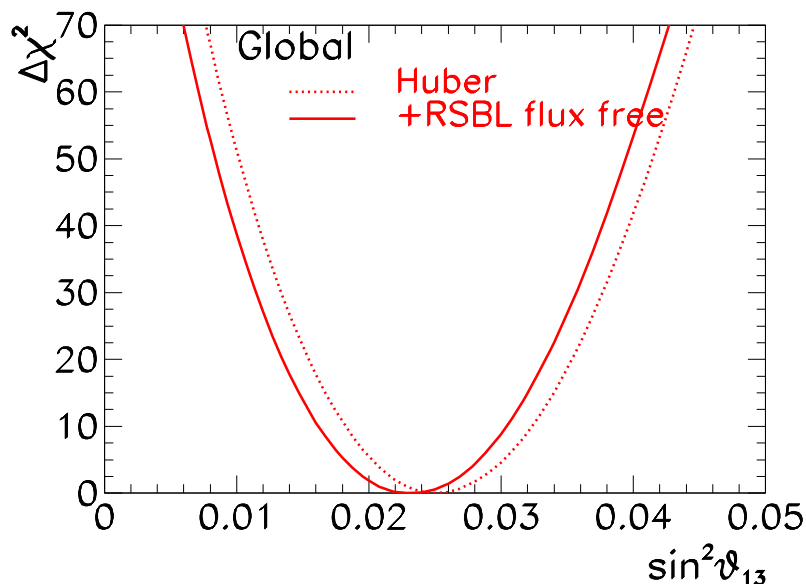
a) Use fluxes from **Huber 1106.0687** without RSBL data

$$\sin^2 \theta_{13} = 0.023^{+0.0026}_{-0.0024}$$

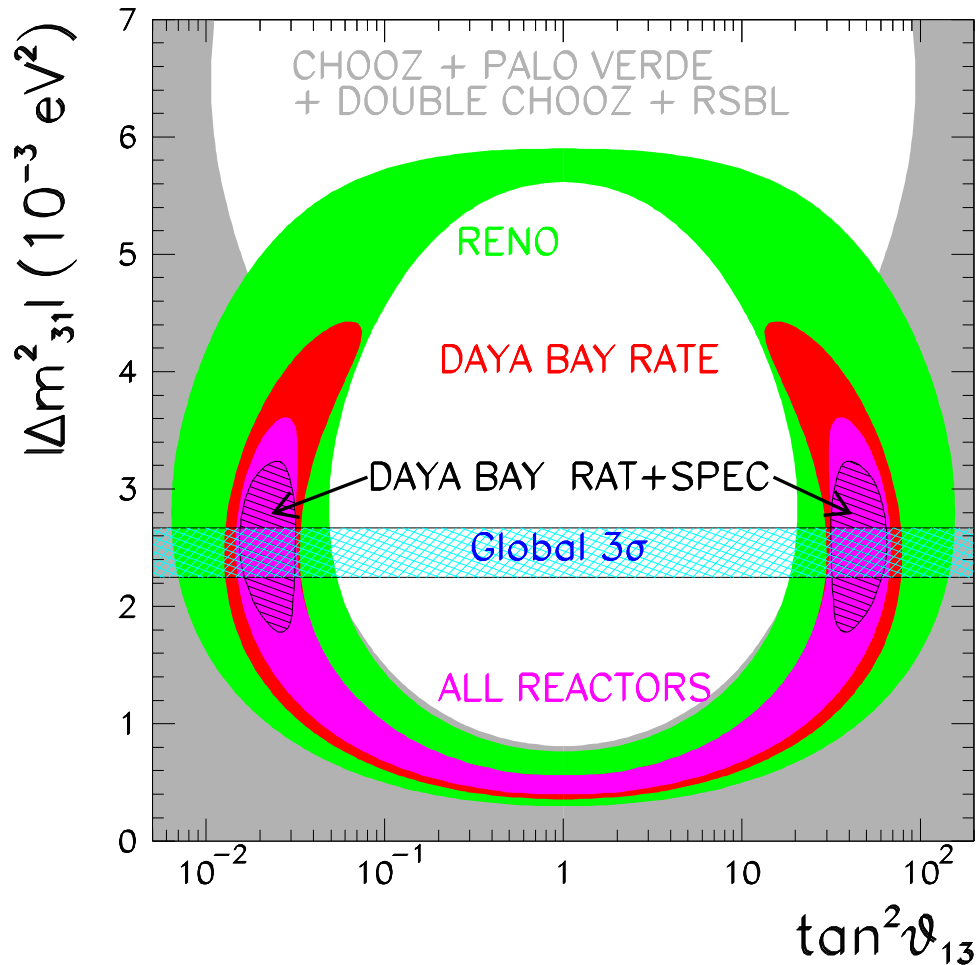
b) Leave flux free and include RSBL

$$\sin^2 \theta_{13} = 0.022^{+0.0026}_{-0.0023}$$

Uncertainty at $\sim 0.5-1\sigma$ level



3 ν Analysis: Reactor Data and Δm_{31}^2



3 σ regions 2dof

- Due to different baselines the combination of reactors provides independent determination of the largest mass splitting
- Improved with Daya-Bay spectrum

Talks at LEN IV Parallel Session

3 ν Analysis: LBL vs REACT and θ_{23} and Ordering

- In LBL APP $\nu_\mu \rightarrow \nu_e$

$$P_{\mu e} \simeq s_{23}^2 \sin^2 2\theta_{13} \left(\frac{\Delta_{31}}{B_\mp} \right)^2 \sin^2 \left(\frac{B_\mp L}{2} \right) + \tilde{J} \frac{\Delta_{12}}{V_E} \frac{\Delta_{31}}{B_\mp} \sin \left(\frac{V_E L}{2} \right) \sin \left(\frac{B_\mp L}{2} \right) \cos \left(\frac{\Delta_{31} L}{2} \pm \delta_{CP} \right)$$

$$B_\pm = \Delta_{31} \pm V_E \quad \tilde{J} = c_{13} \sin^2 2\theta_{13} \sin^2 2\theta_{23} \sin^2 2\theta_{12}$$

So $\sin^2 2\theta_{APP} = 2 \sin^2 \theta_{23} \sin^2 2\theta_{13}$

- In LBL DIS $P_{\mu\mu} \simeq 1 - \sin^2 2\theta_{DIS} \sin^2 \left(\frac{\Delta_{31} L}{2} \right)$

So $\sin^2 \theta_{DIS} = \cos^2 \theta_{13} \sin^2 \theta_{23} \neq \frac{\pi}{4}$

\Rightarrow two possible octacts for θ_{23}

- In Reactor $P_{ee} \simeq \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta_{31} L}{2} \right)$

So $\sin^2 2\theta_{REAC} = \sin^2 2\theta_{13}$

If $\begin{cases} \sin^2 2\theta_{REAC} \leq \sin^2 2\theta_{APP} & \Rightarrow \theta_{23} \geq \frac{\pi}{4} \text{ favoured} \\ \sin^2 2\theta_{REAC} \geq \sin^2 2\theta_{APP} & \Rightarrow \theta_{23} \leq \frac{\pi}{4} \text{ favoured} \end{cases}$

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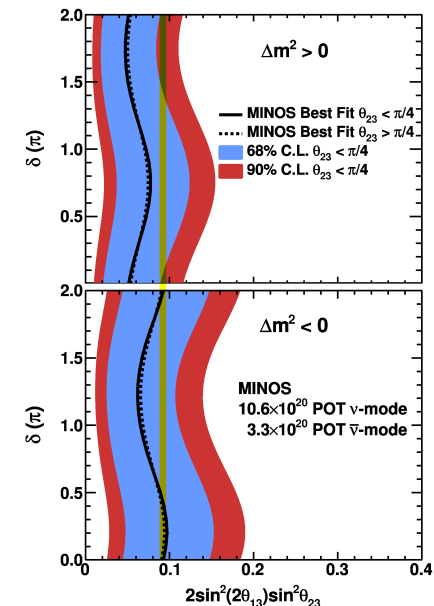
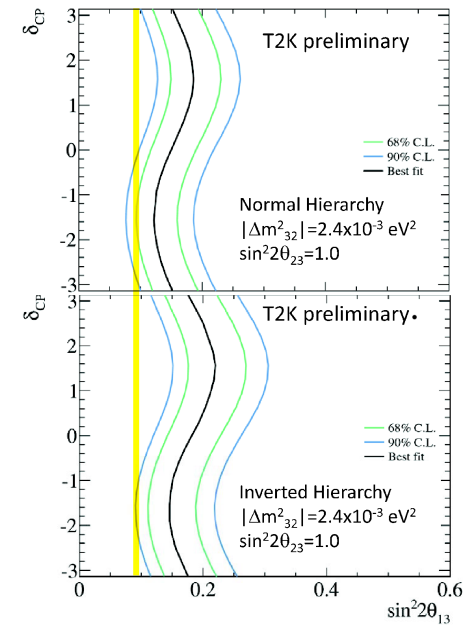
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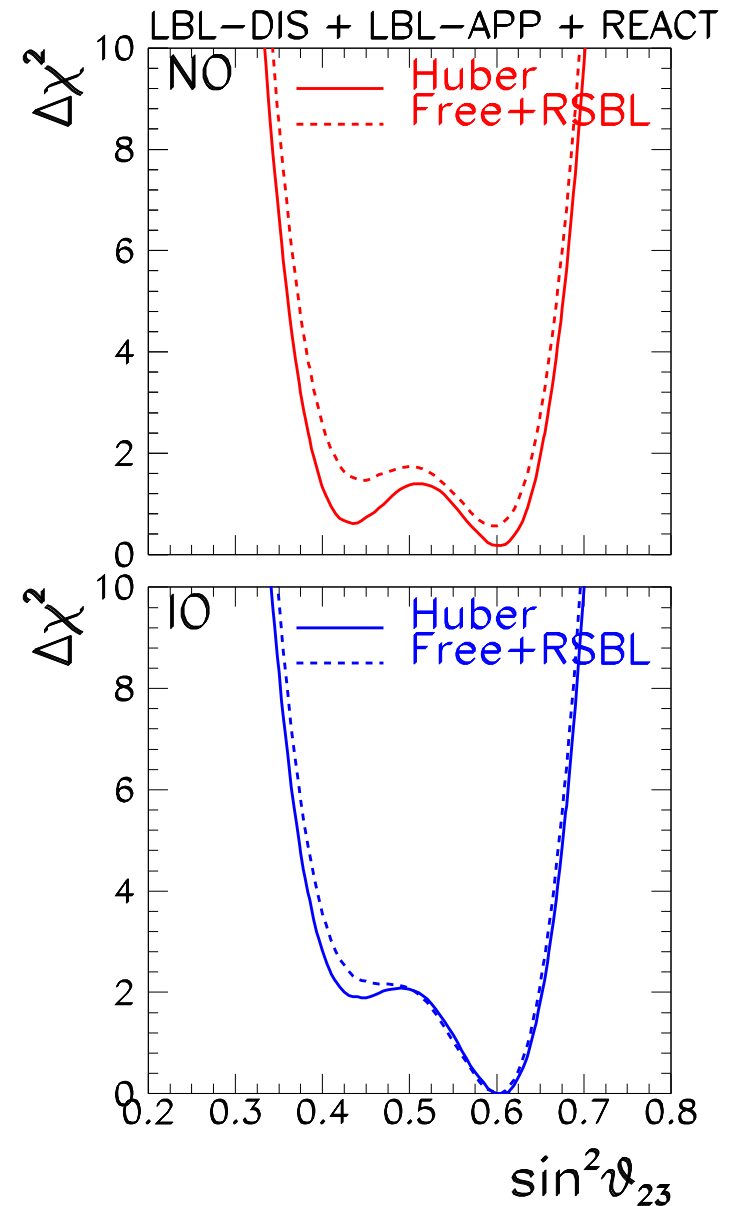
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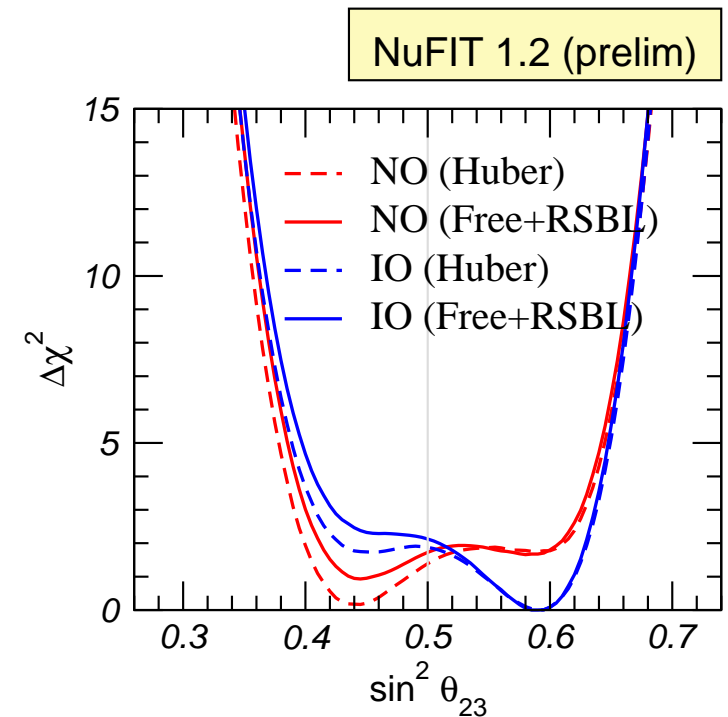
At present with new T2K data

$$\left. \begin{array}{l} \sin^2 2\theta_{REAC} \simeq 0.09 \\ \sin^2 2\theta_{APP-T2K} \simeq 0.1 \end{array} \right\} \Rightarrow \theta_{23} \geq \frac{\pi}{4} \text{ favoured}$$



3 ν : Global Status of θ_{23} and Ordering

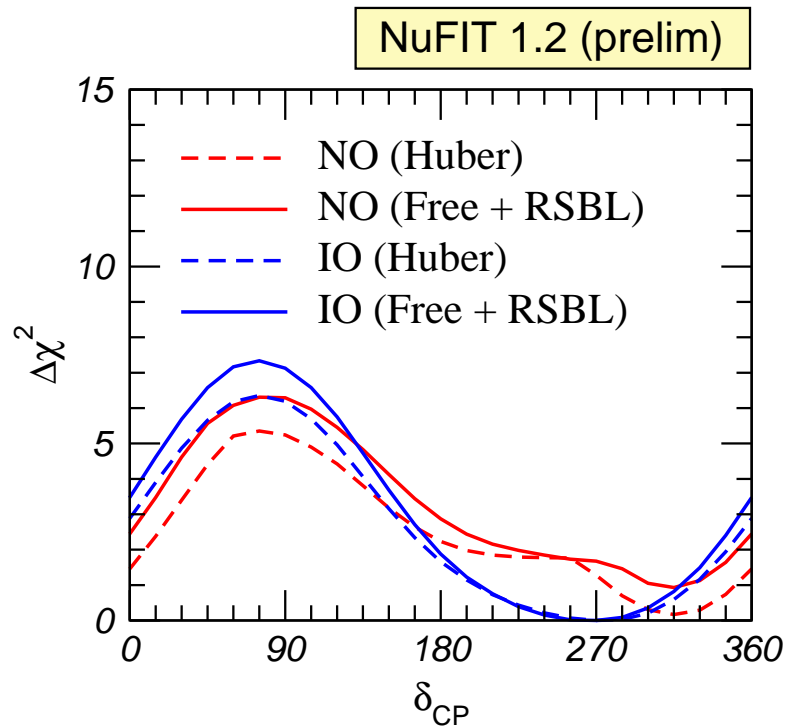
- θ_{23} determination in global analysis:
 - Maximal $\theta_{23} = 45$ Disfavoured at 1.4σ level
Now mostly driven by MINOS ν_μ DIS
 - **NO**: $\theta_{23} < 45$ Favoured at $1.6\text{--}2 \sigma$ level
Driven by SK I–IV ATM Sub-GeV ν_e excess
Also in MINOS-APP+REACT
 - **IO**: $\theta_{23} > 45$ Favoured at $1.4\text{--}1.6 \sigma$ level
Driven by T2K-APP+REACT
- $\text{sign}(\Delta m_{\text{atm}}^2)$ determination in global analysis:
 - No significant difference Normal versus Inverted
IO favoured at $0\text{--}1 \sigma$ level



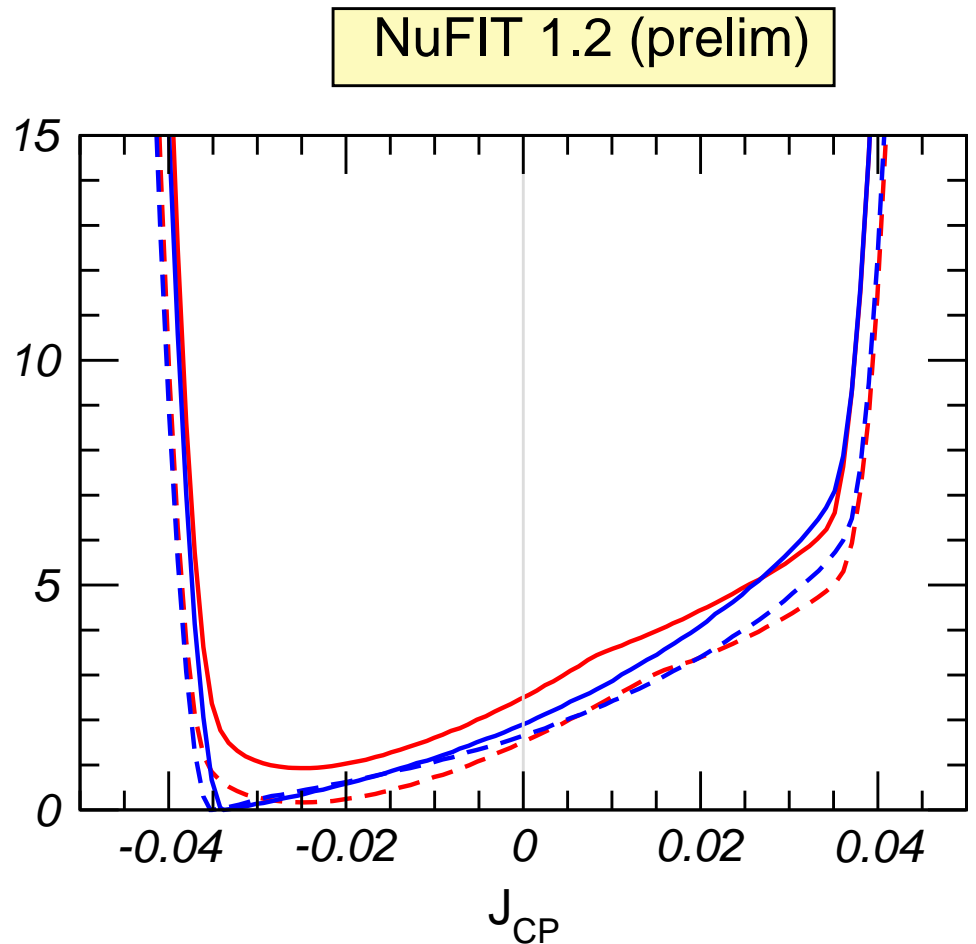
3ν Analysis: Leptonic CP violation

- Driven by the LBL-APP vs REACT θ_{13} with slight influence of ATM
- Projection over leptonic Jarlskog param

$$J \equiv \sin_{12} \cos_{12} \sin_{23} \cos_{23} \sin_{13} \cos_{13}^2 \sin \delta_{CP}$$



- For **IO** Best $\delta \simeq 270^\circ$
 - For **NO** Best $\delta \simeq 300^\circ$
- ($\delta_{CP} = 270 \Rightarrow \sin^2 \theta_{T2K}$ is smallest)



Flavour Parameters: Present Status 1σ (3σ):

z-Garcia

$$\begin{aligned}
 \Delta m_{21}^2 &= 7.45 \pm 0.18 \begin{pmatrix} +0.60 \\ -0.46 \end{pmatrix} \times 10^{-5} \text{ eV}^2 & \theta_{12} &= 33.5^\circ \begin{pmatrix} +0.8 \\ -0.7 \end{pmatrix} \begin{pmatrix} +2.5 \\ -2.1 \end{pmatrix} \\
 \Delta m_{31}^2(\text{N}) &= 2.42 \begin{pmatrix} +0.06 \\ -0.06 \end{pmatrix} \begin{pmatrix} +0.21 \\ -0.18 \end{pmatrix} \times 10^{-3} \text{ eV}^2 & \theta_{23} &= \begin{cases} (\text{N}) 41.8^\circ \begin{pmatrix} +9.2^\circ \\ -1.85^\circ \end{pmatrix} \begin{pmatrix} +12.8^\circ \\ -4.8^\circ \end{pmatrix} \\ (\text{I}) 50.2^\circ \begin{pmatrix} +1.7^\circ \\ -2.5^\circ \end{pmatrix} \begin{pmatrix} +4.3^\circ \\ -12.6^\circ \end{pmatrix} \end{cases} \\
 |\Delta m_{32}^2|(\text{I}) &= 2.42 \begin{pmatrix} +0.07 \\ -0.05 \end{pmatrix} \begin{pmatrix} +0.19 \\ -0.18 \end{pmatrix} \times 10^{-3} \text{ eV}^2 & \theta_{13} &= 8.7^\circ \begin{pmatrix} +0.47 \\ -0.36 \end{pmatrix} \begin{pmatrix} +1.3^\circ \\ -1.3^\circ \end{pmatrix} \\
 & & \delta_{\text{CP}} &= \begin{cases} (\text{N}) 315^\circ \begin{pmatrix} +36^\circ \\ -84^\circ \end{pmatrix} \begin{pmatrix} +45^\circ \\ -315^\circ \end{pmatrix} \\ (\text{I}) 270^\circ \begin{pmatrix} +50^\circ \\ -68^\circ \end{pmatrix} \begin{pmatrix} +90^\circ \\ -270^\circ \end{pmatrix} \end{cases}
 \end{aligned}$$

$$|U|_{\text{LEP}(3\sigma)} = \begin{pmatrix} 0.799 \rightarrow 0.844 & 0.515 \rightarrow 0.581 & 0.129 \rightarrow 0.173 \\ 0.212 \rightarrow 0.527 & 0.426 \rightarrow 0.707 & 0.598 \rightarrow 0.805 \\ 0.233 \rightarrow 0.538 & 0.450 \rightarrow 0.722 & 0.573 \rightarrow 0.787 \end{pmatrix}$$

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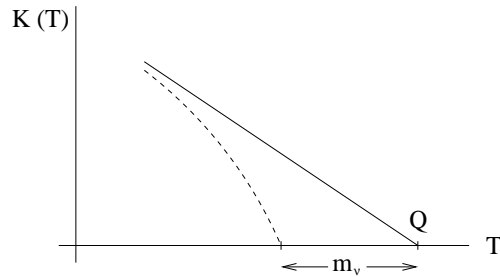
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- Good progress but still precision very far from:

$$|V|_{\text{CKM}} = \begin{pmatrix} 0.97427 \pm 0.00015 & 0.22534 \pm 0.0065 & (3.51 \pm 0.15) \times 10^{-3} \\ 0.2252 \pm 0.00065 & 0.97344 \pm 0.00016 & (41.2 \begin{smallmatrix} +1.1 \\ -5 \end{smallmatrix}) \times 10^{-3} \\ (8.67 \begin{smallmatrix} +0.29 \\ -0.31 \end{smallmatrix}) \times 10^{-3} & (40.4 \begin{smallmatrix} +1.1 \\ -0.5 \end{smallmatrix}) \times 10^{-3} & 0.999146 \begin{smallmatrix} +0.000021 \\ -0.000046 \end{smallmatrix} \end{pmatrix}$$

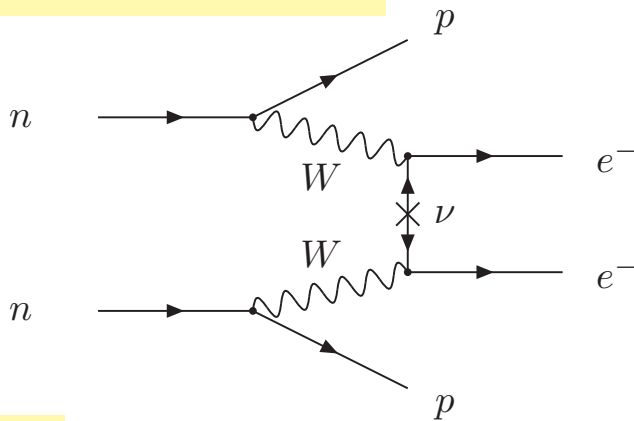
Neutrino Mass Scale

Single β decay : Dirac or Majorana ν mass modify spectrum endpoint



$$m_{\nu_e}^2 = \sum m_j^2 |U_{ej}|^2 = c_{13}^2 c_{12}^2 m_1^2 + c_{13}^2 s_{12}^2 m_2^2 + s_{13}^2 m_3^2$$

ν -less Double- β decay: \Leftrightarrow Majorana ν 's sensitive to Majorana phases



If m_ν only source of ΔL $(T_{1/2}^{0\nu})^{-1} \propto (m_{ee})^2$

$$m_{ee} = \left| \sum U_{ej}^2 m_j \right|$$

$$= \left| c_{13}^2 c_{12}^2 m_1 e^{i\eta_1} + c_{13}^2 s_{12}^2 m_2 e^{i\eta_2} + s_{13}^2 m_3 e^{-i\delta_{CP}} \right|$$

COSMO Neutrino mass (Dirac or Majorana) modify the growth of structures

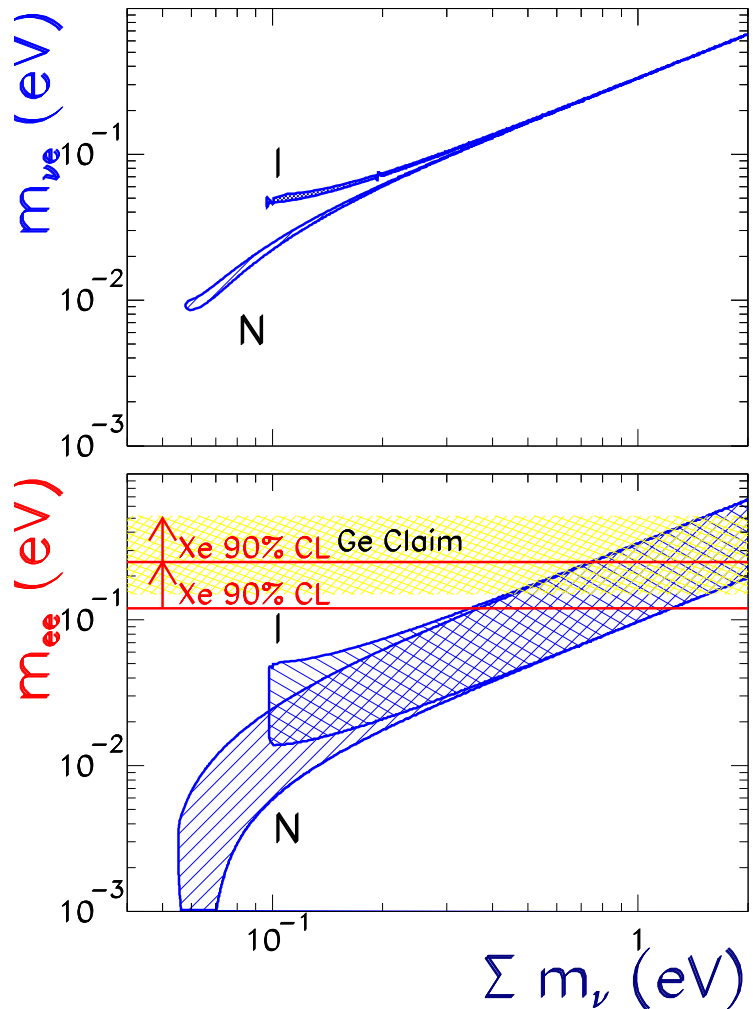
$$\sum m_i$$

Neutrino Mass Scale: The Cosmo-Lab Connection

Global oscillation analysis

⇒ Correlated ranges for m_{ν_e} , m_{ee} and Σm_ν
(Fogli *et al* (04))

Maltoni, Schwetz, Salvado, MCGG (95%)

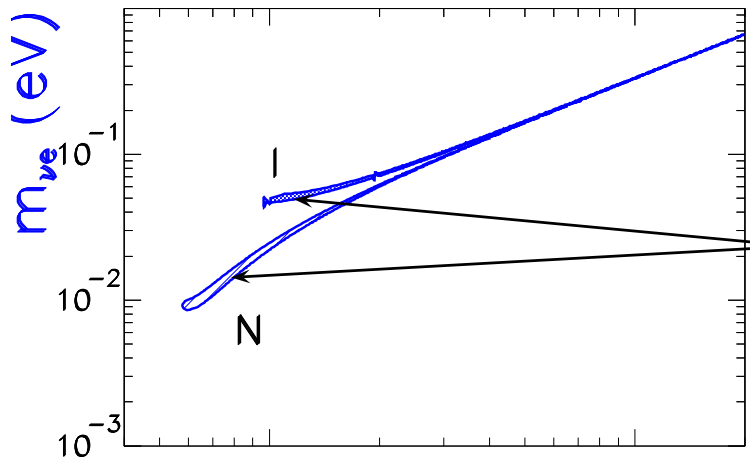


Neutrino Mass Scale: The Cosmo-Lab Connection

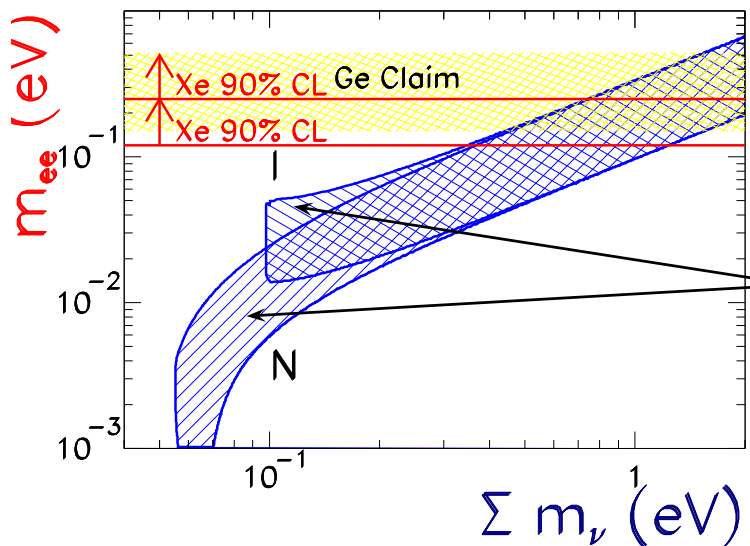
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Maltoni, Schwetz, Salvado, MCGG (95%)



Width due to range in oscillation parameters very narrow
High precision determination of m_{ν_e} and $\sum m_i$ can give information on ordering



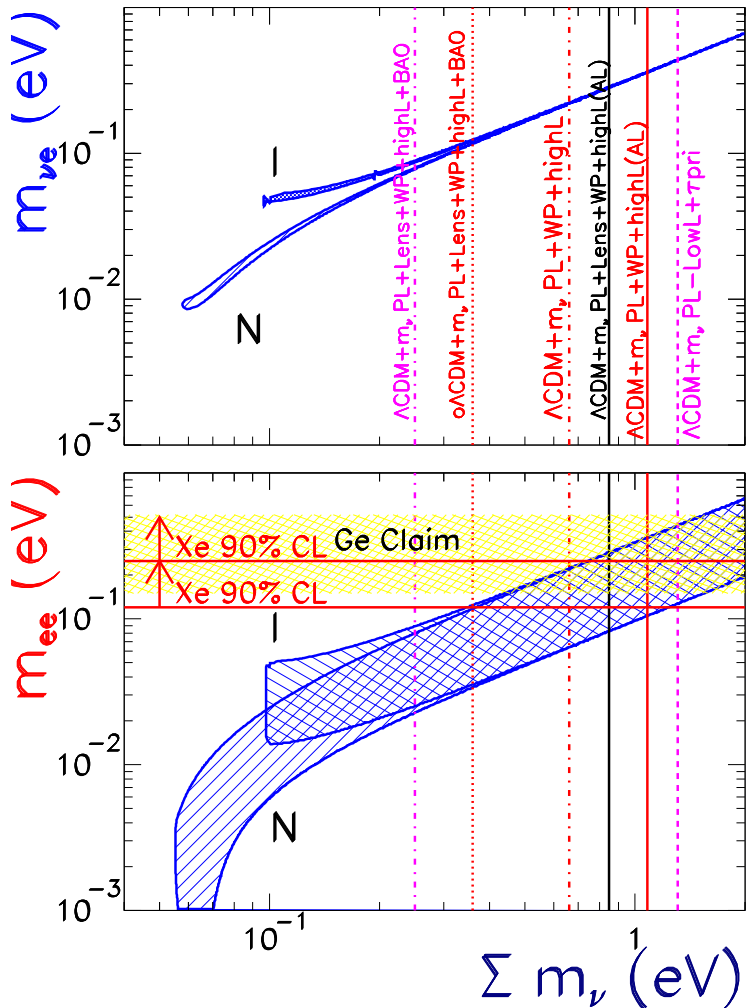
Wide band due to unknown Majorana phases

Neutrino Mass Scale: The Cosmo-Lab Connection

Global oscillation analysis

⇒ Correlated ranges for m_{ν_e} , m_{ee} and $\sum m_\nu$
(Fogli *et al* hep-ph/0408045)

Maltoni, Schwetz, Salvado, MCGG (95%)



Analysis of Cosmological data

Bound on $\sum m_\nu$ changes with:
cosmo parameters fix in analysis
cosmo observables considered

Model	Observables	Σm_ν (eV) 95%
Λ CDM + m_ν	Planck-lowL+ τ prior	≤ 1.31
Λ CDM + m_ν	Planck+WP+highL(A_L)	≤ 1.08
Λ CDM + m_ν	Planck+Lens+WP+highL(A_L)	≤ 0.85
Λ CDM + m_ν	Planck+WP+highL	≤ 0.66
Λ CDM + m_ν	Planck+WP+highL	≤ 0.98
Λ CDM + m_ν	Planck+Lens+WP+highL+BAO	≤ 0.25
Λ CDM + m_ν	Planck+Lens+WP+highL+BAO	≤ 0.36

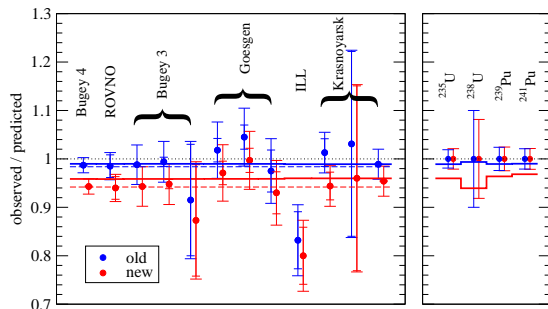
Talk by M. Lattanzi

Light Sterile Neutrinos

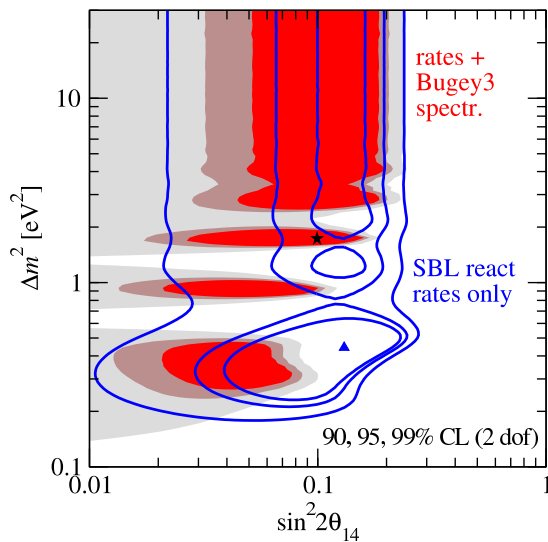
- Several Observations which can be Interpreted as Oscillations with $\Delta m^2 \sim eV^2$

Reactor Anomaly

New reactor flux calculation
 \Rightarrow Deficit in data at $L \lesssim 100$ m



Explained as ν_e disappearance



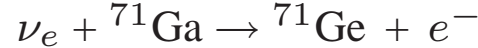
Kopp etal, ArXiv 1303.3011

Gallium Anomaly

Acero, Giunti, Laveder, 0711.4222
 Giunti, Laveder, 1006.3244

Radioactive Sources (^{51}Cr , ^{37}Ar)

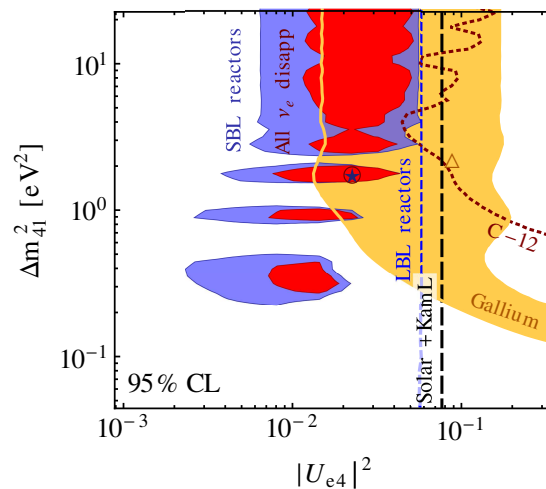
in calibration of Ga Solar Exp;



Give a rate lower than expected

$$R = \frac{N_{\text{obs}}}{N_{\text{Bahc}}^{\text{th}}} = 0.86 \pm 0.05 \quad (2.8\sigma)$$

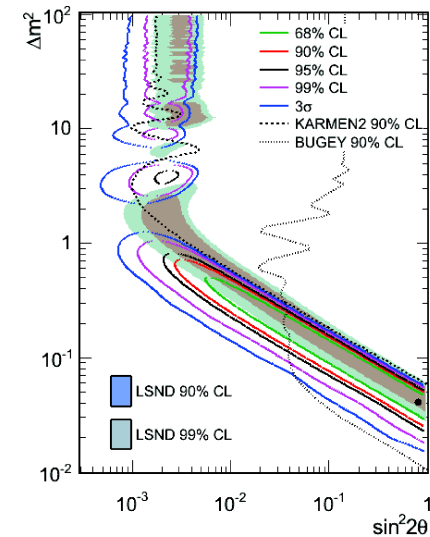
Explained as ν_e disappearance



Kopp etal, ArXiv 1303.3011

LSND, MiniBoone

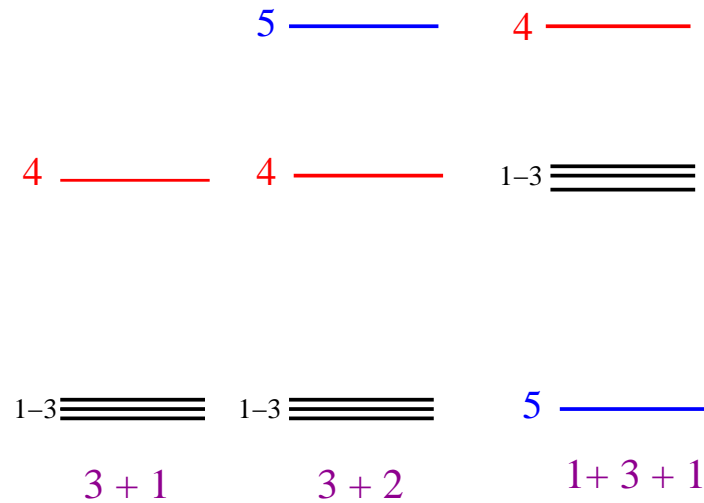
$\nu_\mu \rightarrow \nu_e$ and $\bar{\nu}_\mu \rightarrow \bar{\nu}_e$



Light Sterile Neutrinos

Concha Gonzalez-Garcia

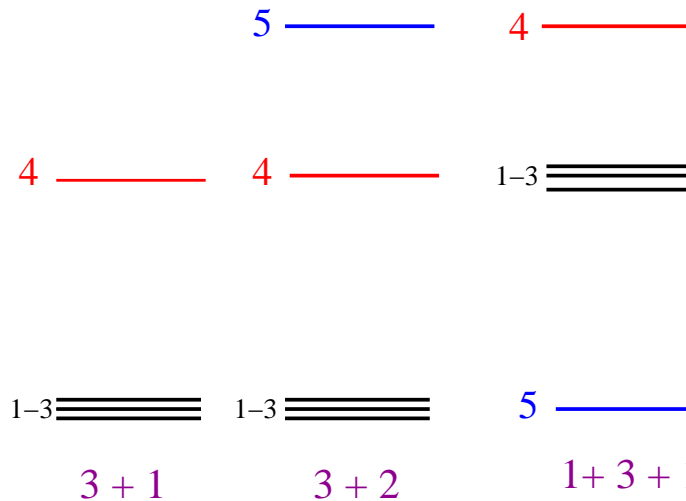
- These explanations require $3+N_s$ mass eigenstates $\rightarrow N_s$ sterile neutrinos



Light Sterile Neutrinos

Concha Gonzalez-Garcia

- These explanations require $3+N_s$ mass eigenstates $\rightarrow N_s$ sterile neutrinos



$\nu_e \rightarrow \nu_e$ **disapp** (REACT,Gallium,Solar, LSND/KARMEN)

- Problem: fit together $\nu_\mu \rightarrow \nu_e$ **app** (LSND,KARMEN,NOMAD,MiniBooNE,E776,ICARUS)

$\nu_\mu \rightarrow \nu_\mu$ **disapp** (CDHS,ATM,MINOS,MiniBooNE)

- Generically: $P(\nu_e \rightarrow \nu_\mu) \sim |U_{ei}^* U_{\mu i}|$ [i =heavier state(s)]

But $|U_{ei}|$ constrained by $P(\nu_e \rightarrow \nu_e)$ disappearance data
 And $|U_{\mu i}|$ constrained by $P(\nu_\mu \rightarrow \nu_\mu)$ disappearance data

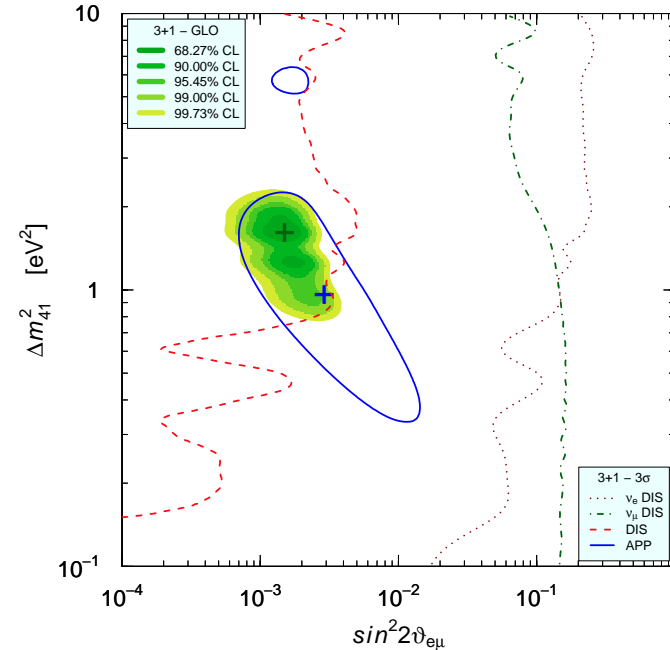
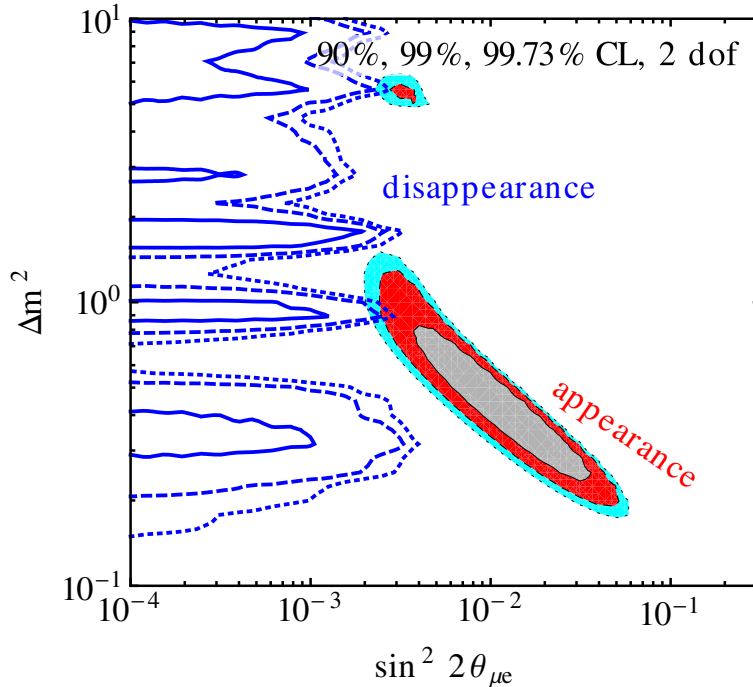
$\} \Rightarrow$ **Severe tension**
 Talk by J.Kopp

Light Sterile Neutrinos:3+1

- Comparing the parameters required to explain signals with bounds from disappearance

Kopp etal, ArXiv 1303.3011

Giunti etal, ArXiv 1308.5288



- Difference in the analysis of both appearance and disappearance
- Somewhat different conclusions:

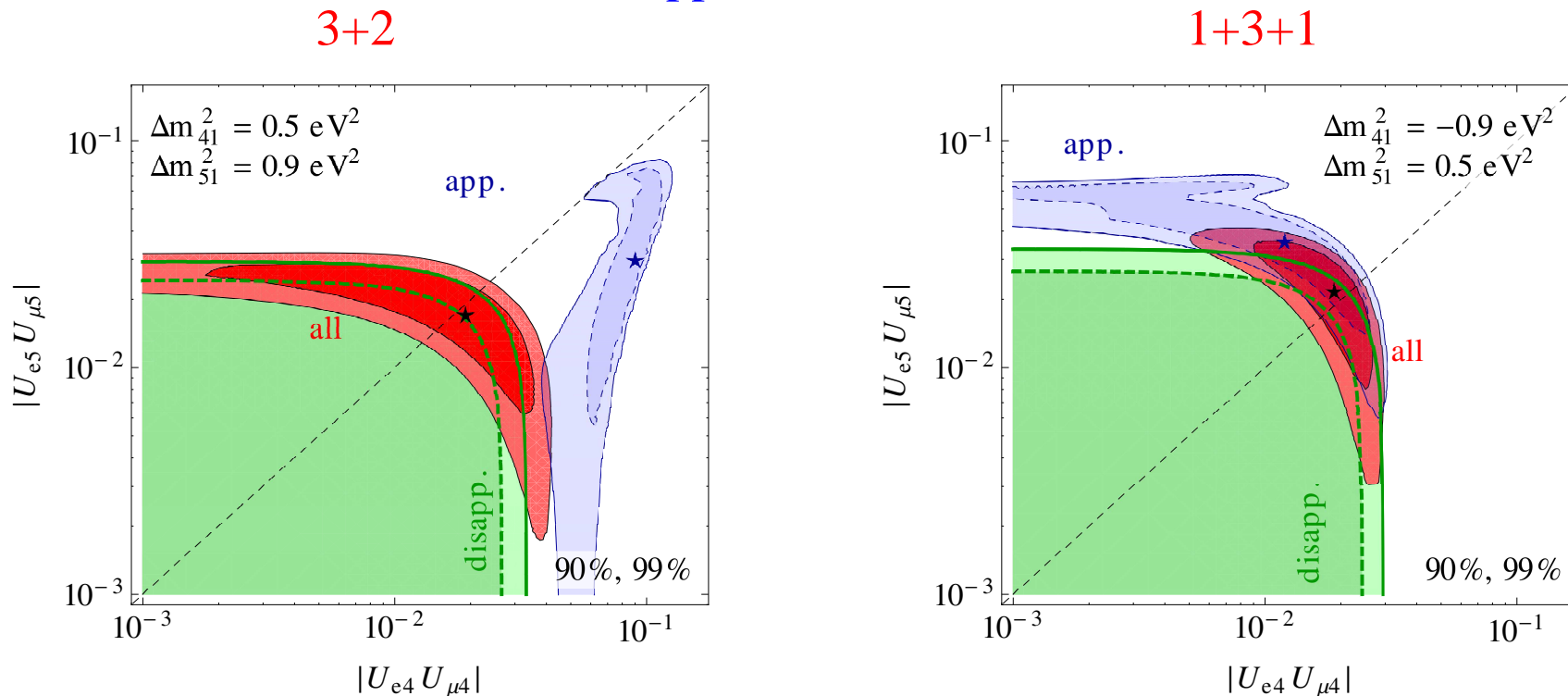
	χ_{\min}^2/dof	$\chi_{\text{PG}}^2/\text{dof}$	PG
K etal	712/(689 - 6)	18.0/2	1.2×10^{-4}
G etal LOW	291.7/(259 - 3)	12.7/2	2×10^{-3}

Light Sterile Neutrinos: Two Steriles

Gonzalez-Garcia

- Comparing the parameters required to explain signals with bounds from dissap

Kopp et al, ArXiv 1303.3011



	χ_{\min}^2/dof	$\chi_{\text{PG}}^2/\text{dof}$	PG
3+2	701/(689 - 14)	25.8/4	3.4×10^{-5}
1+3+1	694/(689 - 14)	16.8/4	2.1×10^{-3}

Also tension with cosmo bounds on dark radiation Talk by N Saviano

Determination of Matter Potential: Non Standard ν Int

- In the three-flavor oscillation picture, the neutrino evolution equation reads:

$$i \frac{d}{dx} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = H^\nu \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} \quad \text{with } H^\nu = H_{\text{vac}} + H_{\text{mat}} \quad \text{and} \quad H^{\bar{\nu}} = (H_{\text{vac}} - H_{\text{mat}})^*$$

- The most general matter potential can be parametrized

$$H_{\text{mat}} = \sqrt{2}G_F N_e(r) \begin{pmatrix} 1 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{pmatrix} + \sqrt{2}G_F \sum_{f=e,u,d} N_f(r) \begin{pmatrix} \varepsilon_{ee}^f & \varepsilon_{e\mu}^f & \varepsilon_{e\tau}^f \\ \varepsilon_{e\mu}^{f*} & \varepsilon_{\mu\mu}^f & \varepsilon_{\mu\tau}^f \\ \varepsilon_{e\tau}^{f*} & \varepsilon_{\mu\tau}^{f*} & \varepsilon_{\tau\tau}^f \end{pmatrix}$$

Deviations from $H_{\text{mat}}^{\text{SM}} = \sqrt{2}G_F N_e(r) \text{diag}(1, 0, 0)$ can be due to **NSI**

$$\mathcal{L}_{\text{NSI}} = -2\sqrt{2}G_F \varepsilon_{\alpha\beta}^{fP} (\bar{\nu}_\alpha \gamma^\mu \nu_\beta) (\bar{f} \gamma_\mu P f), \quad P = L, R$$

$$\text{with } \varepsilon_{\alpha\beta}^f = \varepsilon_{\alpha\beta}^{fL} + \varepsilon_{\alpha\beta}^{fR}$$

- The 3ν evolution depends on 6 (vac) + 8 (mat) = 14 Parameters

Matter Potential/NSI in ATM and LBL

- Weakest constraints when

2 equal eigenvalues of H_{mat}

Friedland, Lunardini, Maltoni 04

- General parametrization for this case

$$H_{\text{mat}} = Q_{\text{rel}} U_{\text{mat}} D_{\text{mat}} U_{\text{mat}}^\dagger Q_{\text{rel}}^\dagger$$

$$\left\{ \begin{array}{l} Q_{\text{rel}} = \text{diag} (e^{i\alpha_1}, e^{i\alpha_2}, e^{-i\alpha_1 - i\alpha_2}), \\ U_{\text{mat}} = R_{12}(\varphi_{12}) R_{13}(\varphi_{13}), \\ D_{\text{mat}} = \sqrt{2} G_F N_e(r) \text{diag}(\varepsilon, 0, 0) \end{array} \right.$$

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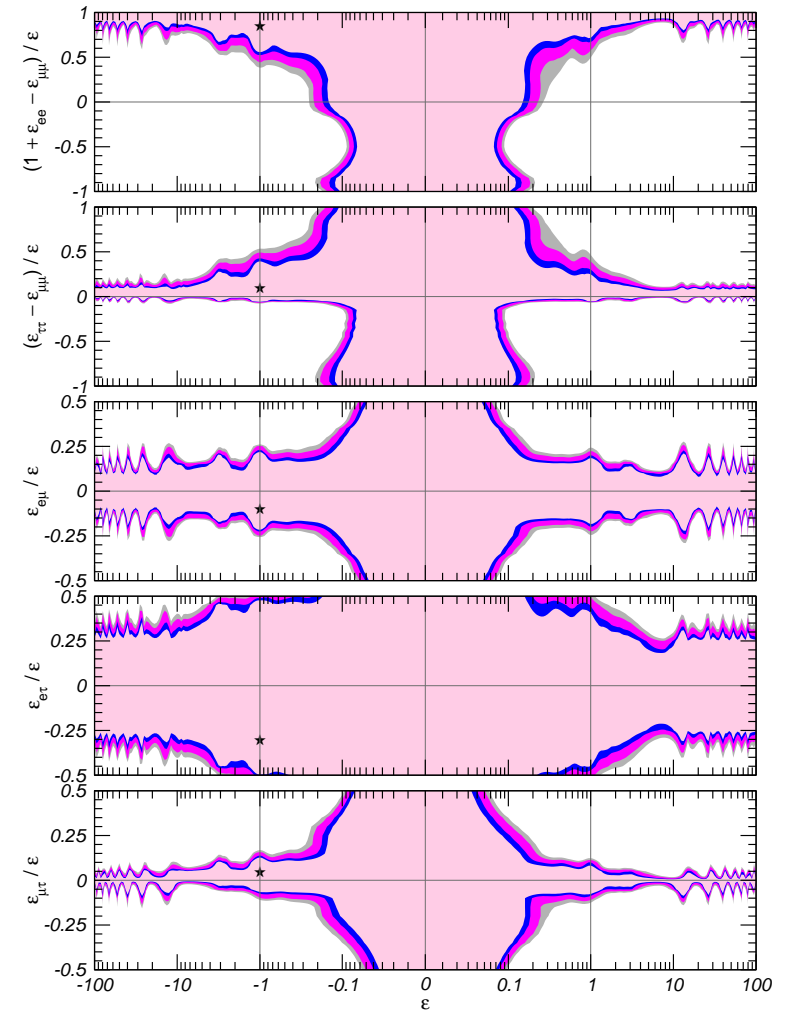
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So

$$\begin{aligned} \varepsilon_{ee} - \varepsilon_{\mu\mu} &= \varepsilon (\cos^2 \varphi_{12} - \sin^2 \varphi_{12}) \cos^2 \varphi_{13} - 1 \\ \varepsilon_{\tau\tau} - \varepsilon_{\mu\mu} &= \varepsilon (\sin^2 \varphi_{13} - \sin^2 \varphi_{12} \cos^2 \varphi_{13}) \\ \varepsilon_{e\mu} &= -\varepsilon \cos \varphi_{12} \sin \varphi_{12} \cos^2 \varphi_{13} e^{i(\alpha_1 - \alpha_2)} \\ \varepsilon_{e\tau} &= -\varepsilon \cos \varphi_{12} \cos \varphi_{13} \sin \varphi_{13} e^{i(2\alpha_1 + \alpha_2)} \\ \varepsilon_{\mu\tau} &= \varepsilon \sin \varphi_{12} \cos \varphi_{13} \sin \varphi_{13} e^{i(\alpha_1 + 2\alpha_2)} \end{aligned}$$

No bound on ε from ATM+LBL



Maltoni, MCG-G, Salvado ArXiv:1103.4265

Matter Potential/NSI in Solar and KamLAND

z-Garcia

- In $|\Delta m_{31}^2| \rightarrow \infty$: $P_{ee} = c_{13}^4 P_{\text{eff}} + s_{13}^4$

$$H_{\text{mat}}^{\text{eff}} = \sqrt{2}G_F N_e(r) \begin{pmatrix} c_{13}^2 & 0 \\ 0 & 0 \end{pmatrix} + \sqrt{2}G_F \sum_f N_f(r) \begin{pmatrix} -\varepsilon_D^f & \varepsilon_N^f \\ \varepsilon_N^{f*} & \varepsilon_D^f \end{pmatrix}$$

$$\begin{aligned} \varepsilon_D^f &= c_{13}s_{13}\text{Re} \left[e^{i\delta_{\text{CP}}} \left(s_{23}\varepsilon_{e\mu}^f + c_{23}\varepsilon_{e\tau}^f \right) \right] \\ &- \left(1 + s_{13}^2 \right) c_{23}s_{23}\text{Re} \left(\varepsilon_{\mu\tau}^f \right) \\ &- \frac{c_{13}^2}{2} \left(\varepsilon_{ee}^f - \varepsilon_{\mu\mu}^f \right) \\ &+ \frac{s_{23}^2 - s_{13}^2 c_{23}^2}{2} \left(\varepsilon_{\tau\tau}^f - \varepsilon_{\mu\mu}^f \right) \end{aligned}$$

$$\begin{aligned} \varepsilon_N^f &= c_{13} \left(c_{23}\varepsilon_{e\mu}^f - s_{23}\varepsilon_{e\tau}^f \right) \\ &+ s_{13}e^{-i\delta_{\text{CP}}} \left[s_{23}^2\varepsilon_{\mu\tau}^f - c_{23}^2\varepsilon_{\mu\tau}^{f*} \right. \\ &\left. + c_{23}s_{23} \left(\varepsilon_{\tau\tau}^f - \varepsilon_{\mu\mu}^f \right) \right] \end{aligned}$$

Matter Potential/NSI in Solar and KamLAND

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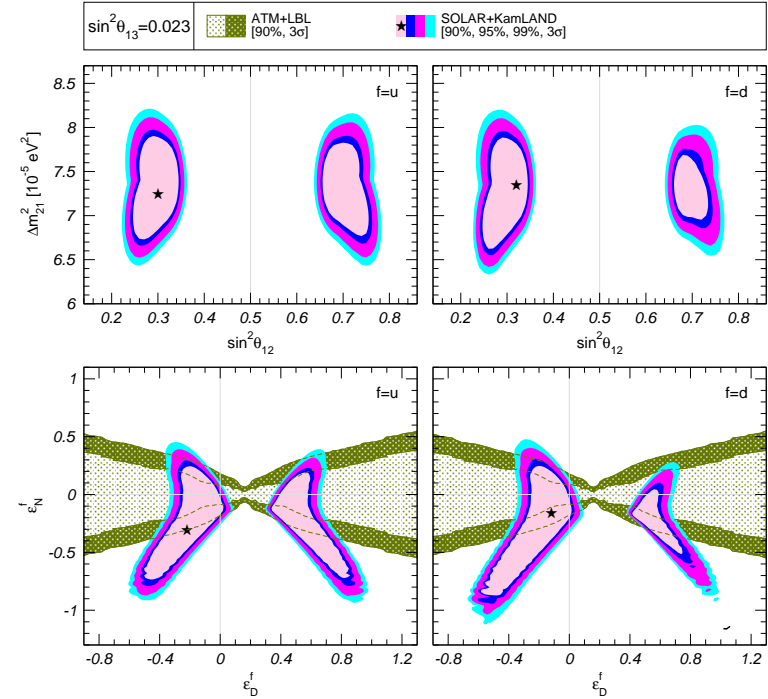
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- LMA and LMA-D ($\theta_{12} > \frac{\pi}{4}$) allowed



Matter Potential/NSI in Solar and KamLAND

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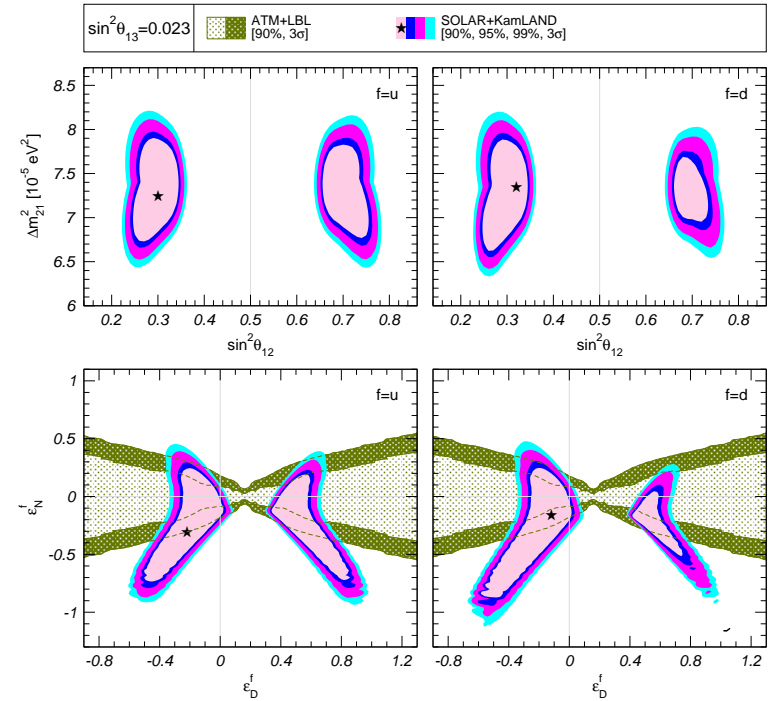
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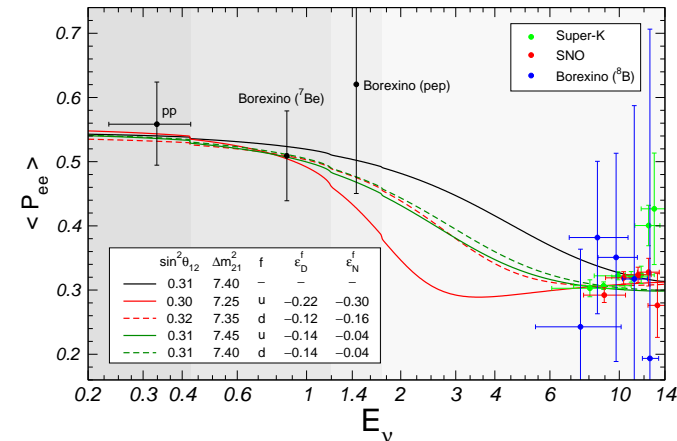
$$\varepsilon_D^f = c_{13}s_{13}\text{Re} \left[e^{i\delta_{\text{CP}}} (s_{23}\varepsilon_{e\mu}^f + c_{23}\varepsilon_{e\tau}^f) \right] - (1 + s_{13}^2)c_{23}s_{23}\text{Re}(\varepsilon_{\mu\tau}^f) - \frac{c_{13}^2}{2}(\varepsilon_{ee}^f - \varepsilon_{\mu\mu}^f) + \frac{s_{23}^2 - s_{13}^2 c_{23}^2}{2}(\varepsilon_{\tau\tau}^f - \varepsilon_{\mu\mu}^f)$$

$$\varepsilon_N^f = c_{13} \left(c_{23}\varepsilon_{e\mu}^f - s_{23}\varepsilon_{e\tau}^f \right) + s_{13}e^{-i\delta_{\text{CP}}} \left[s_{23}^2\varepsilon_{\mu\tau}^f - c_{23}^2\varepsilon_{\mu\tau}^{f*} + c_{23}s_{23}(\varepsilon_{\tau\tau}^f - \varepsilon_{\mu\mu}^f) \right]$$

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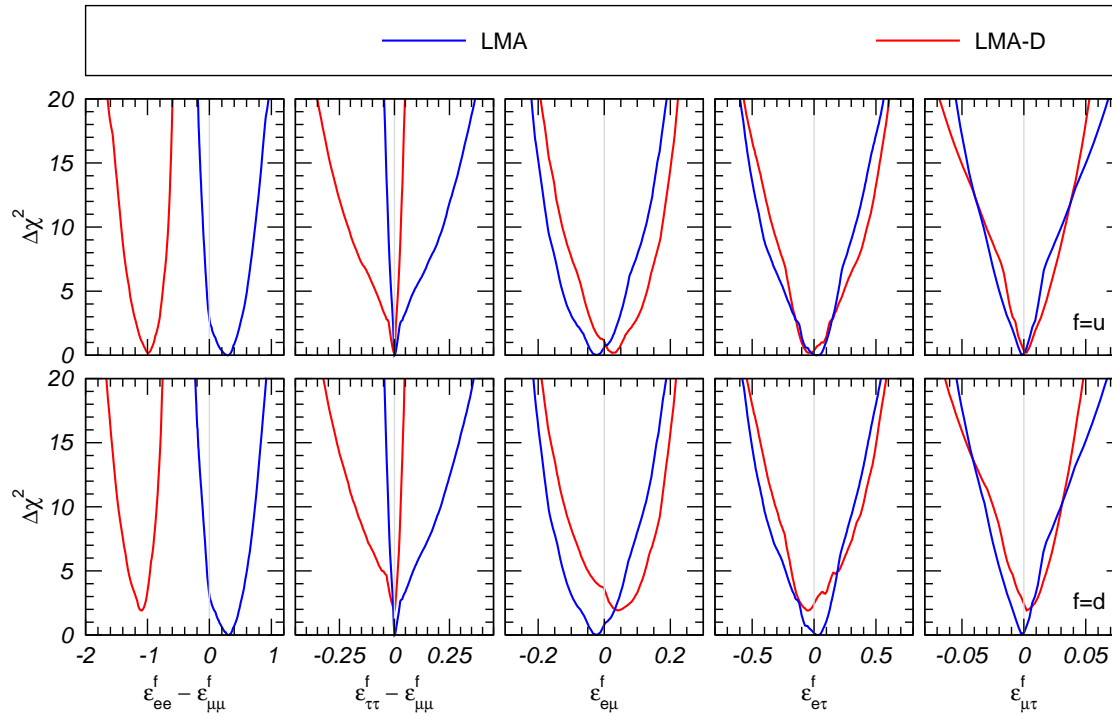
- Better fit with NSI ($\Delta\chi_{\text{osc}}^2 \simeq 5-7$)



Due to no observation of MSW up-turn

Matter Potential/NSI: Global Analysis

- All parameter space of matter potential is bounded



	90% CL			90% CL	
Param.	OSC	SCATT	Param.	OSC	SCATT
$ \varepsilon_{ee}^u $	0.51–1.19	0.7–1	$ \varepsilon_{ee}^d $	0.51–1.17	0.3–0.7
$ \varepsilon_{\tau\tau}^u $	0.03	1.4–3	$ \varepsilon_{\tau\tau}^d $	0.03	1.1–6
$ \varepsilon_{e\mu}^u $	0.09	0.05	$ \varepsilon_{e\mu}^d $	0.09	0.05
$ \varepsilon_{e\tau}^u $	0.15	0.5	$ \varepsilon_{e\tau}^d $	0.14	0.5
$ \varepsilon_{\mu\tau}^u $	0.01	0.05	$ \varepsilon_{\mu\tau}^d $	0.01	0.05

Bounds from global osc fit
stronger than scattering ones
for $\varepsilon_{\tau\beta}^{u,d}$

Summary

- First TAUP with the three leptonic mixing angles determined (at $\pm 3\sigma/6$)

$$\begin{array}{llll}
 \Delta m_{21}^2 = 7.44 \times 10^{-5} \text{ eV}^2 \text{ (2.3\%)} & \Delta m_{31}^2 = 2.45 \times 10^{-3} \text{ eV}^2 \text{ NO} & & (2.6\%) \\
 & |\Delta m_{32}^2| = 2.43 \times 10^{-3} \text{ eV}^2 \text{ IO} & & \\
 \sin^2 \theta_{12} = 0.3 \text{ (4\%)} & \sin^2 \theta_{23} = \begin{array}{l} 0.59 \text{ IO} \\ 0.44 \text{ NO} \end{array} \text{ (8.2\%)} & & \sin^2 \theta_{13} = 0.023 \text{ (9.6\%)}
 \end{array}$$

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- Still **ignore** or **not significantly determined** (But interesting interplay LBL/REACT)

Majorana or Dirac? θ_{23} Octant

Absolute ν mass Normal or Inverted ? CP violation in leptons?

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- Purely empirical determination of matter potential

\Rightarrow strongest constraints on vector NSI of ν_τ